Scilab Textbook Companion for Solid State Electronic Devices by B. G. Streetman And S. K. Banerjee¹

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Book Description

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Scilab numbering policy used in this document and the relation to the above book.

Exa Example (Solved example)

Eqn Equation (Particular equation of the above book)

AP Appendix to Example(Scilab Code that is an Appednix to a particular Example of the above book)

For example, Exa 3.51 means solved example 3.51 of this book. Sec 2.3 means a scilab code whose theory is explained in Section 2.3 of the book.

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Crystal Properties and Growth of Semiconductors

Scilab code Exa 1.1 Maximum packing fraction

```
1 a = 5; // lattice constant
2 b = 0.5*sqrt(a^2 + a^2 + a^2); //separation between
nearest atoms
3 r = 0.5*b; //radius of each atom
4 V = 4/3*%pi*r*r*r; //Volume of each atom
5 n = 1+8*0.125; //number of atoms per cube
6 pf = V*n/(a*a*a); //packing fraction
7 disp("1)")
8 disp(a,"lattice constant (in armstrong)=")
9 disp(r,"radius of atoms (in armstrong) =")
10 disp(pf,"maximum packing fraction =")
```

Scilab code Exa 1.2 planes and directions

1 disp("The plane illustrated in Fig. 1-5 has intercepts at 2a, 4b and 1c along the three

```
crystal axes. Taking the reciprocals of these
     intercepts, we get 1/4, 1/2, and 1. These three
     fractions have the same relationship to each
     other as the integers 2,1, and 4 (obtained by
     multiplying each fraction by 4). Thus the plane
     can be referred to as a (214) plane. The only
     exception is if the intercept is a fraction of
     the lattice constant a. In that case, we do not
     reduce it to the lowest set of integers.")
2 x = 0:0.05:2;
3 y = 0:0.1:4;
4 a=2;
5 b=4;
6 c=1;
7 deff('[z]=fs(x,y)', 'z = (1-(0.5*x)-(0.25*y))');
8 //z = (1 - (0.5 * x) - (0.25 * y));
9 fplot3d(x,y,fs);
```

Scilab code Exa 1.3 Volume density of Silicon in lattice

```
1 a = 5.43*10^-8; // lattice constant
2 d = (1+4*0.25)/(a*a); //areal density on (100) plane
3 n = 2*(6*0.5+8*0.125); //number of atoms per cube
4 V = n/(a*a*a); //volume density
5 disp("3)")
6 disp(a,"lattice constant (in cm)=")
7 disp(d,"areal density on (100) plane (in per cm
square) =")
8 disp(V,"volume density (in per cm cube) =")
```

Scilab code Exa 1.4 Czochralski method for Silicon crystal growth

1 n = 10¹⁶; // desired density of P atoms

```
2 k = 0.35;
3 1 = 5000; //initial load of Si in grams
4 w =31; // atomic weight of P
5 d = 2.33; //density of Si
6 i = n/k; //initial concentration of P in melt,
     assuming C(S) = kC(L)
7 V = 1/d; //volume of Si
8 N = i * V; //number of P atoms
9 W = N*w/(6.02*10^{23})
10 disp("4.a)")
11 disp(n," desired density of P atoms (per cubic
     centimeter = ")
12 disp(i,"initial concentration of P in melt (in per
     cubic cm )=")
13 disp("4.b)")
14 disp(V, "Volume of Si (in cubic cm) =")
15 disp(N,"number of P atoms =")
16 disp(W," weight of phosphorus to be added (in grams) =
     ")
```

Atoms and Electrons

Scilab code Exa 2.1 expectation of momentum

```
1 //j=complex(0,1);
2 //psi = A*exp(j*k*x);
3 disp("px = h_cross*k(x)");
4 disp("If we try to evaluate these integrals directly
, we run into the problem that both numerator and
denominator tend to infinity, because an ideal
plane wave is strictly not a normalizable wave
function. The trick to use is to choose the
limits of integration from, say, -L/2 to +L/2 in
a region of length L. The factor L cancels out in
the numerator and denominator. Then we can
consider L approaches infinity. For wave
functions that are normalizable, such a
mathematical trickdoes not have to be used.")
```

Energy Bands and Charge Carriers in Semiconductors

Scilab code Exa 3.1 free electron momentum

```
1 //j=complex(0,1);
2 //psi = U*exp(j*k*x);
3 disp("px = h_cross*k(x)");
4 disp("With infinite limits of integration, both the
numerator and denominator are infinite. For
problems of this type, one integrates between the
finite limits -LI2 and +L/2 and, in the final
result, then assumes that L approaches infinity.
This result implies that (E, k) diagrams can be
considered plots of electron energy vs. momentum,
with a scaling factor h_cross.")
```

Scilab code Exa 3.2 E k Rleationship



Figure 3.1: E k Rleationship

1 //p = m*v 2 //p = h*k; //electron momentum, where h is constant 3 //E = 0.5*p*p/m 4 //E = 0.5*h*k*k/m; //electron energy 5 k = -10:0.01:10; //limits on wave vector k 6 E = k^2; // E is proportional to square of wave vector 7 plot(k,E)

Scilab code Exa 3.3 radius of electron orbit

```
1 n = 1;
2 epsilonr = 11.8; //relative dielectric constant for
    silicon
3 epsilon = 8.85*10^-12; //dielectric constant
4 m = 9.11*10^-31; //mass of electron
5 mn = 0.26*m; //for silicon
6 h = 6.63*10^-34;
7 q = 1.6*10^-19; //electronic charge
8 r = 10^10*(epsilonr*epsilon*h*h)/(mn*q*q*%pi); //
    radius in armstrong
9 disp(r, "radius of electron orbit around donor (in
    armstrong) =")
10 disp("This is more than 4 lattice spacings a = 5.43
```

```
armstrong.")
```

Scilab code Exa 3.4 density of states effective mass

Scilab code Exa 3.5 equilibrium hole concentration

Scilab code Exa 3.6 conductivity effective mass

Scilab code Exa 3.7 current and resistance in a Si bar

```
1 un= 700;
2 q = 1.6*10^-19;
3 n0 = 10^17;
4 L = 0.1;
5 A = 10^-6;
6 V = 10;
7 sigma = q*un*n0;
8 rho = 1/sigma;
9 R = rho*L/A;
10 I = V/R;
11 disp(sigma, "Conductivity (in per ohm-cm)=")
12 disp(rho, "resistivity (in ohm-cm)=")
13 disp(R, "resistance (in ohm)=")
14 disp(I, "current (in ampere)=")
```

Scilab code Exa 3.8 concentration and mobility of majority carrier

```
1 w = 0.01;
2 w1 = w*10^{-3}
3 t = 10^{-3};
4 L = 0.5;
5 B = 10 * 10^{-5};
6 I = 10^{-3};
7 Vab = -2 * 10^{-3};
8 Vcd = 0.1;
9 q = 1.6 * 10^{-19};
10 q1 = q*10^{-3}
11 n0 = I*B/(q1*-Vab);
12 rho = (Vcd/I)/(L/w1);
13 u = 1/(rho*q*n0);
14 disp(n0," electron concentration (in per cubic
      centimeter = ")
15 disp(rho, "resisitivity (in ohm-cm)=")
```

16 disp(u,"mobility (in square cm per volt-sec)=")

Excess Carriers in Semiconductors

Scilab code Exa 4.1 Excitation and band to band recombination leading to photoluminescence

```
1 t = 0.46 *10^-4;
2 hv = 2;
3 alpha = 5*10^4;
4 I0 = 10^-2;
5 It = I0*exp(-alpha*t);
6 Pabs = I0 - It;
7 f = (2-1.43)/2;
8 P = f*Pabs;
9 n = Pabs/(1.6*10^-19*hv);
10 disp(Pabs,"total energy absorbed per second (in watt
)=")
11 disp(P,"amount of energy converted to heat per
second (in watt)=")
12 disp(n,"number of photons per second given off form
recombination events =")
```



Figure 4.1: decay of excess population for a carrier recombination

Scilab code Exa 4.2 decay of excess population for a carrier recombination

```
1 \text{ p0} = 10^{15};
2 \text{ ni} = 10^{6};
3 n0 = ni^2/p0;
4 disp(n0," Minority electron concentration (in per
      cubic centimeter)=")
5 \, dn = 10^{14};
6 \, dp = 10^{14};
7 tn = 10; //in nanoseconds
8 \text{ tp} = \text{tn};
9 t = 0:10:50;
10 del_n = dn * exp(-t/tn);
11 del_p = dp*exp(-t/tp);
12 p = p0 + del_p;
13 n = del_n; //since n0 is negligible
14 subplot(121);
15 plot(t,log(p));
16 plot(t, log(n));
17 subplot(122);
```



Figure 4.2: decay of excess population for a carrier recombination

18 plot(t,p); 19 plot(t,n);

Scilab code Exa 4.3 steady state carrier generation

```
1 n0 = 10^14;
2 ni = 1.5*10^10;
3 Tn = 2 *10^-6;
4 Tp = 2 *10^-6;
5 p = 2*10^13;
6 p0 = ni^2/n0;
7 disp(p0,"hole concentration (per cubic centimeter)="
)
```

Scilab code Exa 4.4 electron quasi fermi level position and carrier concentration

```
1 n0 = 10^14;
2 dn = 2*10^13;
3 n = n0+dn;
4 kT = 0.0259;
5 ni = 1.5*10^10;
6 Ei = kT*log(n0/ni);
7 Fn = Ei + kT*log(n/ni);
8 E = Fn-Ei;
9 disp(n,"steady state electron concentration=")
10 disp(Ei,"equilibrium Fermi level (in eV)=")
11 disp(E,"electron quasi Fermi level position(in eV)=")
```

Scilab code Exa 4.5 diffusion length and hole current

```
1 A = 0.5;
2 \text{ Na} = 10^{17};
3 \, p0 = Na;
4 ni = 1.5 \times 10^{10};
5 \, dp = 5*10^{16};
6 x = 10^{-5};
7 \text{ up} = 500;
8 Tp = 10^{-10};
9 kT = 0.0259;
10 \ q0 = 1;
11 q = 1.6 \times 10^{-19};
12 Dp = kT*up/q0;
13 Lp = sqrt(Dp*Tp);
14 p = p0 + dp * exp(-x/Lp);
15 E = kT * log(p/ni);
16 E0 = 1.1/2 + E;
17 Ip = q*A*Dp*dp*exp(-x/Lp)/Lp;
18 Qp = q*A*dp*Lp;
19 Qp0 = Qp*10^{6};
20 disp(E0," steady state separation between Fp and Ec (
```

Scilab code Exa 4.6 Haynes Shockley experiment

```
1 l = 1;
2 d = 0.95;
3 E0 = 2;
4 t = 0.25*10^-3;
5 dt = 117*10^-6;
6 up = (d/t)/(E0/1);
7 Dp = dt^2*d^2/(16*t^3);
8 C = Dp/up;
9 kT = 0.0259;
10 disp(up,"hole mobility (in square cm per Volt-second
)=")
11 disp(Dp," diffusion coefficient (in square cm per
second)=")
12 disp(C," Diffisuion coefficient/Hole mobility (in
volts) = ")
```

13 disp("Verified according to Einstein Relation")

Junctions

Scilab code Exa 5.1 contact potential and fermi level position

```
1 Na = 10^18;
2 Nd = 5*10^15;
3 ni = 1.5*10^10;
4 kT = 0.0259;
5 E1 = kT*log(Na/ni);
6 E2 = kT*log(Nd/ni);
7 qV1 = E1+E2;
8 qV2 = kT*log(Na*Nd/ni^2);
9 disp(E1,"Fermi level position in p region (in eV)=")
10 disp(E2,"Fermi level position in n region (in eV)=")
11 disp(qV1,"Contact potential (in eV)=")
12 disp(qV2,"Contact potential (in eV)=")
13 disp("Contact potential value verified")
```

Scilab code Exa 5.2 electric field and charge density in junction

1 Na = 10¹⁸; 2 Nd = 5*10¹⁵;

```
3 \text{ ni} = 1.5 * 10^{10};
4 kT = 0.0259;
5 \text{ epsilon0} = 8.85*10^{-14};
6 \text{ epsilon} = 11.8;
7 q = 1.6 * 10^{-19};
8 E1 = kT * log(Na/ni);
9 E2 = kT * \log(Nd/ni);
10 \text{ qV1} = \text{E1+E2};
11 qV2 = kT * log(Na * Nd/ni^2);
12 \ d = 10*10^{-4}; //in \ centimetre
13 A = %pi*d^2/4;
14 W = sqrt(2*epsilon*epsilon0*qV1/q *(Na<sup>-1</sup> + Nd<sup>-1</sup>));
15 \text{ xn0} = W/(1+(Nd/Na));
16 \text{ xp0} = W/(1+(Na/Nd));
17 Q = q * A * xn0 * Nd;
18 E0 = -q*xn0*Nd/(epsilon*epsilon0);
19 disp(W*10<sup>4</sup>, "width of the transition region(in
      micron = ")
20 disp(xn0*10<sup>4</sup>, "penetration of the space charge
       region into the n material (in micron)=")
21 disp(xp0*10^4," penetration of the space charge
      region into the p material (in micron)=")
22 disp(Q," total uncompensated charge (in coulomb)=")
23 disp(E0, "maximum electric field(in V per cm)=")
```

Scilab code Exa 5.4 Current in forward and reverse biased pn junction

```
1 A = 10<sup>-4</sup>;
2 kT = 0.0259;
3 ni = 1.5*10<sup>10</sup>;
4 q = 1.6*10<sup>-19</sup>;
5 q0 = 1;
6 Na = 10<sup>17</sup>;
7 Nd = 10<sup>15</sup>;
8 Tn = 10<sup>-7</sup>;
```

```
9 Tp = 10^{-5};
10 \text{ upp} = 200;
11 unn = 1300;
12 unp = 700;
13 \text{ upn} = 450;
14 V1 = 0.5;
15 \quad V2 = -0.5;
16 pn = ni^2/Nd;
17 np = ni^2/Na;
18 Dp = kT*upn/q0;
19 Dn = kT*unp/q0;
20 Lp = sqrt(Dp*Tp);
21 Ln = sqrt(Dn*Tn);
22 I1 = q*A*((Dp*pn/Lp)+(Dn*np/Ln))*(exp(q0*V1/kT)-1);
23 I2 = -q*A*((Dp*pn/Lp)+(Dn*np/Ln));
24 disp(pn,"hole concentration (per cubic centmeter)=")
25 disp(np," electron concentration (per cubic centmeter
      )=")
26 disp(Dp," diffusion coefficient on n side (in square
      centimter per second)=")
27 disp(Dn," diffusion coefficient on p side(in square
      centimter per second)=")
  disp(I1*10<sup>6</sup>, "current at forward bias (in
28
      microampere)=")
29 disp(I2*10<sup>6</sup>, "current at reverse bias (in
      microampere)=")
```

Scilab code Exa 5.6 depletion capacitance

```
1 A = 10<sup>-4</sup>;
2 kT = 0.0259;
3 ni = 1.5*10<sup>10</sup>;
4 q = 1.6*10<sup>-19</sup>;
5 Na = 10<sup>17</sup>;
6 Nd = 10<sup>15</sup>;
```

```
7 epsilon0 = 8.85*10^-14;
8 epsilon = 11.8;
9 E1 = kT*log(Na/ni);
10 E2 = kT*log(Nd/ni);
11 V0 = E1+E2;
12 V = -4;
13 Cj = sqrt(epsilon*epsilon0)*A*sqrt(q*Nd*Na/(2*(V0-V)
*(Na+Nd)));
14 disp(V0,"V0 (in volt)=")
15 disp(Cj,"total depletion constant (in farad)=")
```

Scilab code Exa 5.7 Heterojunctions

```
1 dEtg = 1.85;
2 band_gap = 1.43; //for GaAs-AlGaAs system
3 dEg = dEtg - band_gap;
4 dEc = dEg*2/3;
5 dEv = dEg/3;
6 disp(dEc, "Conduction band offset(in eV) =")
7 disp(dEv, "Valence band offset(in eV) =")
```

Field Effect Transistors

Scilab code Exa 6.1 mos transistor

```
1 kT = 0.0259;
2 ni = 1.5*10^{10};
3 q = 1.6 * 10^{-19};
4 \quad q0 = 1;
5 \text{ epsilon0} = 8.85*10^{-14};
6 \text{ epsilon} = 11.8;
7 epsiloni = 3.9;
8 Na = 5*10^{15};
9 \, d = 10^{-6};
10 Qi = 4*10^{10*q};
11 Vf = kT * log(Na/ni)/q0;
12 Wm = 2*sqrt(epsilon*epsilon0*Vf/(q*Na));
13 Vms = -0.95;
14 Ci = epsiloni*epsilon0/d;
15 Vfb = Vms -(Qi/Ci);
16 Qd = -q * Na * Wm;
17 Vt = Vfb-Qd/Ci+2*Vf;
18 Cd = epsilon*epsilon0/Wm;
19 Cmin = Ci*Cd/(Ci+Cd);
20 disp(Vf, "Phi(F) (in eV)=")
21 disp(Wm*10^4, "W(m) (in micron)=")
```

```
22 disp(Qi,"effective interface charge (in coulomb per
square cm)=")
23 disp(Ci*10^6,"C(i) (in microfarad per square cm)=")
24 disp(Vfb,"V(fb)(in V)=")
25 disp(Qd,"Q(d)(in coulomb per square cm)=")
26 disp(Vt,"V(T) (in V)=")
27 disp(Cd*10^6,"C(d) (in microfarad per square cm)=")
```

28 disp(Cmin, "C(min) (in farad per square cm)=")

Scilab code Exa 6.2 drain current in mosfet

```
1 kT = 0.0259;
2 ni = 1.5*10^{10};
3 q = 1.6*10^{-19};
4 \quad q0 = 1;
5 \text{ epsilon0} = 8.85*10^{-14};
6 \text{ epsilon} = 11.8;
7 epsiloni = 3.9;
8 Na = 5*10^{15};
9 \, d = 10^{-6};
10 Vt = 0.6;
11 Z = 25 * 10^{-4};
12 L = 10^{-4};
13 \text{ Vg1} = 5;
14 \, Vd1 = 0.1;
15 \ Vg2=3;
16 \, Vd2=5;
17 Vdsat = Vg2-Vt;
18 Vd3=7;
19 un = 200;
20 Ci = epsiloni*epsilon0/d;
21 Id1 = (Z*un*Ci/L)*((Vg1-Vt)*Vd1-0.5*Vd1^2); //linear
       region
22 Id2 = (Z*un*Ci/L)*((Vg2-Vt)*Vdsat-0.5*Vdsat^2); //
      saturation region
```

```
23 disp(Ci*10<sup>6</sup>, "C(i) (in microfarad per square cm)=")
```

- 24 disp(Id1*10^3, "For V(G)=5V and V(D)=0.1V, we are in the linear region and drain current (in miliampere)=")
- 25 disp(Id2*10^3, "For V(G)=3V and V(D)=5V, we are in the saturation region and drain current (in miliampere)=")
- 26 disp("For VD = 7 V, ID will not increase, because we are in the saturation region.")

Scilab code Exa 6.3 ion implantation

```
1 q = 1.6 * 10^{-19};
2 q0 = 1;
3 \text{ epsilon0} = 8.85*10^{-14};
4 \text{ epsilon} = 11.8;
5 epsiloni = 3.9;
6 d = 10^{-6};
7 Vt1 = -1.1;
8 Vt2 = -0.5;
9 I = 10^{-5};
10 \quad A = 650;
11 Ci = epsiloni*epsilon0/d;
12 Fb = (Vt2-Vt1)*Ci/q;
13 t = Fb*q*A/I;
14 disp(Ci*10^6, "C(i) (in microfarad per square cm)=")
15 disp(Fb, "boron ion dose required (in per square cm)=
      ")
16 disp(t,"implant time (in second)=")
```

Bipolar Junction Transistor

Scilab code Exa 7.1 steady state charge in transistor

Scilab code Exa 7.4 bjt saturation current

1 A=10⁻⁴; 2 q = 1.6*10⁻¹⁹; 3 kT = 0.0259; 4 Wb = 10⁻⁴; 5 ni = 1.5*10¹⁰;

```
6 \text{ Na} = 10^{17};
7 Tn = 10^{-7};
8 \text{ upe}=200;
9 \text{ une} = 700;
10 Nd = 10^{15};
11 Tp=10<sup>-5</sup>;
12 unb=1300;
13 upb=450;
14 Veb = 0.3;
15 \text{ Vcb} = -40;
16 pn = ni^2/Nd;
17 Dp = upb*kT;
18 Lp = sqrt(Dp*Tp);
19 Ies = q*A*Dp*pn/Lp*(csch(Wb/Lp)+tanh(Wb/Lp));
20 dpe = pn * exp(Veb/kT);
21 Ib = q*A*Dp*dpe/Lp*tanh(Wb/2*Lp);
22 Ib1 = q*A*Wb*dpe/(2*Tp);
23 Dn = kT*une;
24 Ln = sqrt(Dn*Tn);
25 \quad \texttt{gamma1} = (1+((Dn*Lp*Nd))/(Dp*Ln*Na))*tanh(Wb/Lp))^{-1};
26 B = sech(Wb/Lp);
27 alpha = B*gamma1;
28 \text{ beta1} = alpha/(1-alpha);
29 disp(pn," hole concentration (in per cubic centimeter
      )=")
30 disp(Dp,"Dp (in sqaure centimeter per second)=")
31 disp(Lp*10, "Lp(in micrometer) =")
32 disp(dpe, "dp(E)(in per cubic centimeter) =")
33 disp(Ies, "I(ES) (in ampere)=")
34 disp(Ib1,"I(B) (in ampere)=")
35 disp(Dn,"Dn (in sqaure centimeter per second)=")
36 disp(Ln*10,"Ln (in micrometer)=")
37 disp(gamma1, "gamma =")
38 disp(B, "B =")
39 disp(alpha, "alpha =")
40 disp(beta1, "beta =")
```

Optoelectronic Devices

Scilab code Exa 8.2 solar cells

```
1 Isc=100;
2 Voc=0.8;
3 ff = 0.7;
4 Pmax = ff*Isc*Voc;
5 disp(Pmax,"maximum power delivered(in miliwatt)=")
```

Scilab code Exa 8.3 fibre optic communication

```
1 wavelength = 0.68;
2 Eg = 1.24/wavelength;
3 disp(Eg,"band gap (in eV)=")
4 disp("From Fig, 3-6, we get Al(0.32)Ga(0.68)As. From
Fig. 8-11, we get GaAs(0.68)P(0.32)")
```