### Scilab Textbook Companion for Digital Signal Processing: Principle, Algorithms And Applications by J. G. Proakis And D. G. Manolakis<sup>1</sup>

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## **Book Description**

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Scilab numbering policy used in this document and the relation to the above book.

Exa Example (Solved example)

Eqn Equation (Particular equation of the above book)

**AP** Appendix to Example(Scilab Code that is an Appednix to a particular Example of the above book)

For example, Exa 3.51 means solved example 3.51 of this book. Sec 2.3 means a scilab code whose theory is explained in Section 2.3 of the book.

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Exa 8.03.6	Graphical
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### Chapter 1

## Introduction

Scilab code Exa 1.2.1 Discrete Time Signal

```
1 //Graphical//
2 //Implementation of Equation 1.2.1 in Chapter 1
3 //Digital Signal Processing by Proakis, Third
Edition, PHI
4 //Page 9
5
6 clear; clc; close;
7 n = 0:10;
8 x = (0.8)^n;
9 //plot2d4(n,x)
10 a=gca();
11 a.thickness = 2;
12 plot2d3('gnn',n,x)
13 xtitle('Graphical Representation of Discrete Time
Signal', 'n', 'x[n]');
```

### Chapter 2

## Discrete Time Signals and Systems

Scilab code Exa 2.1.2 Signal advanced version

```
1 // Graphical//
2 //Implementation of Eample 2.1.2 in Chapter 2
3 // Digital Signal Processing by Proakis, Third
        Edition, PHI
4 //Page 52
\mathbf{5}
6
7 clear;
8 clc;
9 close;
10
11 \quad x = [0 \quad 0 \quad 0 \quad -1 \quad 0 \quad 1 \quad 2 \quad 3 \quad 4 \quad 5 \quad 5 \quad 5 \quad 5 \quad 5];
12
13 x1 = [0 \ 0 \ 0 \ x]; //x(n-3)
14
                                    //x(n+2)
15 x2 = [x 0 0];
16
17
18 a=gca();
```

```
19 a.thickness = 2;
20 a.y_location = "middle";
21 a.x_location = "middle"
22
23 subplot(3,1,1)
24 a=gca();
25 a.thickness = 2;
26 a.y_location = "middle";
27 a.x_location = "middle"
28 plot2d3('gnn',1:length(x),x)
29 xtitle('Graphical Representation of signal x', ' --->
      n', ' = x [n]';
30
31 subplot(3,1,2)
32 \ a = gca();
33 a.thickness = 2;
34 a.y_location = "middle";
35 a.x_location = "middle"
36 plot2d3('gnn',x1)
37 xtitle('Graphical Representation of signal delayed
      version of x', ' ---> n', ' --->x[n-3]');
38
39 subplot(3,1,3)
40 \ a = gca();
41 a.thickness = 2;
42 a.y_location = "middle";
43 a.x_location = "middle"
44 plot2d3('gnn',x2)
45 xtitle('Graphical Representation of signal advanced
      version of x', ' ---> n', ' --->x[n+2]');
```

#### Scilab code Exa 2.1.6 Unit Sample Sequence

```
1 //Graphical//
2 //Implementation of Equation 2.1.6 in Chapter 2
```

```
3 // Digital Signal Processing by Proakis, Third
Edition, PHI
4 // Page 45
5
6 clear; clc; close;
7 L = 4; // Upperlimit
8 n = -L:L;
9 x = [zeros(1,L),1,zeros(1,L)];
10 a=gca();
11 a.thickness = 2;
12 a.y_location = "middle";
13 plot2d3('gnn',n,x)
14 xtitle('Graphical Representation of Unit Sample
Sequence', 'n', 'x[n]');
```

Scilab code Exa 2.1.7 Unit Step Signal

```
1 //Graphical//
2 //Implementation of Equation 2.1.7 in Chapter 2
3 // Digital Signal Processing by Proakis, Third
     Edition, PHI
4 //Page 45
5
6 clear; clc; close;
7 L = 4; // Upperlimit
8 n = -L:L;
9 x = [zeros(1,L), ones(1,L+1)];
10 a=gca();
11 a.thickness = 2;
12 a.y_location = "middle";
13 plot2d3('gnn',n,x)
14 xtitle('Graphical Representation of Unit Step Signal
     ', 'n', 'x[n]');
```

Scilab code Exa 2.1.8 Unit Ramp Signal

```
1 //Graphical//
2 //Implementation of Equation 2.1.8 in Chapter 2
3 // Digital Signal Processing by Proakis, Third
     Edition, PHI
4 //Page 45
5
6 clear; clc; close;
7 L = 4; // Upperlimit
8 n = -L:L;
9 x = [zeros(1,L), 0:L];
10 a=gca();
11 a.thickness = 2;
12 a.y_location = "middle";
13 plot2d3('gnn',n,x)
14 xtitle('Graphical Representation of Unit Ramp Signal
      ', 'n', 'x[n]');
```

Scilab code Exa 2.01.09 Exponential Increasing-Decreasing Signal

```
1 //Graphical//
2 //Implementation of Equation 2.01.09b in Chapter 2
3 //Digital Signal Processing by Proakis, Third
Edition, PHI
4 //Page 46
5 // a < 0
6 clear;
7 clc;
8 close;
9 a =-1.5;
10 n = 0:10;
```

```
11 x = (a)^n;
12 a=gca();
13 a.thickness = 2;
14 a.x_location = "origin";
15 a.y_location = "origin";
16 plot2d3('gnn',n,x)
17 xtitle('Graphical Representation of Exponential
Increasing-Decreasing Signal', 'n', 'x[n]');
```

Scilab code Exa 2.1.09 Exponential Decreasing Signal

```
1 //Graphical//
2 //Implementation of Equation 2.1.09c in Chapter 2
3 // Digital Signal Processing by Proakis, Third
     Edition, PHI
4 //Page 46
5 // a < 1
6 clear;
7 clc;
8 close;
9 a =0.5;
10 n = 0:10;
11 x = (a)^n;
12 a=gca();
13 a.thickness = 2;
14 a.x_location = "middle";
15 plot2d3('gnn',n,x)
16 xtitle('Graphical Representation of Exponential
     Decreasing Signal', 'n', 'x[n]');
```

Scilab code Exa 2.1.9 Exponential Signal

1 // Graphical//

```
2 //Implementation of Equation 2.1.9 in Chapter 2
3 // Digital Signal Processing by Proakis, Third
Edition, PHI
4 // Page 46
5 clear;
6 clc;
7 close;
8 a =1.5;
9 n =1:10;
10 x = (a)^n;
11 a=gca();
12 a.thickness = 2;
13 plot2d3('gnn',n,x)
14 xtitle('Graphical Representation of Exponential
Signal', 'n', 'x[n]');
```

#### Scilab code Exa 2.1.24 Even Signal

```
1 // Graphical //
2 //Implementation of Equation 2.1.24 in Chapter 2
3 // Digital Signal Processing by Proakis, Third
     Edition, PHI
4 //Page 51
5
6 clear; clc; close;
7 n = -7:7;
8 x1 = [0 0 0 1 2 3 4];
9 x = [x1,5,x1(length(x1):-1:1)];
10 a=gca();
11 a.thickness = 2;
12 a.y_location = "middle";
13 plot2d3('gnn',n,x)
14 xtitle('Graphical Representation of Even Signal', 'n'
     , 'x[n]');
```

Scilab code Exa 2.1.25 ODD Signal

```
1 // Graphical //
2 //Implementation of Equation 2.1.25 in Chapter 2
3 // Digital Signal Processing by Proakis, Third
      Edition, PHI
4 //Page 51
5 clear;
6 \quad clc;
7 close;
8 n = -5:5;
9 x1 = [0 1 2 3 4 5];
10 x = [-x1(\$:-1:2),x1];
11 a=gca();
12 a.thickness = 2;
13 a.y_location = "middle";
14 a.x_location = "middle"
15 plot2d3('gnn',n,x)
16 xtitle('Graphical Representation of ODD Signal','
                  n', '
                                     x[n]');
```

### Chapter 3

# The z Transformation and its Applications to the Analysis of LTI Systems

Scilab code Exa 3.1.0 Ztransfer

```
1 // Graphical//
2 function [Ztransfer]=ztransfer_new(sequence,n)
3 z = poly(0, 'z', 'r')
4 Ztransfer=sequence*(1/z)^n'
5 endfunction
```

Scilab code Exa 3.1.1 Z Transform of Finite Duration SIgnals

```
1 //Graphical//
2 //Example 3.1.1
3 //Z Transform of Finite Duration SIgnals
4 clear;
5 clc;
6 close;
```

```
7 function [Ztransfer] = ztransfer_new (sequence,n)
     z = poly (0, 'z', 'r'); Ztransfer = sequence
8
        *(1/z )^n'
9 endfunction
10 x1 = [1, 2, 5, 7, 0, 1];
11 n1 = 0: length(x1) - 1;
12 X1 = ztransfer_new(x1,n1)
13 x^2 = [1, 2, 5, 7, 0, 1];
14 \ n2 = -2:3;
15 X2 = ztransfer_new(x2,n2)
16 x3 = [0, 0, 1, 2, 5, 7, 0, 1];
17 n3 = 0: length(x3) - 1;
18 X3 = ztransfer_new(x3,n3)
19 x4 = [2, 4, 5, 7, 0, 1];
20 \quad n4 = -2:3;
21 X4 = ztransfer_new(x4,n4)
22 x5 = [1,0,0]; //S(n) Unit Impulse sequence
23 n5 = 0: length(x5) - 1;
24 X5 = ztransfer_new(x5, n5)
25 x6 = [0,0,0,1]; //S(n-3) unit impulse sequence
      shifted
26 n6 = 0: length(x6) - 1;
27 \text{ X6} = \text{ztransfer}_{\text{new}}(\text{x6,n6})
28 x7 = [1,0,0,0]; //S(n+3) Unit impulse sequence
      shifted
29 n7 = -3:0;
30 X7 = ztransfer_new(x7,n7)
```

Scilab code Exa 3.1.2 Z transform of x[n] = (0.5)^n. u[n]

```
1 //Graphical//
2 //Example 3.1.2
3 //Z transform of x[n] = (0.5)^n. u[n]
4 clear;
5 clc;
```

```
6 close;
7 syms n z;
8 x=(0.5)^n
9 X=symsum(x*(z^(-n)),n,0,%inf)
10 disp(X,"ans=")
```

Scilab code Exa 3.1.4 Z transform of x[n] = -alpha^n. u[-n-1]

```
1 //Graphical//
2 //Example 3.1.4
3 //Z transform of x[n] = -alpha^n. u[-n-1]
4 //alpha = 0.5
5 clear;
6 close;
7 clc;
8 syms n z;
9 x=-(0.5)^(-n)
10 X=symsum(x*(z^(n)),n,1,%inf)
11 disp(X,"ans=")
```

Scilab code Exa 3.1.5 Z transform of x[n] = a^n.u[n]+b^n.u[-n-1]

```
1 // Graphical//
2 // Example 3.1.5
3 //Z transform of x[n] = a^n.u[n]+b^n.u[-n-1]
4 //a = 0.5 and b = 0.6
5 clear;
6 close;
7 clc;
8 syms n z;
9 x1=(0.5)^(n)
10 X1=symsum(x1*(z^(-n)),n,0,%inf)
11 x2=(0.6)^(-n)
```

```
12 X2=symsum(x2*(z^(n)),n,1,%inf)
13 X = (X1+X2)
14 disp(X,"ans=")
```

Scilab code Exa 3.2.01 Z transform of x[n] = 3.2<sup>n</sup>.u[n]-4.3<sup>n</sup>.u[n]

```
1 //Graphical//
2 //Example 3.2.01
3 //Z transform of x[n] = 3.2^n.u[n]-4.3^n.u[n]
4 clear;
5 close;
6 clc;
7 syms n z;
8 x1=(2)^(n)
9 X1=symsum(3*x1*(z^(-n)),n,0,%inf)
10 x2=(3)^(n)
11 X2=symsum(4*x2*(z^(-n)),n,0,%inf)
12 X = (X1-X2)
13 disp(X,"ans=")
```

Scilab code Exa 3.2.1 Z transform of x[n] = 3.2<sup>n</sup>.u[n]-4.3<sup>n</sup>.u[n]

```
1 // Graphical//
2 // Example 3.2.1
3 //Z transform of x[n] = 3.2^n.u[n]-4.3^n.u[n]
4 clear;
5 close;
6 clc;
7 syms n z;
8 x1=(2)^(n)
9 X1=symsum(3*x1*(z^(-n)),n,0,%inf)
10 x2=(3)^(n)
11 X2=symsum(4*x2*(z^(-n)),n,0,%inf)
```

12 X = (X1-X2) 13 disp(X,"ans=")

Scilab code Exa 3.2.2 Z transform of x[n] = cos(Wo.n).u[n]

```
1 // Graphical //
2 //Example 3.2.2
3 //Z transform of x[n] = cos(Wo.n).u[n]
4 //Z transform of y[n] = sin(Wo.n).u[n]
5 clear;
6 close;
7 \text{ clc};
8 syms n z;
9 Wo =2;
10 x1=\exp(sqrt(-1)*Wo*n);
11 X1=symsum(x1*(z^(-n)),n,0,%inf);
12 x2 = \exp(-sqrt(-1) * Wo * n);
13 X2=symsum(x2*(z^(-n)),n,0,%inf)
14 X = (X1 + X2)
15 disp(X,"ans=")
16 Y = (1/(2*sqrt(-1)))*(X1-X2)
17 disp(Y, "ans=")
```

Scilab code Exa 3.2.3 Time Shifting Property of Z-transform

```
1 // Graphical//
2 // Example 3.2.3
3 // Time Shifting Property of Z-transform
4 clear;
5 clc;
6 close;
7 function [Ztransfer]= ztransfer_new (sequence,n)
```

```
8 z = poly (0, 'z', 'r'); Ztransfer = sequence
	*(1/z)^n'
9 endfunction
10 x1 = [1,2,5,7,0,1];
11 n1 = 0:length(x1)-1;
12 X1 = ztransfer_new(x1,n1)
13 //x2 = [1,2,5,7,0,1];
14 n2 = 0-2:length(x1)-1-2;
15 X2 = ztransfer_new(x1,n2)
16 //x3 = [0,0,1,2,5,7,0,1];
17 n3 = 0+2:length(x1)-1+2;
18 X3 = ztransfer_new(x1,n3)
```

Scilab code Exa 3.2.4 Z transform of x[n] = u[n]

```
1 // Graphical//
2 // Example 3.2.4
3 //Z transform of x[n] = u[n]
4 clear;
5 clc;
6 close;
7 syms n z;
8 x=(1)^n
9 X=symsum(x*(z^(-n)),n,0,%inf)
10 disp(X,"ans=")
```

Scilab code Exa 3.2.6 Z transform of x[n] = u[-n]

```
1 //Graphical//
2 //Example 3.2.6
3 //Z transform of x[n] = u[-n]
4 clear;
5 clc;
```

```
6 close;
7 syms n z;
8 x=(1)^n
9 X=symsum(x*(z^(n)),n,0,%inf)
10 disp(X,"ans=")
```

Scilab code Exa 3.2.7 Z transform of x[n] = n.a<sup>n.u</sup>[n]

```
1 //Graphical//
2 //Example 3.2.7
3 //Z transform of x[n] = n.a^n.u[n]
4 clear;
5 clc;
6 close;
7 syms n z;
8 x=(1)^n;
9 X=symsum(x*(z^(-n)),n,0,%inf)
10 disp(X,"ans=")
11 Y = diff(X,z)
```

Scilab code Exa 3.2.9 Convolution Property Proof

```
1 // Graphical//
2 // Example 3.2.9
3 // Convolution Property Proof
4 clear;
5 clc;
6 close;
7 function [Ztransfer]= ztransfer_new (sequence,n)
8 z = poly (0, 'z', 'r'); Ztransfer = sequence
        *(1/z)^n'
9 endfunction
10 x1 = [1,-2,1];
```

```
11 n1 = 0:length(x1)-1;
12 X1 = ztransfer_new(x1,n1)
13 x2 = [1,1,1,1,1,1];
14 n2 = 0:length(x2)-1;
15 X2 = ztransfer_new(x2,n2)
16 X = X1.*X2
```

Scilab code Exa 3.2.10 Correlation Property Proof

```
1 // Graphical//
2 // Example 3.2.10
3 // Correlation Property Proof
4 syms n z;
5 x1 = (0.5)^n
6 X1 = symsum(x1*(z^(-n)),n,0,%inf)
7 X2 = symsum(x1*(z^(n)),n,0,%inf)
8 disp(X1,"X1 =")
9 disp(X2,"X2 =")
10 X = X1*X2
11 disp(X,"X=")
12 // Result
13 // Which is equivalent to Rxx(Z) = 1/(1-0.5(z+z^-1))
+(0.5^2))
14 // i.e for a = 0.5 Rxx(Z) = 1/(1-a(z+z^-1)+(a^2))
```

### Chapter 4

## Frequency Analysis of Signal and Systems

Scilab code Exa 4.1.2 Continuous Time Fourier Transform

```
1 // Graphical//
2 //Example 4.1.2 Continuous Time Fourier Transform
3 //and Energy Density Function of a Square Waveform
4 // x(t) = A, from -T/2 to T/2
5 clear;
6 \, \operatorname{clc};
7 close;
8 // Analog Signal
9 A =1; //Amplitude
10 Dt = 0.005;
11 T = 4; //Time in seconds
12 t = -T/2:Dt:T/2;
13 for i = 1:length(t)
14
     xa(i) = A;
15 \text{ end}
16 //
17 // Continuous-time Fourier Transform
18 Wmax = 2*%pi*2;
                           //Analog Frequency = 2Hz
19 K = 4; k = 0:(K/800):K;
```

```
20 W = k*Wmax/K;
21 disp(size(xa))
22 Xa=xa'*exp(-sqrt(-1)*t'*W)*Dt;
23 Xa = real(Xa);
24 W = [-mtlb_fliplr(W), W(2:501)]; // Omega from -Wmax
       to Wmax
25 Xa = [mtlb_fliplr(Xa), Xa(2:501)];
26 ESD = Xa<sup>2</sup>; //Energy Density Spectrum
27 subplot(3,1,1);
28 plot(t,xa);
29 xlabel('t in msec.');
30 ylabel('xa(t)')
31 title('Analog Signal')
32 subplot(3,1,2);
33 plot(W/(2*%pi),Xa);
34 xlabel('Frequency in Hz');
35 ylabel('Xa(jW)')
36 title('Continuous-time Fourier Transform')
37 subplot(3,1,3);
38 plot(W/(2*%pi),ESD);
39 xlabel('Frequency in Hz');
40 ylabel('SXX')
41 title('Energy Density Spectrum')
```

#### Scilab code Exa 4.02.7 Plotting Discrete Time Fourier Transform

```
1 //Graphical//
2 //Example 4.02.7 Sampling a Nonbandlimited Signal
3 //Plotting Discrete Time Fourier Transform of
4 //Discrete Time Signal x(nT)= exp(-A*T*abs(n))
5 clear;
6 clc;
7 close;
8 // Analog Signal
9 A =1; //Amplitude
```

```
10 Dt = 0.005;
11 t = -2:Dt:2;
12 //Continuous Time Signal
13 xa = \exp(-A*abs(t));
14 // Discrete Time Signal
15 Fs =input('Enter the Sampling Frequency in Hertz');
     //Fs = 1Hz(or) 20Hz
16 Ts = 1/Fs;
17 n = -5:1:5;
18 nTs = n*Ts;
19 x = \exp(-A*abs(nTs));
20 // Analog Signal reconstruction
21 \text{ Dt} = 0.005;
22 t = -2:Dt:2;
23 Xa = x *sinc_new(Fs*(ones(length(nTs),1)*t-nTs'*ones
      (1, length(t)));
24 // check
25 \text{ error} = \max(\text{abs}(Xa - xa))
26 subplot(2,1,1);
27 a = gca();
28 a.x_location = "origin";
29 a.y_location = "origin";
30 plot(t,xa);
31 xlabel('t in msec.');
32 ylabel('xa(t)')
33 title('Original Analog Signal')
34 subplot(2,1,2);
35 \ a = gca();
36 a.x_location = "origin";
37 a.y_location = "origin";
38 xlabel('t in msec.');
39 ylabel('xa(t)')
40 title('Reconstructed Signal from x(n) using sinc
      function ');
41 plot(t,Xa);
```

check Appendix AP 1 for dependency: sinc\_new4\_02\_7.sci

Scilab code Exa 4.2.07 Sampling a Nonbandlimited Signal

```
1 //Graphical//
2 //Example 4.2.07 Sampling a Nonbandlimited Signal
3 // Plotting Discrete Time Fourier Transform of
4 // Discrete Time Signal x(nT) = \exp(-A*T*abs(n))
5 clear;
6 \text{ clc};
7 close;
8 // Analog Signal
9 A =1;
           //Amplitude
10 Dt = 0.005;
11 t = -2:Dt:2;
12 //Continuous Time Signal
13 xa = \exp(-A*abs(t));
14 //Discrete Time Signal
15 Fs =input('Enter the Sampling Frequency in Hertz');
     //Fs = 2Hz(or) 20Hz
16 Ts = 1/Fs;
17 n = -5:1:5;
18 x = \exp(-A*abs(n*Ts));
19 // Discrete-time Signal
20 // Discrete-time Fourier transform
21 \text{ K} = 500;
22 k = 0:1:K;
23 w = %pi*k/K;
24 X = x * exp(-sqrt(-1)*n'*w);
25 X = real(X);
26 w = [-mtlb_fliplr(w), w(2:K+1)]; // Omega from -w to
      W
27 X = [mtlb_fliplr(X), X(2:K+1)];
28 subplot(3,1,1);
29 plot(t,xa );
30 xlabel('t in msec.');
```

```
31 ylabel('xa(t)')
32 title('Analog Signal')
33 subplot(3,1,2);
34 plot2d3('gnn',n,x )
35 xlabel('Discrete Time n.');
36 ylabel('x(nT)')
37 title('Discrete Signal');
38 subplot(3,1,3);
39 plot(w/(2*%pi),X);
40 xlabel('Frequency in pi units');
41 ylabel('X(w)')
42 title('Discrete-time Fourier Transform')
```

```
Scilab code Exa 4.2.7 Plotting Continuous Time Fourier Transform
```

```
1 // Graphical//
2 //Example 4.2.7 Sampling a Nonbandlimited Signal
3 // Plotting Continuous Time Fourier Transform of
4 // Continuous Time Signal x(t) = \exp(-A*abs(t))
5 clear;
6 \text{ clc};
7 close;
8 // Analog Signal
9 A =1; //Amplitude
10 Dt = 0.005;
11 t = -2:Dt:2;
12 xa = \exp(-A*abs(t));
13 //
14 // Continuous-time Fourier Transform
15 Wmax = 2*%pi*2;
                         //Analog Frequency = 2Hz
16 K = 4;
17 k = 0:(K/500):K;
18 W = k*Wmax/K;
19 Xa = xa * exp(-sqrt(-1)*t'*W) * Dt;
20 Xa = real(Xa);
```

```
21 W = [-mtlb_fliplr(W), W(2:501)]; // Omega from -Wmax
      to Wmax
22 Xa = [mtlb_fliplr(Xa), Xa(2:501)];
23 subplot(2,1,1);
24 a =gca();
25 a.x_location = "origin";
26 a.y_location = "origin";
27 plot(t,xa);
28 xlabel('t in msec.');
29 ylabel('xa(t)')
30 title('Analog Signal')
31 subplot(2,1,2);
32 \ a = gca();
33 a.x_location = "origin";
34 a.y_location = "origin";
35 plot(W/(2*%pi),Xa);
36 xlabel('Frequency in Hz');
37 ylabel('Xa(jW) * 1000')
38 title('Continuous-time Fourier Transform')
```

#### Scilab code Exa 4.3.4 Convolution Property Example

```
1 //Graphical//
2 //Example 4.3.4
3 //Convolution Property Example
4 //x1(n)=x2(n)= [1,1,1]
5 clear;
6 clc;
7 close;
8 n =-1:1;
9 x1 = [1,1,1];
10 x2 = x1;
11 //Discrete-time Fourier transform
12 K = 500;
13 k = 0:1:K;
```

```
14 w = %pi*k/K;
15 X1 = x1 * \exp(-\operatorname{sqrt}(-1)*n'*w);
16 X2 = x2 * exp(-sqrt(-1)*n'*w);
17 w = [-mtlb_fliplr(w), w(2:K+1)]; // Omega from -w to
       W
18 X1 = [mtlb_fliplr(X1), X1(2:K+1)];
19 X2 = [mtlb_fliplr(X2), X2(2:K+1)];
20 \quad \text{Freq}_X1 = \text{real}(X1);
21 Freq_X2 = real(X2);
22 X = X1.*X2;
23 K1 = length(X)
24 k1 = 0:1:K1;
25 w1 = \%pi*k1/K1;
26 \text{ w1} = [-2*\text{mtlb_fliplr(w)}, 2*\text{w}];
27 X = [mtlb_fliplr(X), X(1:K1)];
28 \operatorname{Freq}X = \operatorname{real}(X);
29 //Inv_X = X.*exp(sqrt(-1)*n'*w)
30 x = convol(x1, x2)
31 // Plotting Magitude Responses
32 figure(1)
33 a =gca();
34 a.x_location = 'middle'
35 a.y_location = 'middle'
36 a.x_label
37 a.y_label
38 plot2d(w/%pi,Freq_X1)
39 x_label =a.x_label
40 y_label = a.y_label
                                     Frequency in Radians'
41 x_label.text = '
                                                       X1(w)
42 y_label.text ='
43 //xlabel('Frequency in Radians')
44 // ylabel ('X1(w)')
45 title('Frequency Response')
46 \text{ figure}(2)
47 a =gca();
48 a.x_location = 'middle'
49 a.y_location = 'middle'
50 a.x_label
```

```
51 a.y_label
52 plot2d(w/%pi,Freq_X2)
53 x_label =a.x_label
54 y_label = a.y_label
55 x_label.text = '
                                              Frequency
     in Radians'
56 y_label.text = '
                                                X2(w)
57 title('Frequency Response')
58 figure(3)
59 a =gca();
60 a.y_location = 'middle'
61 a.x_label
62 a.y_label
63 plot2d(w1/(2*%pi),Freq_X)
64 x_label =a.x_label
65 y_label = a.y_label
66 x_label.text = '
                                              Frequency
     in Radians'
67 y_label.text ='
                                                 X(w)
68 title('Frequency Response')
```

Scilab code Exa 4.4.2 Frequency Response of Three point Moving Average System

```
1 //Graphical//
2 //Example 4.4.2
3 //Frequency Response of Three point Moving Average
System
4 //y(n)= (1/3) [x(n+1)+x(n)+x(n-1)]
5 //h(n) = [1/3,1/3,1/3]
6 clear;
7 clc;
8 close;
9 //Calculation of Impulse Response
```

```
10 n = -1:1;
11 h = [1/3, 1/3, 1/3];
12 // Discrete-time Fourier transform
13 K = 500;
14 k = 0:1:K;
15 w = %pi * k/K;
16 H = h * exp(-sqrt(-1)*n'*w);
17 //phasemag used to calculate phase and magnitude in
     dB
18 [Phase_H,m] = phasemag(H);
19 H = abs(H);
20 subplot(2,1,1)
21 plot2d(w/%pi,H)
22 xlabel('Frequency in Radians')
23 ylabel('abs(H)')
24 title('Magnitude Response')
25 subplot(2,1,2)
26 plot2d(w/%pi,Phase_H)
27 xlabel('Frequency in Radians')
28 ylabel('<(H)')
29 title('Phase Response')
```

Scilab code Exa 4.4.4 Frequency Response of First Order Difference Equation

```
1 //Graphical//
2 //Example 4.4.4
3 //Frequency Response of First Order Difference
    Equation
4 //a = 0.9 and b = 1-a
5 //Impulse Response h(n) = b.(a^n).u(n)
6 clear;
7 clc;
8 close;
9 a = input('Enter the constant value of Ist order
    Difference Equation');
```

```
10 b= 1-a;
11 // Calculation of Impulse Response
12 n =0:50;
13 h =b*(a.^n) ;
14 // Discrete-time Fourier transform
15 K = 500;
16 k = 0:1:K;
17 w = %pi*k/K;
18 H = h * exp(-sqrt(-1)*n'*w);
19 //phasemag used to calculate phase and magnitude in
     dB
20 [Phase_H,m] = phasemag(H);
21 H = real(H);
22 subplot(2,1,1)
23 plot2d(w/%pi,H)
24 xlabel('Frequency in Radians')
25 ylabel('abs(H)')
26 title('Magnitude Response')
27 subplot(2,1,2)
28 plot2d(w/%pi,Phase_H)
29 xlabel('Frequency in Radians')
30\, ylabel( '\!<\!(H) ')
31 title('Phase Response')
```

### Chapter 5

# Discrete Fourier Transform its Properties and Applications

Scilab code Exa 5.1.2 Determination of N-point DFT

```
1 // Graphical //
2 //Example 5.1.2
3 // Determination of N-point DFT
4 // Plotting Magnitude and Phase spectrum
5 clear;
6 \, \operatorname{clc};
7 close;
8 L = 10; // Length of the sequence
9 N = 10; // N -point DFT
10 for n = 0: L-1
11
     x(n+1) = 1;
12 end
13 //Computing DFT and IDFT
14 X = fft(x, -1)
15 x_{inv} = abs(fft(X,1))
16 //Computing Magnitude and Phase Spectrum
17 //Using DTFT
18 n = 0:L-1;
19 K = 500;
```

```
20 \ k = 0:1:K;
21 w = 2*%pi*k/K;
22 X_W = x' * exp(-sqrt(-1)*n'*w);
23 Mag_X = abs(X_W);
24 //phasemag used to calculate phase and magnitude in
     dB
25 Phase_X = atan(imag(X_W), real(X_W))
26 subplot(2,1,1)
27 plot2d(w,Mag_X)
28 xlabel('Frequency in Radians')
29 ylabel(abs(X))
30 title('Magnitude Response')
31 subplot(2,1,2)
32 plot2d(w,Phase_X)
33 xlabel('Frequency in Radians')
34 ylabel('<(X)')
35 title('Phase Response')
```

#### Scilab code Exa 5.1.3 Finding DFT and IDFT

```
1 // Graphical //
2 // Example 5.1.3
3 // Finding DFT and IDFT
4 clear;
5 clc;
6 close;
7 L = 4; // Length of the sequence
8 N = 4; // N -point DFT
9 x = [0,1,2,3];
10 // Computing DFT
11 X = fft(x,-1)
12 // Computing IDFT
13 x_inv = real(fft(X,1))
```
Scilab code Exa 5.2.1 Performing Circular COnvolution

```
1 //Graphical//
2 / Example 5.2.1 and Example 5.2.2
3 // Performing Circular COnvolution
4 //Using DFT
5 clear;
6 \, \text{clc};
7 close;
8 L = 4; //Length of the Sequence
9 N = 4; // N -point DFT
10 x1 = [2, 1, 2, 1];
11 x^2 = [1, 2, 3, 4];
12 //Computing DFT
13 X1 = fft(x1,-1)
14 X2 = fft(x2, -1)
15 // Multiplication of 2 DFTs
16 X3 = X1.*X2
17 // Circular Convolution Result
18 x3 = abs(fft(X3,1))
```

Scilab code Exa 5.3.1 Performing Linear Filtering (i.e) Linear Convolution

```
1 // Graphical//
2 // Example 5.3.1
3 // Performing Linear Filtering (i.e) Linear
Convolution
4 // Using DFT
5 clear;
6 clc;
7 close;
8 h = [1,2,3]; // Impulse Response of LTI System
```

```
//Input Response of LTI System
9 x = [1, 2, 2, 1];
10 N1 = length(x)
11 N2 = length(h)
12 disp('Length of Output Response y(n)')
13 N = N1 + N2 - 1
14 //Padding zeros to Make Length of 'h' and 'x'
15 //Equal to length of output response 'y'
16 \text{ h1} = [h, \text{zeros}(1, 8-N2)]
17 \text{ x1} = [x, \text{zeros}(1, 8-N1)]
18 //Computing DFT
19 H = fft(h1, -1)
20 X = fft(x1, -1)
21 // Multiplication of 2 DFTs
22 Y = X . * H
23 //Linear Convolution Result
24 \text{ y} = abs(fft(Y,1))
25 for i =1:8
26
     if(abs(H(i))<0.0001)
        H(i) = 0;
27
28
     end
29
     if(abs(X(i))<0.0001)</pre>
30
        X(i) = 0;
31
     end
     if(abs(y(i))<0.0001)</pre>
32
33
        y(i) = 0;
34
     end
35 end
36 \operatorname{disp}(X, 'X=')
37 disp(H, 'H=')
38 disp(y, 'Output response using Convolution function ')
39 y = convol(x,h)
```

#### Scilab code Exa 5.4.1 Effect of Zero Padding

```
1 // Graphical//
```

```
2 / Example 5.4.1
3 // Effect of Zero Padding
4 clear;
5 \, \text{clc};
6 close;
7 L = 100; // Length of the sequence
8 N = 200; // N -point DFT
9 n = 0:L-1;
10 x = (0.95).^{n};
11 //Padding zeros to find N = 200 point DFT
12 \text{ x_padd} = [x, \text{zeros}(1, N-L)];
13 // Computing DFT
14 X = fft(x, -1);
15 X_padd = fft(x_padd, -1);
16 subplot(2,1,1)
17 plot2d(X)
18 xlabel('K')
19 ylabel('X(k)')
20 title('For L =100 and N =100')
21 subplot(2,1,2)
22 plot2d(X_padd)
23 xlabel('K')
24 ylabel('X(k) zero padded')
25 title('For L =100 and N =200')
```

## Chapter 6

# Efficient Computation of DFT Fast Fourier Transform and Algorithms

Scilab code Exa 6.4.1 Signal to Quantization Noise Ratio

```
1 //Graphical//
2 //Example 6.4.1
3 //Program to Calculate No.of bits required for given
4 //Signal to Quantization Noise Ratio
5 //in computing DFT
6 clear;
7 clc;
8 close;
9 N = 1024;
10 SQNR = 30; //SQNR = 30 dB
11 v = log2(N); //number of stages
12 b = (log2(10^(SQNR/10))+2*v)/2;
13 b = ceil(b)
14 disp(b, 'The number of bits required rounded to:')
```

Scilab code Exa 6.4.2 Signal to Quantization Noise Ratio

```
1 // Graphical//
2 // Example 6.4.2
3 // Program to Calculate No.of bits required for given
4 // Signal to Quantization Noise Ratio
5 // in FFT algorithm
6 clear;
7 clc;
8 close;
9 N = 1024;
10 SQNR = 30; //SQNR = 30 dB
11 v = log2(N); //number of stages
12 b = (log2(10^(SQNR/10))+v+1)/2;
13 b = ceil(b)
14 disp(b, 'The number of bits required rounded to:')
```

Scilab code Exa 6.8 DFT using DIF-FFT algorithm

```
1 //Graphical//
2 //Exercise 6.8
3 //Program to Calculate DFT using DIF-FFT algorithm
4 //x[n]= 1, 0<=n<=7
5 clear;
6 clc;
7 close;
8 x = [1,1,1,1,1,1,1];
9 X = fft(x,-1)
10 //Inverse FFT
11 x_inv = real(fft(X,1))
```

Scilab code Exa 6.11 DFT using DIF-FFT algorithm

```
1 // Graphical//
2 // Exercise 6.11
3 // Program to Calculate DFT using DIF-FFT algorithm
4 //x[n]= [1/2,1/2,1/2,1/2,0,0,0,0]
5 clear;
6 clc;
7 close;
8 x = [1/2,1/2,1/2,1/2,0,0,0,0];
9 X = fft(x,-1)
10 // Inverse FFT
11 x_inv = real(fft(X,1))
```

## Chapter 7

## Implementation of Discrete Time System

Scilab code Exa 6.4.17 Signal to Quantization Noise Ratio

```
1 // Graphical//
2 //Equation 6.4.17
3 //page492
4 //Program to Calculate Signal to Quantization Noise
      Ratio
5 //in FFT algorithm
6 clear;
7 \text{ clc};
8 close;
9 N = input('Enter the N point FFT value');
10 b = log2(N)
11 Quantization_Noise = (2/3)*(2^{(-2*b)})
12 Signal_Power = (1/(3*N))
13 SQNR = Signal_Power/Quantization_Noise
14 //RESULT
15 //Enter the N point FFT value 1024
16 // b = 10.
17 // Quantization_Noise =
                               0.000006
18 // Signal_Power = 0.0003255
```

```
19 // SQNR = 512.
20 //-->10*log10 (SQNR) = 27.0927
```

Scilab code Exa 7.6.3 Quantization Noise in FIR Filter

```
1 //Graphical//
2 //Example 7.6.3
3 //Program to Calculate Quantization Noise in FIR
Filter
4 //For M = 32 and No. of bits = 12
5 clear;
6 clc;
7 close;
8 b = input('Enter the number of bits');
9 M = input('Enter the FIR filter length');
10 disp('Coefficient Quantization Error in FIR Filter')
11 Sigma_e_square = (2^(-2*(b+1))*M/12)
```

Scilab code Exa 7.7.01 Determination of Variance of round-off noise

```
1 // Graphical //
2 // Example 7.7.01
3 // Determination of Variance of round-off noise
4 // at the output of cascade realization
5 //H1(Z) = 1/(1-(1/2)z-1)
6 //H2(Z) = 1/(1-(1/4)z-1)
7 //H(Z) = (2/(1-(1/2)z-1)) -(1/(1-(1/4)z-1))
8 clear;
9 clc;
10 close;
11 a1 = (1/2); // pole of first system in cascade
connection
```

```
12 a2 = (1/4); //ploe of second system in cascade
      connection
13 sigma_e = 1; //quantization noise variance
14 //Noise variance of H1(Z)
15 sigma_2 = (1/(1-a2^2))*sigma_e<sup>2</sup>//noise variance of
      second system
16 //Noise variance of H2(Z)
17 sigma_1 = 1/(1-a1^2)*sigma_e<sup>2</sup>//noise variance of
      first system
18 //Nosie variance of H(Z)
19 sigma = (((2<sup>2</sup>)/(1-a1<sup>2</sup>))-((2<sup>2</sup>)/(1-a1*a2))+(1/(1-a2
      ^2)))*sigma_e^2
20 noise_variance = sigma+sigma_2 //Total noise
      variance
21 //Result
22 / sigma_2 = 1.0666667
23 // sigma_1 = 1.3333333
24 // sigma = 1.8285714
25 //noise_variance =
                            2.8952381
```

Scilab code Exa 7.7.1 Dead band of First order Recursive System

```
1 //Graphical//
2 //Equation 7.7.1
3 //Program to find Dead band of First order Recursive
System
4 //y(n) = a y(n-1)+x(n); a = (1/2) and a = (3/4)
5 clear;
6 clc;
7 close;
8 a = input('Enter the constant value of first
Recursive system');
9 b = 4; //No. of bits used to represent
10 Dead_Band = (2^-b)*[(1/2)*(1/(1-a)),-(1/2)*(1/(1-a)))
1
```

11 // Result 12 // For a = (1/2)13 // Dead Band = [0.0625 - 0.0625]14 // For a = (3/4)15 // Dead Band = [0.125 - 0.125]

### Chapter 8

## **Design of Digital Filters**

Scilab code Exa 8.2.1 Graphical

```
1 // Graphical //
2 //Example 8.2.1
3 //Design of FIR Filter using Frequecny Sampling
      Technique
4 //Low Pass Filter Design
5 clear;
6 \quad clc;
7 close;
8 M = 15;
9 Hr = [1, 1, 1, 1, 0.4, 0, 0, 0];
10 for k =1:length(Hr)
11
       G(k) = ((-1)^{(k-1)} * Hr(k);
12 end
13 h = zeros(1, M);
14 \ U = (M-1)/2
15 \text{ for } n = 1:M
16
    h1 = 0;
17
     for k = 2: U+1
       h1 =G(k) cos((2*\%pi/M)*(k-1)*((n-1)+(1/2)))+h1;
18
19
     end
20
    h(n) = (1/M) * (G(1) + 2 * h1);
```

```
21 \text{ end}
22 h
23 [hzm,fr]=frmag(h,256);
24 \text{ hzm}_{dB} = 20 * \log 10 (\text{hzm}) . / \max(\text{hzm});
25 figure
26 plot(2*fr,hzm)
27 a=gca();
28 xlabel('Normalized Digital Frequency W');
29 ylabel('Magnitude');
30 title('Frequency Response Of FIR LPF using Frequency
       Sampling Technique with M = 15 with Cutoff
      Frequency = 0.466 ')
31 xgrid(2)
32 figure
33 plot(2*fr,hzm_dB)
34 a=gca();
35 xlabel('Normalized Digital Frequency W');
36 ylabel('Magnitude in dB');
37 title('Frequency Response Of FIR LPF using Frequency
       Sampling Technique with M = 15 with Cutoff
      Frequency = 0.466')
38 xgrid(2)
```

#### Scilab code Exa 8.2.2 Graphical

```
1 //Graphical//
2 //Example 8.2.2
3 //Design of FIR Filter using Frequeeny Sampling
    Technique
4 //Low Pass Filter Design
5 clear;
6 clc;
7 close;
8 M =32;
9 T1 = 0.3789795; //for alpha = 0 (Type I)
```

```
10 Hr = [1, 1, 1, 1, 1, 1, 1, T1, 0, 0, 0, 0, 0, 0, 0, 0, 0];
11 for k =1:length(Hr)
12
       G(k) = ((-1)^{(k-1)} * Hr(k);
13 end
14 h = zeros(1, M);
15 \ \text{U} = (M-1)/2
16 \text{ for } n = 1:M
     h1 = 0;
17
     for k = 2: U+1
18
       h1 =G(k)*cos((2*%pi/M)*(k-1)*((n-1)+(1/2)))+h1;
19
20
     end
21
    h(n) = (1/M) * (G(1) + 2 * h1);
22 end
23 h
24 [hzm,fr]=frmag(h,256);
25 \text{ hzm}_{dB} = 20 * \log 10 (\text{hzm}) . / \max(\text{hzm});
26 figure
27 plot(2*fr,hzm)
28 a = gca();
29 xlabel('Normalized Digital Frequency W');
30 ylabel('Magnitude');
31 title('Frequency Response Of FIR LPF using Frequency
       Sampling Technique with M = 15 with Cutoff
      Frequency = 0.466 ')
32 xgrid(2)
33 figure
34 plot(2*fr,hzm_dB)
35 a = gca();
36 xlabel('Normalized Digital Frequency W');
37 ylabel('Magnitude in dB');
38 title('Frequency Response Of FIR LPF using Frequency
       Sampling Technique with M = 15 with Cutoff
      Frequency = 0.466')
39 xgrid(2)
```

Scilab code Exa 8.2.3 Graphical

```
1 //Graphical//
2 //Example 8.2.3
3 //Low Pass FIlter of length M = 61
4 //Pass band Edge frequency fp = 0.1 and a Stop edge
      frequency fs = 0.15
5 // Choose the number of cosine functions and create
      a dense grid
6 // in [0, 0.1) and [0.15, 0.5)
7 //magnitude for pass band = 1 & stop band = 0 (i.e)
      \begin{bmatrix} 1 & 0 \end{bmatrix}
8 //Weighting function = \begin{bmatrix} 1 & 1 \end{bmatrix}
9 clear;
10 clc;
11 close;
12 hn=eqfir(61,[0 .1;.15 .5],[1 0],[1 1]);
13 [hm,fr]=frmag(hn,256);
14 disp('The Filter Coefficients are:')
15 hn
16 figure
17 plot(fr,hm)
18 xlabel('Normalized Digital Frequency fr');
19 ylabel('Magnitude');
20 title('Frequency Response of FIR LPF using REMEZ
      algorithm M=61')
21 figure
22 plot(.5*(0:255)/256,20*log10(frmag(hn,256)));
23 xlabel('Normalized Digital Frequency fr');
24 ylabel('Magnitude in dB');
25 title('Frequency Response of FIR LPF using REMEZ
      algorithm M=61')
```

Scilab code Exa 8.2.4 Graphical

```
1 //Graphical//
2 //Example 8.2.4
3 //Band Pass FIlter of length M = 32
4 //Lower Cutoff frequency fp = 0.2 and Upper Cutoff
      frequency fs = 0.35
5 // Choose the number of cosine functions and create
      a dense grid
6 // in [0, 0.1) and [0.2, 0.35] and [0.425, 0.5]
7 //magnitude for pass band = 1 & stop band = 0 (i.e)
      \begin{bmatrix} 0 & 1 & 0 \end{bmatrix}
8 //Weighting function = \begin{bmatrix} 10 & 1 & 10 \end{bmatrix}
9 clear;
10 clc;
11 close;
12 hn = 0;
13 \text{ hm} = 0;
14 hn=eqfir(32,[0.1;.2.35;.425.5],[0 1 0],[10 1 10])
      ;
15 [hm,fr]=frmag(hn,256);
16 disp('The Filter Coefficients are:')
17 hn
18 figure
19 plot(fr,hm)
20 \ a = gca();
21 xlabel('Normalized Digital Frequency fr');
22 ylabel('Magnitude');
23 title('Frequency Response of FIR BPF using REMEZ
      algorithm M=32')
24 xgrid(2)
25 figure
26 plot(.5*(0:255)/256,20*log10(frmag(hn,256)));
27 \ a = gca();
28 xlabel('Normalized Digital Frequency fr');
29 ylabel('Magnitude in dB');
30 title('Frequency Response of FIR BPF using REMEZ
      algorithm M=32')
31 xgrid(2)
```

Scilab code Exa 8.2.5 Graphical

```
1 // Graphical //
2 //Example 8.2.5
3 //Linear Phase FIR Differentiator of length M = 60
4 //Pass Band Edge frequency fp = 0.1
5 clear;
6 \, \text{clc};
7 close;
8 M =60;
9 tuo = (M/2) - 1;
10 \text{ Wc} = 0.1;
11 h = zeros(1, M);
12 \text{ for } n = 1:M
     if n \sim = M/2
13
       h(n) = \cos((n-1-tuo)*Wc)/(n-1-tuo);
14
15
     end
16 end
17 [hm,fr]=frmag(h,1024);
18 disp('The Filter Coefficients are:')
19 h
20 figure
21 plot(fr,hm/max(hm))
22 a = gca();
23 xlabel('Normalized Digital Frequency fr');
24 ylabel('Magnitude');
25 title('Frequency Response of FIR Differentiator for
     M=60')
26 xgrid(2)
```

Scilab code Exa 8.2.6 Graphical

```
1 //Graphical//
2 //Example 8.2.6
3 // Plotting Hibert Transformer of Length M = 31
4 // Default Window Rectangular Window
5 //Chebyshev approx default parameter = \begin{bmatrix} 0 & 0 \end{bmatrix}
6 clear;
7 clc;
8 close;
9 M =31; // Hibert Transformer Length = 31
10 tuo = (M-1)/2;
11 Wc = %pi;
12 h = zeros(1, M);
13 \text{ for } n = 1:M
      if n ~= ((M-1)/2)+1
14
        h(n) = (2/\% pi) * (sin((n-1-tuo) * Wc/2)^2)/(n-1-tuo)
15
16
      end
17 end
18 disp('The Hilbert Coefficients are:')
19 h
20 Rec_Window = ones(1,M);//Rectangular Window
      generation
21 h_Rec = h.*Rec_Window;//Windowing With Rectangular
      window
22 //Hamming Window geneartion
23 for n=1:M
24
     hamm_Window(n) = 0.54-0.46*\cos(2*\%pi*(n-1)/(M-1));
25 end
26 h_hamm = h.*hamm_Window'; //Windowing With hamming
      window;
27 //Hilbert Transformer using Rectangular window
28 [hm_Rec,fr]=frmag(h_Rec,1024);
29 \text{ hm}_{\text{Rec}} dB = 20 * \log 10 (\text{hm}_{\text{Rec}});
30 figure
31 plot(fr,hm_Rec_dB)
32 \ a = gca();
33 xlabel('Normalized Digital Frequency fr');
34 ylabel('Magnitude');
```

```
35 title('Frequency Response of FIR Hibert Transformer
	using Rectangular window for M=31')
36 xgrid(2)
37 // Hilbert Transformer using Hamming window
38 [hm_hamm,fr]=frmag(h_hamm,1024);
39 disp('The Hilbert Coefficients are:')
40 hm_hamm_dB = 20*log10(hm_hamm);
41 figure
42 plot(fr,hm_hamm_dB)
43 a =gca();
44 xlabel('Normalized Digital Frequency fr');
45 ylabel('Magnitude');
46 title('Frequency Response of FIR Hibert Transformer
	using hamming window for M=31')
47 xgrid(2)
```

Scilab code Exa 8.3.2 Graphical

```
1 //Graphical//
2 //Example 8.3.2
3 //mapping = (z-(z^-1))/T
4 //To convert analog filter into digital filter
5 clear;
6 clc;
7 close;
8 s = poly(0, 's');
9 H = 1/((s+0.1)^2+9)
10 T =1;//Sampling period T = 1 Second
11 z = poly(0, 'z');
12 Hz = horner(H,(1/T)*(z-(z^-1)))
```

Scilab code Exa 8.3.4 Graphical

```
1 // Graphical//
2 // Example 8.3.4
3 // Bilinear Transformation
4 // To convert analog filter into digital filter
5 clear;
6 clc;
7 close;
8 s = poly(0, 's');
9 H = (s+0.1)/((s+0.1)^2+16);
10 Omega_Analog = 4;
11 Omega_Digital = %pi/2;
12 // Finding Sampling Period
13 T = (2/Omega_Analog)*(tan(Omega_Digital/2))
14 z = poly(0, 'z');
15 Hz = horner(H,(2/T)*((z-1)/(z+1)))
```

#### Scilab code Exa 8.03.5 Graphical

```
1 // Graphical //
2 //Example 8.03.5
3 // First Order Butterworth Filter
4 //Low Pass Filter
5 clear;
6 \text{ clc};
7 close;
8 \ s = poly(0, 's');
9 Omegac = 0.2*%pi;
10 H = Omegac/(s+Omegac);
11 T =1; //Sampling period T = 1 Second
12 z = poly(0, 'z');
13 Hz = horner(H, (2/T)*((z-1)/(z+1)))
14 HW = frmag(Hz(2), Hz(3), 512);
15 W = 0:%pi/511:%pi;
16 plot(W/%pi,HW)
17 a=gca();
```

```
18 a.thickness = 3;
19 a.foreground = 1;
20 a.font_style = 9;
21 xgrid(1)
22 xtitle('Magnitude Response of Single pole LPF Filter
Cutoff frequency = 0.2*pi', 'Digital Frequency
---->', 'Magnitude');
```

#### Scilab code Exa 8.3.05 Graphical

```
1 //Graphical//
2 //Example 8.3.05
3 // First Order Butterworth Filter
4 //High Pass Filter
5 //Table 8.13: Using Digital Filter Transformation
6 clear;
7 clc:
8 close;
9 \ s = poly(0, 's');
10 Omegac = 0.2*%pi;
11 H = Omegac/(s+Omegac);
12 T =1; //Sampling period T = 1 Second
13 z = poly(0, 'z');
14 Hz_LPF = horner(H, (2/T)*((z-1)/(z+1));
15 alpha = -(cos((Omegac+Omegac)/2))/(cos((Omegac-
     Omegac)/2));
16 HZ_HPF=horner(Hz_LPF,-(z+alpha)/(1+alpha*z))
17 HW = frmag(HZ_HPF(2), HZ_HPF(3), 512);
18 W = 0:%pi/511:%pi;
19 plot(W/%pi,HW)
20 a = gca();
21 a.thickness = 3;
22 a.foreground = 1;
23 \text{ a.font_style} = 9;
24 xgrid(1)
```

```
25 xtitle('Magnitude Response of Single pole HPF Filter
Cutoff frequency = 0.2*pi', 'Digital Frequency
--->', 'Magnitude');
```

Scilab code Exa 8.3.5 Graphical

```
1 //Graphical//
2 //Example 8.3.5 Sigle pole analog filter
3 // Bilinear Transformation
4 //To convert analog filter into digital filter
5 clear;
6 \text{ clc};
7 close;
8 \ s = poly(0, 's');
9 Omegac = 0.2*%pi;
10 H = Omegac/(s+Omegac);
11 T =1; //Sampling period T = 1 Second
12 z = poly(0, 'z');
13 Hz = horner(H, (2/T)*((z-1)/(z+1)))
14 disp(Hz, 'Hz = ')
15 HW = frmag(Hz(2), Hz(3), 512);
16 W = 0:%pi/511:%pi;
17 plot(W/%pi,HW)
18 a=gca();
19 a.thickness = 3;
20 a.foreground = 1;
21 a.font_style = 9;
22 xgrid(1)
23 xtitle('Magnitude Response of Single pole LPF Filter
       Cutoff frequency = 0.2 * \text{pi}', 'Digital Frequency
     ---->', 'Magnitude');
24 //Result
25 / Hz =
26 //
27 //
         0.6283185 + 0.6283185z
```

28 // 29 // - 1.3716815 + 2.6283185z 30 // 31 //--> Hz(3) = Hz(3) / 2.628318532 / / Hz =33 // 34 // 0.6283185 + 0.6283185z35 // 36 // - 0.5218856 + z 37 // 38 //-->Hz(2)=Hz(2)/2.628318539 // Hz =40 // 41 // 0.2390572 + 0.2390572z42 // 43 //  $-\ 0.5218856\ +\ z$ 44 // which is equivalent to 45 // 46 / Hz =47 // 48 //  $0.2390572(1 + z^{-1})$ 49 //  $1 - 0.5218856 * z^{-1}$ 50 //

Scilab code Exa 08.3.6 Graphical

```
1 //Graphical//
2 //Example 08.3.6
3 // To Design an Analog Butterworth Filter
4 //For the given cutoff frequency Wc = 500 Hz
5 clear;
6 clc;
7 close;
8 omegap = 500;
9 omegas = 1000;
```

```
10 delta1_in_dB = -3;
11 delta2_in_dB = -40;
12 delta1 = 10^{(delta1_in_dB/20)}
13 delta2 = 10^{(delta2_in_dB/20)}
14 // Calculation of Filter Order
15 N = \log 10 ((1/(delta2^2)) - 1)/(2 \cdot \log 10 (omegas/omegap))
16 \text{ N} = \text{ceil}(\text{N})
17 omegac = omegap;
18 //Poles and Gain Calculation
19 [pols,gain]=zpbutt(N,omegac);
20 //Magnitude Response of Analog IIR Butterworth
       Filter
21 h=buttmag(N, omegac, 1:1000);
22 //Magnitude in dB
23 \text{ mag}=20*\log 10(h);
24 plot2d((1:1000),mag,[0,-180,1000,20]);
25 a = gca();
26 a.thickness = 3;
27 \text{ a.foreground} = 1;
28 \text{ a.font_style} = 9;
29 xgrid(5)
30 xtitle('Magnitude Response of Butterworth LPF Filter
       Cutoff frequency = 500 Hz', 'Analog frequency in
      Hz \longrightarrow ', 'Magnitude in dB \longrightarrow ');
```

#### Scilab code Exa 8.03.06 Graphical

```
1 //Graphical//
2 //Example 8.03.06
3 // To Design an Analog Butterworth Filter
4 //For the given cutoff frequency Wc = 500 Hz
5 clear;
6 clc;
7 close;
8 omegap = 500;
```

```
9 \text{ omegas} = 1000;
10 delta1_in_dB = -3;
11 delta2_in_dB = -40;
12 delta1 = 10^{(delta1_in_dB/20)}
13 delta2 = 10^{(delta2_in_dB/20)}
14 //Calculation of Filter Order
15 N = \log 10 ((1/(delta2^2)) - 1)/(2 \cdot \log 10 (omegas/omegap))
16 \text{ N} = \text{ceil}(\text{N})
17 omegac = omegap;
18 //Poles and Gain Calculation
19 [pols,gain]=zpbutt(N,omegac);
20 //Magnitude Response of Analog IIR Butterworth
       Filter
21 h=buttmag(N,omegac,1:1000);
22 //Magnitude in dB
23 \text{ mag}=20*\log 10(h);
24 plot2d((1:1000),mag,[0,-180,1000,20]);
25 \ a=gca();
26 a.thickness = 3;
27 \text{ a.foreground} = 1;
28 a.font_style = 9;
29 xgrid(5)
30 xtitle('Magnitude Response of Butterworth LPF Filter
       Cutoff frequency = 500 \text{ Hz}', 'Analog frequency in
      Hz \longrightarrow ', 'Magnitude in dB \longrightarrow');
```

#### Scilab code Exa 8.03.6 Graphical

```
1 //Graphical//
2 //Example 8.03.6
3 // To Design an Analog Low Pass IIR Butterworth
    Filter
4 //For the given cutoff frequency Wc = 500 Hz
5 clear;
6 clc;
```

```
7 close;
8 \text{ omegap} = 500;
9 \text{ omegas} = 1000;
10 delta1_in_dB = -3;
11 delta2_in_dB = -40;
12 delta1 = 10^{(delta1_in_dB/20)}
13 delta2 = 10^{(delta2_in_dB/20)}
14 //Calculation of Filter Order
15 N = \log 10 ((1/(delta2^2)) - 1)/(2 \cdot \log 10 (omegas/omegap))
16 N = ceil(N)
17 omegac = omegap;
18 //Poles and Gain Calculation
19 [pols,gain]=zpbutt(N,omegac);
20 //Magnitude Response of Analog IIR Butterworth
      Filter
21 h=buttmag(N,omegac,1:1000);
22 //Magnitude in dB
23 \text{ mag}=20*\log 10(h);
24 plot2d((1:1000),mag,[0,-180,1000,20]);
25 \ a = gca();
26 a.thickness = 3;
27 \text{ a.foreground} = 1;
28 \text{ a.font_style} = 9;
29 xgrid(5)
30 xtitle('Magnitude Response of Butterworth LPF Filter
       Cutoff frequency = 500 Hz', 'Analog frequency in
      Hz \longrightarrow ', 'Magnitude in dB \longrightarrow ');
```

#### Scilab code Exa 8.3.06 Graphical

```
1 //Graphical//
2 //Example 8.3.06
3 // To Convert LPF to Analog [1]. High Pass [2]. Band
Pass [3]. Band Stop IIR Butterworth Filter
4 //Using Analog Filter Transformations: Refer Table
```

```
:8.12
5 //For the given cutoff frequency Wc = 500 Hz
6 clear;
7 clc;
8 close;
9 \text{ omegap} = 500;
10 \text{ omegas} = 1000;
11 delta1_in_dB = -3;
12 delta2_in_dB = -40;
13 delta1 = 10^{(delta1_in_dB/20)}
14 delta2 = 10^{(delta2_in_dB/20)}
15 //Calculation of Filter Order
16 \text{ N} = \frac{\log 10}{((1/(delta2^2)) - 1)/(2 \cdot \log 10} (omegas/omegap))}
17 \text{ N} = \text{ceil}(\text{N})
18 omegac = omegap;
19 //Poles and Gain Calculation
20 [pols,gain]=zpbutt(N,omegac);
21 N =1;
22 //
23 omega_LPF = omegap; //Analog LPF Cutoff frequency
24 omega_HPF = omega_LPF; //Analog HPF Cutoff
      frequency
25 omega2 = 600; //Upper Cutoff frequency
26 omega1 = 300; //Lower Cutoff Frequency
27 omega0 = (omega2*omega1);
28 BW = omega2 - omega1; //Bandwidth
29 disp('Analog LPF Transfer function')
30 [hs,pols,zers,gain] = analpf(N, 'butt',[0,0],
      omega_LPF)
31 \text{ hs}_LPF = \text{hs};
32 \text{ hs}_{LPF}(2) = \text{hs}_{LPF}(2)/500;
33 hs_LPF(3) = hs_LPF(3)/500;
34 \text{ s} = poly(0, 's');
35 disp('Analog HPF Transfer function')
36 h_HPF = horner(hs_LPF,omega_LPF*omega_HPF/s)
37 disp('Analog BPF Transfer function')
38 \text{ num} = (s^2) + \text{omega0}
39 \text{ den} = BW * s
```

```
40 h_BPF = horner(hs_LPF,omega_LPF*(num/den))
41 disp('Analog BSF Transfer function')
42 \text{ num} = s * BW
43 \text{ den} = (s^2) + \text{omega0}
44 h_BSF = horner(hs_LPF,omega_LPF*(num/den))
45 // Plotting Low Pass Filter Frequency Response
46 figure
47 fr=0:.1:1000;
48 hf=freq(hs_LPF(2),hs_LPF(3),%i*fr);
49 hm=abs(hf);
50 plot(fr,hm)
51 a=gca();
52 a.thickness = 3;
53 a.foreground = 1;
54 \text{ a.font_style} = 9;
55 xgrid(1)
56 xtitle('Magnitude Response of LPF Filter Cutoff
      frequency = 500Hz', 'Analog Frequency---->', '
      Magnitude');
57 // Plotting High Pass Filter Frequency Response
58 figure
59 fr=0:.1:1000;
60 hf_HPF=freq(h_HPF(2),h_HPF(3),%i*fr);
61 hm_HPF=abs(hf_HPF);
62 plot(fr,hm_HPF)
63 \ a = gca();
64 a.thickness = 3;
65 a.foreground = 1;
66 a.font_style = 9;
67 xgrid(1)
68 xtitle('Magnitude Response of HPF Filter Cutoff
      frequency = 500Hz', 'Analog Frequency--->', '
      Magnitude');
69 // Plotting Band Pass Filter Frequency Response
70 figure
71 fr=0:.1:1000;
72 hf_BPF=freq(h_BPF(2),h_BPF(3),%i*fr);
73 hm_BPF=abs(hf_BPF);
```

```
74 plot(fr,hm_BPF)
75 \ a = gca();
76 a.thickness = 3;
77 a.foreground = 1;
78 a.font_style = 9;
79 xgrid(1)
80 xtitle('Magnitude Response of BPF Filter Upper
      Cutoff frequency = 600Hz & Lower Cutoff frequency
      = 300Hz', 'Analog Frequency ---->', 'Magnitude');
81 // Plotting Band Stop Filter Frequency Response
82 figure
83 fr=0:.1:1000;
84 hf_BSF=freq(h_BSF(2),h_BSF(3),%i*fr);
85 hm=abs(hf_BSF);
86 plot(fr, hf_BSF)
87 \ a = gca();
88 a.thickness = 3;
89 a.foreground = 1;
90 a.font_style = 9;
91 xgrid(1)
92 xtitle('Magnitude Response of BSF Filter Upper
      Cutoff frequency = 600Hz & Lower Cutoff frequency
      = 300Hz', 'Analog Frequency ---->', 'Magnitude');
```

#### Scilab code Exa 8.3.6 Graphical

```
1 // Graphical//
2 // Example 8.3.6
3 // To Design an Analog Butterworth Filter
4 // For the given cutoff frequency Wc = 500 Hz
5 clear;
6 clc;
7 close;
8 omegap = 2*%pi*500;
9 omegas = 2*%pi*1000;
```

```
10 delta1_in_dB = -3;
11 delta2_in_dB = -40;
12 delta1 = 10^{(delta1_in_dB/20)}
13 delta2 = 10^{(delta2_in_dB/20)}
14 //Calculation of Filter Order
15 N = log10((1/(delta2<sup>2</sup>))-1)/(2*log10(omegas/omegap))
16 \text{ N} = \text{ceil}(\text{N})
17 omegac = omegap;
18 //Poles and Gain Calculation
19 [pols,gain]=zpbutt(N,omegac);
20 disp(N, 'Filter order N = ')
21 disp(pols, 'Pole positions are pols =')
22 //Magnitude Response of Analog IIR Butterworth
      Filter
23 h=buttmag(N, omegac, 1:1000);
24 //Magnitude in dB
25 mag=20*log10(h);
26 plot2d((1:1000),mag,[0,-180,1000,20]);
27 \ a = gca();
28 a.thickness = 3;
29 a.foreground = 1;
30 a.font_style = 9;
31 xgrid(5)
32 xtitle ('Magnitude Response of Butterworth LPF Filter
       Cutoff frequency = 500 \text{ Hz}', 'Analog frequency in
      Hz \longrightarrow ', 'Magnitude in dB \longrightarrow');
33 //Result
34 //Filter order N =
                              7.
35 / s =
36 // \text{ column 1 to } 3
37 // -699.07013+3062.8264 i -1958.751+2456.196 i
      -2830.4772 + 1363.086 i
38 // column 4 to 6
39 // -3141.5927+3.847D-13i -2830.4772-1363.086 i
      -1958.751 - 2456.196 i
40 //column 7
41 //- 699.07013-3062.8264 i
```

#### Scilab code Exa 8.3.7 Graphical

```
1 //Graphical//
2 //Example 8.3.7
3 //To Design an Analog Chebyshev Filter
4 //For the given cutoff frequency = 500 \text{ Hz}
5 clear;
6 \, \operatorname{clc};
7 close;
8 omegap = 1000*%pi; //Analog Passband Edge frequency
      in radians/sec
9 omegas = 2000*%pi; //Analog Stop band edge frequency
       in radians/sec
10 delta1_in_dB = -1;
11 delta2_in_dB = -40;
12 delta1 = 10^(delta1_in_dB/20);
13 delta2 = 10^{(delta2_in_dB/20)};
14 delta = sqrt(((1/delta2)^2)-1)
15 epsilon = sqrt(((1/delta1)^2)-1)
16 //Calculation of Filter order
17 num = ((sqrt(1-delta2^2))+(sqrt(1-((delta2^2)*(1+
      epsilon^2)))))/(epsilon*delta2)
18 den = (omegas/omegap)+sqrt((omegas/omegap)^2-1)
19 N = \log 10 (\text{num}) / \log 10 (\text{den})
20 //N = (acosh (delta / epsilon))/(acosh (omegas / omegap))
21 \text{ N} = \text{floor}(\text{N})
22 // Cutoff frequency
23 omegac = omegap
24 //Calculation of poles and zeros
25 [pols,Gn] = zpch1(N,epsilon,omegap)
26 disp(N, 'Filter order N = ');
27 disp(pols, 'Poles of a type I lowpass Chebyshev
      filter are Sk = ')
```

```
28 //Analog Filter Transfer Function
```

```
29 h = poly(Gn, 's', 'coeff')/real(poly(pols, 's'))
30 //Magnitude Response of Chebyshev filter
31 [h2]=cheb1mag(N,omegac,epsilon,1:1000)
32 //Magnitude in dB
33 mag=20*log10(h2);
34 plot2d((1:1000),mag,[0,-180,1000,20]);
35 a=gca();
36 a.thickness = 3;
37 a.foreground = 1;
38 a.font_style = 9;
39 xgrid(5)
40 xtitle('Magnitude Response of Chebyshev Type 1 LPF
Filter Cutoff frequency = 500 Hz', 'Analog
frequency in Hz-->', 'Magnitude in dB -->');
```

#### Scilab code Exa 8.4.1 Graphical

```
1 // Graphical//
```

2 //Caption:Conveting single pole LPF Butterworth filter into BPF

```
3 //Exa8.4.1
```

```
4 //page698
```

- 5 clc;
- 6 Op = sym('Op'); //pass band edge frequency of low pass filter

```
7 \ s = sym('s');
```

- 8 Ol = sym('Ol'); //lower cutoff frequency of band
   pass filter
- 9 Ou = sym('Ou'); //upper cutoff frequency of band
   pass filter
- 10 s1 = Op\*(s^2+Ol\*Ou)/(s\*(Ou-Ol)); //Analog transformation for LPF to BPF
- 11 H\_Lpf = Op/(s+Op); //single pole analog LPF Butterworth filter
- 12 H\_Bpf = limit(H\_Lpf,s,s1); //analog BPF Butterworth

```
filter
13 disp(H_Lpf, 'H_Lpf = ')
14 disp(H_Bpf, 'H_Bpf = ')
15 //Result
16 //H_Lpf = Op/(s+Op)
17 //H_Bpf = (Ou-Ol)*s/(s^2+(Ou-Ol)*s+Ol*Ou)
```

#### Scilab code Exa 8.4.02 Graphical

```
1 //Graphical//
2 //Example 8.4.02
3 //To Design an Digital IIR Butterworth Filter from
      Analog IIR Butterworth Filter
4 //and to plot its magnitude response
5 //TRANSFORMATION OF LPF TO BSF USING DIGITAL
     TRANSFORMATION
6 clear:
7 \, \text{clc};
8 close;
9 omegaP = 0.2*%pi;
10 omegaL = (2/5)*%pi;
11 omegaU = (3/5)*%pi;
12 \ z = poly(0, 'z');
13 H_LPF = (0.245)*(1+(z^{-1}))/(1-0.509*(z^{-1}))
14 alpha = (cos((omegaU+omegaL)/2)/cos((omegaU-omegaL)
      /2));
15 k = tan((omegaU - omegaL)/2) * tan(omegaP/2);
16 NUM = ((z^2) - ((2*alpha/(1+k))*z) + ((1-k)/(1+k)));
17 DEN = (1-((2*alpha/(1+k))*z)+((((1-k)/(1+k))*(z^2)));
18 HZ_BPF=horner(H_LPF,NUM/DEN)
19 HW = frmag(HZ_BPF(2), HZ_BPF(3), 512);
20 W = 0:%pi/511:%pi;
21 plot(W/%pi,HW)
22 a=gca();
23 a.thickness = 3;
```

```
24 a.foreground = 1;
25 a.font_style = 9;
26 xgrid(1)
27 xtitle('Magnitude Response of BSF Filter', 'Digital
Frequency--->', 'Magnitude');
```

Scilab code Exa 8.4.2 Graphical

```
1 // Graphical//
2 //Example 8.4.2
3 //To Design an Digital IIR Butterworth Filter from
      Analog IIR Butterworth Filter
4 //and to plot its magnitude response
5 //TRANSFORMATION OF LPF TO BPF USING DIGITAL
     TRANSFORMATION
6 clear;
7 clc;
8 close;
9 omegaP = 0.2*%pi;
10 omegaL = (2/5)*%pi;
11 omegaU = (3/5)*%pi;
12 z=poly(0, 'z');
13 H_LPF = (0.245)*(1+(z^{-1}))/(1-0.509*(z^{-1}))
14 alpha = (cos((omegaU+omegaL)/2)/cos((omegaU-omegaL)
      /2));
15 k = (\cos((\text{omegaU} - \text{omegaL})/2)/\sin((\text{omegaU} - \text{omegaL}))
     /2))*tan(omegaP/2);
16 NUM =-((z^2)-((2*alpha*k/(k+1))*z)+((k-1)/(k+1)));
17 DEN = (1-((2*alpha*k/(k+1))*z)+(((k-1)/(k+1))*(z^2)))
      );
18 HZ_BPF=horner(H_LPF,NUM/DEN)
19 disp(HZ_BPF, 'Digital BPF IIR Filter H(Z) = ')
20 HW = frmag(HZ_BPF(2), HZ_BPF(3), 512);
21 W = 0:%pi/511:%pi;
22 plot(W/%pi,HW)
```

```
23 a=gca();
24 a.thickness = 3;
25 a.foreground = 1;
26 a.font_style = 9;
27 xgrid(1)
28 xtitle('Magnitude Response of BPF Filter', 'Digital
      Frequency ---->', 'Magnitude');
29 //Result
30 // Digital BPF IIR Filter H(Z) =
                                        \mathbf{2}
                                                       3
31 //
                   4
         0.245 - 1.577D - 17z - 0.245z + 1.577D - 17z +
32 //
      1.360D - 17z
33 //
                                      \mathbf{2}
                                                     3
34 //
                   4
        -0.509 + 1.299D - 16z - z + 6.438D - 17z + 5.551D
35
   -17z
36 //
37 // which is equivalent to
38 // H(z) =
39 //
                               \mathbf{2}
40 //
          0.245 - 0 - 0.245z + 0 + 0
41 //
42 //
                           2
43 //
          - 0.509 + 0 - z + 0 + 0
44 //
45 //
46 //H(z) =
47 //
48 //
                         2
          0.245 - 0.245 z
49 //
50 //
                     \mathbf{2}
51 //
52 //
          - 0.509 - z
53 //
```

```
69
```

#### Scilab code Exa 8.5 Graphical

```
1 // Graphical //
2 //Figure 8.5
3 //Program to generate different window functions
4 clear;
5 close;
6 clc
7 M = 61;
8 \text{ for } n = 1:M
     h_Rect(n) = 1;
9
     h_{hann}(n) = 0.5-0.5*\cos(2*\%pi*(n-1)/(M-1));
10
     h_{hamm}(n) = 0.54-0.46*\cos(2*\%pi*(n-1)/(M-1));
11
     h_balckmann(n) = 0.42-0.5*cos(2*%pi*n/(M-1))+0.08*
12
        cos(4*%pi*n/(M-1));
13 \text{ end}
14 plot2d(1:M,[h_Rect,h_hann,h_hamm,h_balckmann
      ],[2,5,7,9]);
  legend(['Rectangular Window'; 'Hanning'; 'Hamming'; '
15
      Balckmann ']);
16 title('Window Functions for Length M = 61')
```

Scilab code Exa 8.6 Graphical

```
1 //Graphical//
2 //Figure 8.6 and Figure 8.7
3 //Program to frequency response of
4 //(1) Hanning window (2) Hamming window for M = 31
      and M = 61
5 clear;
6 close;
7 clc
8 M1 = 31;
9 M2 = 61;
10 \text{ for } n = 1:M1
     h_{n_1}(n) = 0.5 - 0.5 \cdot \cos(2 \cdot \sqrt{pi} \cdot (n-1)/(M1-1));
11
12
     h_hamm_31(n) = 0.54-0.46*\cos(2*\%pi*(n-1)/(M1-1));
13 end
14 \text{ for } n = 1:M2
15
     h_{hann_{61}(n)} = 0.5-0.5*\cos(2*\%pi*(n-1)/(M2-1));
     h_ham_{61}(n) = 0.54 - 0.46 \cdot \cos(2 \cdot \sqrt{pi} \cdot (n-1) / (M2-1));
16
17 end
18 subplot(2,1,1)
19 [h_hann_31_M,fr]=frmag(h_hann_31,512);
20 [h_hann_61_M,fr]=frmag(h_hann_61,512);
21 h_hann_31_M = 20*log10(h_hann_31_M./max(h_hann_31_M)
      );
22 \text{ h}_{\text{hann}_{61}} = 20 \times \log 10 (\text{h}_{\text{hann}_{61}} \text{M}./\text{max})
      h_hann_61_M));
23 plot2d(fr,h_hann_31_M,2);
24 plot2d(fr,h_hann_61_M,5);
25 legend(['Length M = 31'; 'Length M = 61']);
26 title('Frequency Response Of Hanning window')
27 subplot(2,1,2)
28 [h_hamm_31_M,fr]=frmag(h_hamm_31,512);
29 [h_hamm_61_M,fr]=frmag(h_hamm_61,512);
30 h_hamm_31_M = 20*log10(h_hamm_31_M./max(h_hamm_31_M)
      );
31 h_hamm_61_M = = 20*log10(h_hamm_61_M./max(
      h_hamm_61_M));
32 plot2d(fr,h_hamm_31_M,2);
33 plot2d(fr,h_hamm_61_M,5);
```
- 34 legend(['Length M = 31'; 'Length M = 61']);
- 35 title('Frequency Response of Hamming window')

Scilab code Exa 1.08 Graphical

```
1 //Graphical//
2 //PROGRAM TO DESIGN AND OBTAIN THE FREQUENCY
      RESPONSE OF FIR FILTER
3 //Band Stop FILTER (or)Band Reject Filter
4 clear;
5 \, \text{clc};
6 close;
7 M = 11
                         //Filter length = 11
8 Wc = [%pi/4,3*%pi/4]; // Digital Cutoff
      frequency
9 \text{ Wc2} = \text{Wc}(2)
10 \text{ Wc1} = \text{Wc(1)}
11 Tuo = (M-1)/2
                        //Center Value
12 hd = zeros(1,M);
13 W = zeros(1,M);
14 \text{ for } n = 1:11
15
   if (n == Tuo+1)
    hd(n) = 1 - ((Wc2 - Wc1) / \%pi);
16
             hd(n) = (sin(\%pi*((n-1)-Tuo))-sin(Wc2*((n-1)-Tuo)))
17
    else
       Tuo))+sin(Wc1*((n-1)-Tuo)))/((((n-1)-Tuo)*%pi);
18
     end
     if (abs(hd(n)) <(0.00001))
19
20
       hd(n)=0;
21
     end
22 end
23 hd
24 //Rectangular Window
25 \text{ for } n = 1:M
26
     W(n) = 1;
27 end
```

```
28 //Windowing Fitler Coefficients
29 h = hd.*W;
30 disp('Filter Coefficients are')
31 h;
32 [hzm,fr]=frmag(h,256);
33 \text{ hzm}_dB = 20 * \log 10 (\text{hzm}) . / \max(\text{hzm});
34 subplot(2,1,1)
35 plot(2*fr,hzm)
36 xlabel('Normalized Digital Frequency W');
37 ylabel('Magnitude');
38 title('Frequency Response Of FIR BPF using
      Rectangular window M=11')
39 subplot(2,1,2)
40 plot(2*fr,hzm_dB)
41 xlabel('Normalized Digital Frequency W');
42 ylabel('Magnitude in dB');
43 title('Frequency Response Of FIR BPF using
      Rectangular window M=11')
```

#### Scilab code Exa 1.8 Graphical

```
1 //Graphical//
2 //PROGRAM TO DESIGN AND OBTAIN THE FREQUENCY
     RESPONSE OF FIR FILTER
3 //Band PASS FILTER
4 clear;
5 \, \text{clc};
6 close;
                       //Filter length = 11
7 M = 11
8 Wc = [%pi/4,3*%pi/4]; // Digital Cutoff
      frequency
9 Wc2 = Wc(2)
10 \text{ Wc1} = \text{Wc(1)}
11 Tuo = (M-1)/2
                  //Center Value
12 hd = zeros(1,M);
```

```
13 W = zeros(1,M);
14 \text{ for } n = 1:11
     if (n == Tuo+1)
15
16
         hd(n) = (Wc2-Wc1)/\%pi;
17
     else
18
            n
         hd(n) = (sin(Wc2*((n-1)-Tuo)) - sin(Wc1*((n-1)-Tuo)))
19
            Tuo)))/(((n-1)-Tuo)*%pi);
20
     end
21
     if(abs(hd(n))<(0.00001))</pre>
22
        hd(n)=0;
23
     end
24 \text{ end}
25 hd:
26 //Rectangular Window
27 \text{ for } n = 1:M
     W(n) = 1;
28
29 end
30 //Windowing Fitler Coefficients
31 h = hd.*W;
32 disp('Filter Coefficients are')
33 h;
34 [hzm,fr]=frmag(h,256);
35 \text{ hzm}_{dB} = 20 * \log 10 (\text{hzm}) . / \max(\text{hzm});
36 subplot(2,1,1)
37 plot(2*fr,hzm)
38 xlabel('Normalized Digital Frequency W');
39 ylabel('Magnitude');
40 title('Frequency Response Of FIR BPF using
      Rectangular window M=11')
41 subplot(2,1,2)
42 plot (2*fr,hzm_dB)
43 xlabel('Normalized Digital Frequency W');
44 ylabel('Magnitude in dB');
45 title('Frequency Response Of FIR BPF using
      Rectangular window M=11')
```

Scilab code Exa 2.8 Graphical

```
1 //Graphical//
2 //PROGRAM TO DESIGN AND OBTAIN THE FREQUENCY
      RESPONSE OF FIR FILTER
3 //HIGH PASS FILTER
4 clear;
5 \, \text{clc};
6 close;
7 M = 61
                         //Filter length = 61
                         //Digital Cutoff frequency
8 Wc = %pi/5;
9 \text{ Tuo} = (M-1)/2
                        //Center Value
10 \text{ for } n = 1:M
       if (n == Tuo+1)
11
12
          hd(n) = 1 - Wc / \% pi;
13
       else
          hd(n) = (sin(%pi*((n-1)-Tuo)) - sin(Wc*((n-1)-Tuo)))
14
             Tuo)))/(((n-1)-Tuo)*%pi);
15
     end
16 \text{ end}
17 //Rectangular Window
18 \text{ for } n = 1:M
19
     W(n) = 1;
20 end
21 //Windowing Fitler Coefficients
22 h = hd. *W;
23 disp('Filter Coefficients are')
24 h;
25 [hzm,fr]=frmag(h,256);
26 \text{ hzm}_dB = 20 * \log 10 (\text{hzm}) . / \max(\text{hzm});
27 subplot(2,1,1)
28 plot(2*fr,hzm)
29 xlabel('Normalized Digital Frequency W');
30 ylabel('Magnitude');
```

#### Scilab code Exa 8.10 Graphical

```
1 // Graphical //
2 //Figure 8.9 and 8.10
3 //PROGRAM TO DESIGN AND OBTAIN THE FREQUENCY
      RESPONSE OF FIR FILTER
4 //LOW PASS FILTER
5 clear;
6 \, \text{clc};
7 close;
8 M = 61
                       //Filter length = 61
                       //Digital Cutoff frequency
9 Wc = %pi/5;
                       //Center Value
10 \text{ Tuo} = (M-1)/2
11 for n = 1:M
12
       if (n == Tuo+1)
13
         hd(n) = Wc/%pi;
14
       else
         hd(n) = sin(Wc*((n-1)-Tuo))/((((n-1)-Tuo)*%pi))
15
             ;
16
     end
17 end
18 //Rectangular Window
19 for n = 1:M
20
     W(n) = 1;
21 \text{ end}
22 //Windowing Fitler Coefficients
```

```
23 h = hd.*W;
24 disp('Filter Coefficients are')
25 h;
26 [hzm,fr]=frmag(h,256);
27 \text{ hzm}_{dB} = 20 * \log 10 (\text{hzm}) . / \max(\text{hzm});
28 subplot(2,1,1)
29 plot(fr,hzm)
30 xlabel('Normalized Digital Frequency W');
31 ylabel('Magnitude');
32 title('Frequency Response Of FIR LPF using
      Rectangular window M=61')
33 subplot(2,1,2)
34 plot(fr,hzm_dB)
35 xlabel('Normalized Digital Frequency W');
36 ylabel('Magnitude in dB');
37 title('Frequency Response Of FIR LPF using
      Rectangular window M=61')
```

## Chapter 10

# Multirate Digital Signal Processing

Scilab code Exa 10.5.1 Frequency Response of DECIMATOR

1 // Graphical // 2 //Example 10.5.1 3 //Decimation by 2, Filter Length = 304 //Cutoff Frequency Wc = % pi/25 //Pass band Edge frequency fp = 0.25 and a Stop band edge frequency fs = 0.316 // Choose the number of cosine functions and create a dense grid 7 // in [0, 0.25] and [0.31, 0.5]8 //magnitude for pass band = 1 & stop band = 0 (i.e)  $\begin{bmatrix} 1 & 0 \end{bmatrix}$ 9 //Weighting function = $\begin{bmatrix} 2 & 1 \end{bmatrix}$ 10 clear; 11 clc; 12 close; 13 M = 30; //Filter Length 14 D = 2; // Decimation Factor = 2 15 Wc = %pi/2; //Cutoff Frequency 16 Wp = Wc/(2\*%pi); //Passband Edge Frequency

```
17 Ws = 0.31; //Stopband Edge Frequency
18 hn=eqfir(M,[0 Wp;Ws .5],[1 0],[2 1]);
19 [hm,fr]=frmag(hn,256);
20 disp('The LPF Filter Coefficients are:')
21 hn
22 //Obtaining Polyphase Filter Coefficients from hn
23 p = zeros(D, M/D);
24 \text{ for } k = 1:D
     for n = 1: (length(hn)/D)
25
       p(k,n) = hn(D*(n-1)+k);
26
27
     end
28 end
29 disp('The Polyphase Decimator for D = 2 are:')
30 p
31 figure
32 plot(fr,hm)
33 xlabel('Normalized Digital Frequency fr');
34 ylabel('Magnitude');
35 title('Frequency Response of FIR LPF using REMEZ
      algorithm M=61')
36 figure
37 plot(.5*(0:255)/256,20*log10(frmag(hn,256)));
38 xlabel('Normalized Digital Frequency fr');
39 ylabel('Magnitude in dB');
40 title('Frequency Response of DECIMATOR (D=2) using
     REMEZ algorithm M=30')
```

#### Scilab code Exa 10.5.2 Frequency Response of INTERPOLATOR

```
1 //Graphical//
2 //Example 10.5.2
3 //Interpolation by 5, Filter Length = 30
4 //Cutoff Frequency Wc = %pi/5
5 //Pass band Edge frequency fp = 0.1 and a Stop band
```

```
edge frequency fs = 0.16
```

```
6 // Choose the number of cosine functions and create
      a dense grid
7 // in [0, 0.1) and [0.16, 0.5)
8 //magnitude for pass band = 1 & stop band = 0 (i.e)
      \begin{bmatrix} 1 & 0 \end{bmatrix}
9 //Weighting function = \begin{bmatrix} 3 & 1 \end{bmatrix}
10 clear;
11 clc;
12 close;
13 M = 30;
            //Filter Length
14 I = 5; //Interpolation Factor = 5
15 Wc = %pi/5; //Cutoff Frequency
16 Wp = Wc/(2*%pi); //Passband Edge Frequency
17 Ws = 0.16; //Stopband Edge Frequency
18 hn=eqfir(M,[0 Wp;Ws .5],[1 0],[3 1]);
19 [hm,fr]=frmag(hn,256);
20 disp('The LPF Filter Coefficients are:')
21 hn
22 //Obtaining Polyphase Filter Coefficients from hn
23 p = zeros(I,M/I);
24 \text{ for } k = 1:I
25
     for n = 1:(length(hn)/I)
       p(k,n) = hn(I*(n-1)+k);
26
27
     end
28 \text{ end}
29 disp('The Polyphase Interpolator for I = 5 are:')
30 p
31 figure
32 plot(fr,hm)
33 xlabel('Normalized Digital Frequency fr');
34 ylabel('Magnitude');
35 title('Frequency Response of FIR LPF using REMEZ
      algorithm M=61')
36 figure
37 plot(.5*(0:255)/256,20*log10(frmag(hn,256)));
38 xlabel('Normalized Digital Frequency fr');
39 ylabel('Magnitude in dB');
40 title('Frequency Response of INTERPOLATOR(I=5) using
```

Scilab code Exa 10.6.1 Multistage Implementation of Sampling Rate Conversion

```
1 // Graphical //
2 //Example 10.6.1
3 // Multistage Implementation of Sampling Rate
     Conversion
4 //Decimation factor D = 50
5 //D = D1xD2, D1 = 25, D2 = 2
6 clear;
7 clc;
8 close;
9 Fs = 8000; //Sampling Frequency = 8000Hz
10 Fpc = 75; //Passband Frequency
11 Fsc = 80; //Stopband Frequency
12 Delta_F = (Fsc-Fpc)/Fs; //Transition Band
13 Pass_Band = [0,Fpc];
14 Transition_Band = [Fpc,Fsc];
15 Delta1 = (10^{-2}); //Passband Ripple
16 Delta2 = (10^{-4}); //Stopband Ripple
                     //Decimation Factor
17 D = Fs/(2*Fsc);
18 //Decimator Implemented in Two Stages
19 D1 = D/2; //Decimator 1
20 D2 = 2; //\text{Decimator } 2
21 //Decimator Single Stage Implementation
22 M = ((-10*log10(Delta1*Delta2)-13)/(14.6*Delta_F))
     +1:
23 M = ceil(M)
24 //Decimator Multistage Implementation
25 //First Stage Implementation
26 F1 = Fs/D1; //New passband for stage1
27 Fsc1 = F1-Fsc; //New Stopband for stage1
28 Delta_F1 = (Fsc1-Fpc)/Fs //New Transition for
     stage1
```

```
29 Delta11 = Delta1/2; //New Passband Ripple
30 Delta21 = Delta2; //Stopband Ripple same
31 M1 = ((-10*log10(Delta11*Delta21)-13)/(14.6*Delta_F1
     ))+1
32 \text{ M1} = \text{floor}(\text{M1})
33 //Second Stage Implementation
34 F2 = F1/D2; //New passband for stage2
35 Fsc2 = F2-Fsc; //New Stopband for stage2
36 Delta_F2 = (Fsc2-Fpc)/F1 //New Transition for
      stage2
37 Delta12 = Delta1/2; //New Passband Ripple
38 Delta22 = Delta2; //Stopband Ripple same
39 M2 = ((-10*log10(Delta12*Delta22)-13)/(14.6*Delta_F2
     ))+1
40 \text{ M2} = \text{floor}(M2)
41 disp('The Filter length Required in Single stage
      Implementation of Decimator is: ')
42 M
43 disp('The Filter length Required in Multistage
      Implementation of Decimator is: ')
44 M1+M2
45 //Calculation of Reduction Factor
46 R = M/(M1+M2);
47 disp('The Reduction in Filter Length is:')
48 R.
```

#### Scilab code Exa 10.8.1 Signal to Distortion Ratio

```
1 // Graphical//
2 // Example 10.8.1
3 // Signal to Distortion Ratio
4 // Calculation of no. of subfilters
5 clear;
6 clc;
7 close;
```

```
8 SDR_dB = 50; //Signal to distortion ratio = 50 dB
9 Wx = 0.8*%pi; //Digital maximum frequency of input
data
10 SDR = 10^(SDR_dB/10)
11 disp('The Number of subfilters required')
12 I = Wx*sqrt(SDR/12);
13 I = ceil(I)
```

Scilab code Exa 10.8.2 Signal to Distortion Ratio using Linear Interpolation

```
1 // Graphical//
2 // Example 10.8.2
3 // Signal to Distortion Ratio using Linear
Interpolation
4 // Calculation of no. of subfilters
5 clear;
6 clc;
7 close;
8 SDR_dB = 50; // Signal to distortion ratio = 50 dB
9 Wx = 0.8*%pi; // Digital maximum frequency of input
data
10 SDR = 10^(SDR_dB/10)
11 disp('The Number of subfilters required')
12 I = Wx*((SDR/80)^(1/4));
13 I = ceil(I)
```

Scilab code Exa 10.9.1 Multistage Implementation of Sampling Rate Conversion

4 //Decimation factor D = 100

```
5 / D = D1xD2, D1 = 50, D2 = 2
6 //Interpolation factor I = 100
7 / I = I1 \times I2, I1 = 2, I2 = 50
8 clear;
9 clc;
10 close;
11 Fs = 8000; //Sampling Frequency = 8000Hz
12 Fpc = 75; //Passband Frequency
13 Fsc = 80; //Stopband Frequency
14 Delta_F = (Fsc-Fpc)/Fs; //Transition Band
15 Pass_Band = [0, Fpc];
16 Transition_Band = [Fpc,Fsc];
17 Delta1 = (10^{-2}); //Passband Ripple
18 Delta2 = (10^-4); //Stopband Ripple
19 D = Fs/(2*Fsc); //Decimation Factor
20 //Decimator Implemented in Two Stages
21 D1 = D/2; //\text{Decimator 1}
22 D2 = 2; //Decimator 2
23 //Decimator Single Stage Implementation
24 M = ((-10*\log 10(\text{Delta}1*\text{Delta}2/2)-13)/(14.6*\text{Delta}F))
      +1;
25 \text{ M} = \text{ceil}(\text{M})
26 //Decimator Multistage Implementation
27 // First Stage Implementation
28 Delta_F1 = 0.020625 / Obtained from Example 10.6.1
29 M1 = ((-10*log10(Delta1*Delta2/4)-13)/(14.6*Delta_F1
      ))+1
30 \text{ M1} = \text{floor}(\text{M1})
31 //Second Stage Implementation
32 Delta_F2 = 0.015625 //Obtained from Example 10.6.1
33 M2 = ((-10*\log 10(Delta1*Delta2/4)-13)/(14.6*Delta_F2)
      ))+1
34 \text{ M2} = \text{floor}(M2)
35 disp('The Filter length Required in Single stage
      Implementation of Decimator is: ')
36 M
37 disp('The Filter length Required in Multistage
      Implementation of Decimator is: ')
```

```
38 M1+M2
39 //Calculation of Reduction Factor
40 R = M/(M1+M2);
41 disp('The Reduction in Filter Length is:')
42 R
```

## Chapter 11

# Linear Predictions and Optimum Linear Filter

Scilab code Exa 11.6.1 Design of wiener filter

```
1 // Graphical //
2 //Example 11.6.1
3 //Design of wiener filter of Length M = 2
4 clear;
5 close;
6 \, \text{clc};
7 M =2; //Wiener Filter Length
8 Rdx = [0.6 2 0.6] //Cross correlation matrix between
       the desired input sequence and actual input
     sequence
9 C = Rdx(M:\$) //Right sided sequence
10 To_M = toeplitz(C)
11 Rxx = [0.6 \ 1 \ 0.6] / Auto correlation matrix
12 Rss = Rxx(M:\$)
13 // Filter coefficients
14 h = [0.451 0.165]
15 // Calculation of Minimum Mean Square Error
16 sigma_d = 1; //Average power of desired sequence
17 MSE = sigma_d - h*Rss'
```

### Chapter 12

### **Power Spectrum Estimation**

Scilab code Exa 12.1.1 Determination of spectrum of a signal

```
1 //Graphical//
   2 //Example 12.1.1
   3 // Determination of spectrum of a signal
   4 //With maximum normalized frequency f = 0.1
   5 //using Rectangular window and Blackmann window
   6 clear;
   7 close;
   8 clc;
   9 N = 61;
10 \text{ cfreq} = [0.1 \ 0];
11 [wft,wfm,fr]=wfir('lp',N,cfreq,'re',0);
                                                                                                                              // Time domain filter
12 wft;
                               coefficients
                                                                                                                              // Frequency domain filter
13 wfm;
                               values
14 fr;
                                                                                                                              // Frequency sample points
15 WFM_dB = 20*log10(wfm); //Frequency response in dB
16 \text{ for } n = 1:N
                     h_balckmann(n) = 0.42 - 0.5 * \cos(2*\% pi * n/(N-1)) + 0.08 * \cos(2*\% pi * n/
17
                                    (4*%pi*n/(N-1));
18 end
```

```
19 wft_blmn = wft'.*h_balckmann;
20 wfm_blmn = frmag(wft_blmn,length(fr));
21 WFM_blmn_dB =20*log10(wfm_blmn);
22 subplot(2,1,1)
23 plot2d(fr,WFM_dB)
24 xtitle('Frequency Response of Rectangular window
Filtered output M = 61', 'Frequency in cycles per
samples f', 'Energy density in dB')
25 subplot(2,1,2)
26 plot2d(fr,WFM_blmn_dB)
27 xtitle('Frequency Response of Blackmann window
Filtered output M = 61', 'Frequency in cycles per
samples f', 'Energy density in dB')
```

Scilab code Exa 12.1.2 Evaluating power spectrum of a discrete sequence

```
1 // Graphical //
2 //Example 12.1.2
3 //Evaluating power spectrum of a discrete sequence
4 //Using N-point DFT
5 clear;
6 \, \operatorname{clc};
7 close;
8 N = 16;
           //Number of samples in given sequence
9 n = 0: N - 1;
10 delta_f = [0.06,0.01]; // frequency separation
11 x1 = sin(2*%pi*0.315*n)+cos(2*%pi*(0.315+delta_f(1))
      *n):
12 x2 = sin(2*%pi*0.315*n)+cos(2*%pi*(0.315+delta_f(2))
      *n);
13 L = [8, 16, 32, 128];
14 \text{ k1} = 0:L(1)-1;
15 \text{ k2} = 0:L(2)-1;
16 \ k3 = 0:L(3)-1;
17 k4 = 0:L(4)-1;
```

```
18 fk1 = k1./L(1);
19 fk2 = k2./L(2);
20 \text{ fk3} = \text{k3./L(3)};
21 \text{ fk4} = \text{k4./L(4)};
22 for i =1:length(fk1)
     Pxx1_fk1(i) = 0;
23
24
     Pxx2_fk1(i) = 0;
25
     for m = 1:N
       Pxx1_fk1(i)=Pxx1_fk1(i)+x1(m)*exp(-sqrt(-1)*2*
26
          %pi*(m-1)*fk1(i));
       Pxx2_fk1(i) = Pxx1_fk1(i) + x1(m) * exp(-sqrt(-1) * 2*
27
          %pi*(m-1)*fk1(i));
28
     end
     Pxx1_fk1(i) = (Pxx1_fk1(i)^2)/N;
29
     Pxx2_fk1(i) = (Pxx2_fk1(i)^2)/N;
30
31 end
32 for i =1:length(fk2)
     Pxx1_fk2(i) = 0;
33
     Pxx2_fk2(i) = 0;
34
35
     for m = 1:N
       Pxx1_fk2(i)=Pxx1_fk2(i)+x1(m)*exp(-sqrt(-1)*2*
36
          %pi*(m-1)*fk2(i));
       Pxx2_fk2(i) = Pxx1_fk2(i) + x1(m) * exp(-sqrt(-1) * 2*
37
          %pi*(m-1)*fk2(i));
38
     end
39
     Pxx1_fk2(i) = (Pxx1_fk2(i)^2)/N;
     Pxx2_fk2(i) = (Pxx1_fk2(i)^2)/N;
40
41 end
42 for i =1:length(fk3)
     Pxx1_fk3(i) = 0;
43
     Pxx2_fk3(i) = 0;
44
45
     for m = 1:N
46
       Pxx1_fk3(i) =Pxx1_fk3(i)+x1(m)*exp(-sqrt(-1)*2*
          %pi*(m-1)*fk3(i));
       Pxx2_fk3(i) =Pxx1_fk3(i)+x1(m)*exp(-sqrt(-1)*2*
47
          %pi*(m-1)*fk3(i));
48
     end
     Pxx1_fk3(i) = (Pxx1_fk3(i)^2)/N;
49
```

```
50
     Pxx2_fk3(i) = (Pxx1_fk3(i)^2)/N;
51 \text{ end}
52 for i =1:length(fk4)
53
     Pxx1_fk4(i) = 0;
54
     Pxx2_fk4(i) = 0;
55
     for m = 1:N
       Pxx1_fk4(i) =Pxx1_fk4(i)+x1(m)*exp(-sqrt(-1)*2*
56
          %pi*(m-1)*fk4(i));
       Pxx2_fk4(i) =Pxx1_fk4(i)+x1(m)*exp(-sqrt(-1)*2*
57
          %pi*(m-1)*fk4(i));
58
     end
59
     Pxx1_fk4(i) = (Pxx1_fk4(i)^2)/N;
60
     Pxx2_fk4(i) = (Pxx1_fk4(i)^2)/N;
61 end
62 figure
63 title('for frequency separation = 0.06')
64 subplot (2,2,1)
65 plot2d3('gnn',k1,abs(Pxx1_fk1))
66 subplot(2,2,2)
67 plot2d3('gnn',k2,abs(Pxx1_fk2))
68 subplot(2,2,3)
69 plot2d3('gnn',k3,abs(Pxx1_fk3))
70 subplot(2,2,4)
71 plot2d3('gnn',k4,abs(Pxx1_fk4))
72 figure
73 title('for frequency separation = 0.01')
74 subplot(2,2,1)
75 plot2d3('gnn',k1,abs(Pxx2_fk1))
76 subplot(2,2,2)
77 plot2d3('gnn',k2,abs(Pxx2_fk2))
78 subplot(2,2,3)
79 plot2d3('gnn',k3,abs(Pxx2_fk3))
80 subplot(2,2,4)
81 plot2d3('gnn',k4,abs(Pxx2_fk4))
```

Scilab code Exa 12.5.1 Determination of power, frequency and varaince of Additive

```
1 //Graphical//
2 //Example 12.5.1
3 //Determination of power, frequency and varaince of
4 //Additive noise
5 clear;
6 \quad clc;
7 close;
8 ryy = [0,1,3,1,0]; // Autocorrelation of signal
9 cen_ter_value = ceil(length(ryy)/2);//center value
      of autocorrelation
10 //Method1
11 //TO find out the variance of the additive Noise
12 C = ryy(ceil(length(ryy)/2):$);
13 corr_matrix = toeplitz(C); // correlation matrix
14 evals = spec(corr_matrix); // Eigen Values computation
15 sigma_w = min(evals); //Minimum of eigen value =
      varinace of noise
16 //Method2
17 //TO find out the variance of the additive Noise
18 P = [1,-sqrt(2),1]; // Ploynomial in decreasing order
19 Z = roots(P);//roots of the polynomial
20 P1 = ryy(cen_ter_value+1)/real(Z(1));//power of the
     sinusoid
21 A = sqrt(2*P1);//amplitude of the sinusoid
22 sigma_w1 = ryy(cen_ter_value)-P1;//variance of noise
      method2
23 disp(P1, 'Power of the additive noise')
24 f1 = acos(real(Z(1)))/(2*%pi)
25 disp(f1, 'frequency of the additive noise')
26 disp(sigma_w1, 'Variance of the additive noise')
```

## Appendix

Scilab code AP 1 data