

Scilab Textbook Companion for
Trigonometry
by M. Corral¹

Created by
S Sai Ashrith Reddy
B.Tech
Electrical Engineering
NITK
College Teacher
None
Cross-Checked by
Chaitanya Potti

July 16, 2014

¹Funded by a grant from the National Mission on Education through ICT, <http://spoken-tutorial.org/NMEICT-Intro>. This Textbook Companion and Scilab codes written in it can be downloaded from the "Textbook Companion Project" section at the website <http://scilab.in>

Book Description

Title: Trigonometry

Author: M. Corral

Publisher: Createspace Independent Publishing North Charlesth

Edition: 2

Year: 2010

ISBN: 9781475074574

Scilab numbering policy used in this document and the relation to the above book.

Exa Example (Solved example)

Eqn Equation (Particular equation of the above book)

AP Appendix to Example(Scilab Code that is an Appednix to a particular Example of the above book)

For example, Exa 3.51 means solved example 3.51 of this book. Sec 2.3 means a scilab code whose theory is explained in Section 2.3 of the book.

Contents

List of Scilab Codes	4
1 Right Triangle Trigonometry	11
2 General Triangles	55
3 Identities	76
4 Radian Measure	77
5 Graphing and inverse functions	91
6 Additional Topics	116
8 Appendix B	125

List of Scilab Codes

Exa 1.1	To determine unknown angle in 3 given triangles . . .	11
Exa 1.3	To determine length of unknown side in 3 given right triangles	12
Exa 1.4	To determine height of the top of ladder touching the wall	13
Exa 1.5	To find values of all trigonometric functions for angles A and B	15
Exa 1.6	To find values of all trigonometric functions for 45 degree	18
Exa 1.7	To find values of all trigonometric functions for 60 degree	19
Exa 1.8	To find all trigonometric functions when sine functions is given	21
Exa 1.9	To convert given function into function of angle less than 45	23
Exa 1.10	To find sine cosine and tangent functions for 75 degree	24
Exa 1.11	To find the height of the flagpole	27
Exa 1.12	To find the height of mountain	28
Exa 1.13	To find the horizontal distance from blimp to house . .	29
Exa 1.14	To estimate radius of earth when angle of depression is known	30
Exa 1.15	To find the distance from centre of earth to sun	32
Exa 1.16	To determine the radius of sun	34
Exa 1.17	To determine the diameter of larger roller	35
Exa 1.19	To solve the right triangle with given information . . .	37
Exa 1.20	To find values of all trigonometric values of given angle of 120	39
Exa 1.21	To find values of all trigonometric values of given angle of 225	41

Exa 1.22	To find values of all trigonometric values of given angle of 330	43
Exa 1.23	To find trigonometric ratios of 0 90 180 and 270 degrees	45
Exa 1.24	To determine reference angle and angle between 0 to 360 with same terminal side as given angle	49
Exa 1.25	To find sin theta and tan theta when cos theta is given	51
Exa 1.27	To find all the angles with a given sine function value	53
Exa 2.1	To solve the triangle when one side and 2 angles are given	55
Exa 2.2	To solve the triangle when 2 sides and one opposite angle is given	57
Exa 2.3	To solve the triangle when 2 sides and opposite angle is given	57
Exa 2.4	To solve the triangle when 2 sides and angle between them is given	58
Exa 2.5	To solve the triangle when 2 sides and angle between them is given	60
Exa 2.6	To solve the triangle when 3 sides are given	60
Exa 2.7	To determine solution of a triangle when 3 sides are given	61
Exa 2.8	To solve the triangle when 2 sides and opposite angle is given	63
Exa 2.10	To solve the triangle when 2 sides and included angle is given	64
Exa 2.11	To check the solution of triangle using Mollweide equation	65
Exa 2.12	To determine if a triangle can be formed with given dimension	66
Exa 2.13	To determine area of triangle when 2 sides and an angle is given	67
Exa 2.14	To determine area of triangle when 3 angles and a side is given	68
Exa 2.15	To determine area of triangle when 3 sides are given	69
Exa 2.16	To determine area of triangle when 3 sides are given	70
Exa 2.17	To find radius of circumscribed circle for triangle ABC	71
Exa 2.18	To find the radius of circumscribed circle for triangle ABC	73
Exa 2.19	To determine radius of inscribed circle ABC	74
Exa 3.8	To determine values of functions of sum of 2 angles when functions of 2 angles are given	76

Exa 4.1	To convert a degree measure to radians	77
Exa 4.2	To convert a radian measure to degree	77
Exa 4.3	To determine length of the intercepted arc	78
Exa 4.4	To determine length of the arc intercepted	78
Exa 4.5	To determine angle in radians and degrees	78
Exa 4.6	To determine the length of the rope	79
Exa 4.7	To determine the length of the belt around the pulleys	81
Exa 4.8	To find the area of sector of circle	82
Exa 4.9	To determine area of sector of a circle	82
Exa 4.10	To determine area of sector of circle	83
Exa 4.11	To determine area insude belt pulley system	84
Exa 4.12	To determine area of segment formed by a chord in circle	85
Exa 4.13	To determine area of intersection of 2 circles	86
Exa 4.14	To find linear and angular speed of a moving object .	87
Exa 4.15	To find linear and angular speed of a moving object .	88
Exa 4.16	To find the central angle swept by a moving object . .	88
Exa 4.17	To find the angular speed of larger gear interlocked with smaller gear	89
Exa 5.1	To sketch the graph of minus $\sin x$ in a given interval .	91
Exa 5.2	To sketch the graph of given function of in given interval	93
Exa 5.4	To determine the period of given sinusoidal function .	94
Exa 5.5	To determine the period of 2 given cosine functions . .	95
Exa 5.6	To determine the amplitude and period of given function	97
Exa 5.7	To find amplitude and period of given composite func- tion	99
Exa 5.8	To find the amplitude and period of given function . .	102
Exa 5.9	To find the amplitude and period of given function . .	104
Exa 5.10	To find the period of given function	107
Exa 5.11	To find the amplitude phase shift and period of given function	108
Exa 5.12	To find the amplitude phase shift and period of given function	110
Exa 5.13	To determine inverse sine function of a given value . .	113
Exa 5.14	To determine inverse sine function of a given value . .	113
Exa 5.15	To determine inverse cosine function of a given value .	113
Exa 5.16	To determine inverse cosine function of a given value .	114
Exa 5.17	To determine inverse tan function of a given value . .	114
Exa 5.18	To determine inverse tan function of a given value . .	115

Exa 5.19	To determine exact value of given expression involving inverse trigonometric functions	115
Exa 6.3	To solve the given equation	116
Exa 6.4	To solve the given equation	116
Exa 6.9	To find the result of basic operations on 2 given complex numbers	117
Exa 6.10	To represent given complex number in trigonometric form	118
Exa 6.11	To determine product and ratio of complex numbers using formula	119
Exa 6.12	To find higher powers of complex number using demoivre theorem	120
Exa 6.13	To determine the cube roots of i	120
Exa 6.15	To convert from polar to cartesian coordinates	121
Exa 6.16	To convert from cartesian to polar coordinates	122
Exa 6.17	To express an equation in polar coordinates	123
Exa 6.19	To express an equation in polar coordinates	123
Exa 8.1	To plot the function of $\sin x$	125

List of Figures

1.1	To determine unknown angle in 3 given triangles	11
1.2	To determine length of unknown side in 3 given right triangles	12
1.3	To determine height of the top of ladder touching the wall .	14
1.4	To find values of all trigonometric functions for angles A and B	15
1.5	To find values of all trigonometric functions for 45 degree . .	17
1.6	To find values of all trigonometric functions for 60 degree . .	20
1.7	To find all trigonometric functions when sine functions is given	22
1.8	To convert given function into function of angle less than 45	23
1.9	To find sine cosine and tangent functions for 75 degree	25
1.10	To find the height of the flagpole	27
1.11	To find the height of mountain	28
1.12	To find the horizontal distance from blimp to house	30
1.13	To estimate radius of earth when angle of depression is known	31
1.14	To find the distance from centre of earth to sun	33
1.15	To determine the radius of sun	34
1.16	To determine the diameter of larger roller	36
1.17	To solve the right triangle with given information	38
1.18	To find values of all trigonometric values of given angle of 120	40
1.19	To find values of all trigonometric values of given angle of 225	42
1.20	To find values of all trigonometric values of given angle of 330	44
1.21	To find trigonometric ratios of 0 90 180 and 270 degrees	46
1.22	To determine reference angle and angle between 0 to 360 with same terminal side as given angle	50
1.23	To find sin theta and tan theta when cos theta is given	51
1.24	To find all the angles with a given sine function value	53
2.1	To solve the triangle when one side and 2 angles are given .	56

2.2	To solve the triangle when 2 sides and one opposite angle is given	56
2.3	To solve the triangle when 2 sides and angle between them is given	58
2.4	To solve the triangle when 2 sides and angle between them is given	59
2.5	To solve the triangle when 3 sides are given	61
2.6	To determine solution of a triangle when 3 sides are given . .	62
2.7	To solve the triangle when 2 sides and included angle is given	65
2.8	To determine area of triangle when 2 sides and an angle is given	67
2.9	To determine area of triangle when 3 angles and a side is given	68
2.10	To determine area of triangle when 3 sides are given	69
2.11	To find radius of circumscribed circle for triangle ABC	71
2.12	To find the radius of circumscribed circle for triangle ABC .	72
2.13	To determine radius of inscribed circle ABC	74
4.1	To determine the length of the rope	80
4.2	To determine the length of the belt around the pulleys	81
4.3	To determine area insude belt pulley system	83
4.4	To determine area of segment formed by a chord in circle . .	85
4.5	To determine area of intersection of 2 circles	86
4.6	To find the angular speed of larger gear interlocked with smaller gear	89
5.1	To sketch the graph of minus $\sin x$ in a given interval	92
5.2	To sketch the graph of minus $\sin x$ in a given interval	92
5.3	To sketch the graph of given function of in given interval . .	93
5.4	To sketch the graph of given function of in given interval . .	94
5.5	To determine the period of given sinusoidal function	94
5.6	To determine the period of given sinusoidal function	96
5.7	To determine the period of 2 given cosine functions	96
5.8	To determine the period of 2 given cosine functions	98
5.9	To determine the amplitude and period of given function . . .	98
5.10	To determine the amplitude and period of given function . . .	100
5.11	To find amplitude and period of given composite function . .	100
5.12	To find amplitude and period of given composite function . .	102
5.13	To find the amplitude and period of given function	103
5.14	To find the amplitude and period of given function	104

5.15	To find the amplitude and period of given function	105
5.16	To find the amplitude and period of given function	106
5.17	To find the period of given function	107
5.18	To find the period of given function	109
5.19	To find the amplitude phase shift and period of given function	109
5.20	To find the amplitude phase shift and period of given function	111
5.21	To find the amplitude phase shift and period of given function	111
5.22	To find the amplitude phase shift and period of given function	112
8.1	To plot the function of $\sin x$	126
8.2	To plot the function of $\sin x$	127

Chapter 1

Right Triangle Trigonometry

Scilab code Exa 1.1 To determine unknown angle in 3 given triangles

```
1  clc, clear
2  //example 1.1
3  //To determine unknown angle in 3 given triangles
4
5  //Triangle ABC
6  A = 35 //angle at vertex A in degrees
7  C = 20 //angle at vertex C in degrees
8  B=180- (A+C) //unknown angle
9  printf('Triangle ABC: B = %.0f degree\n',B)
10
11 //Triangle DEF
```

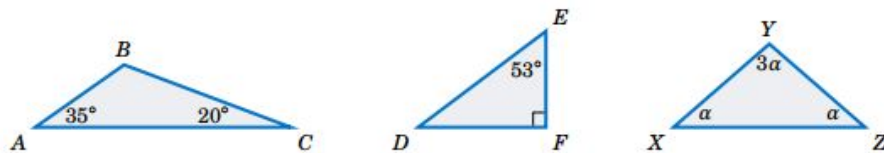


Figure 1.1: To determine unknown angle in 3 given triangles

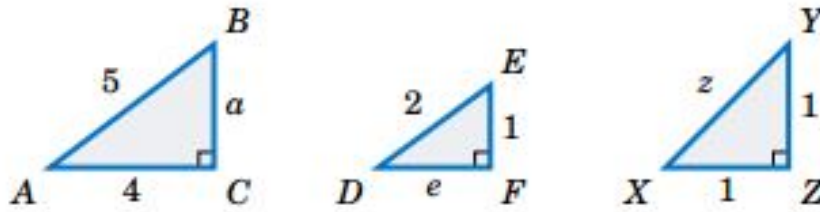


Figure 1.2: To determine length of unknown side in 3 given right triangles

```

12 E = 53 //angle at vertex E in degree
13 //F = 90, DEF is right triangle
14 //So angles E and D are complimentary
15 D = 90 - E //unknown angle
16 printf(' Triangle DEF: D = %.0f degree\n',D)
17
18 //Triangle XYZ
19 sum_multiple= 1+3+1 //for solving for alpha
20 alpha = 180/ sum_multiple
21 X= alpha //unknown angle
22 Y= 3* alpha //unknown angle
23 Z= alpha //unknown angle
24 printf(' Triangle XYZ: X=%.0f degree Y=%.0f degree Z
    =%.0f degree ',X,Y,Z)

```

Scilab code Exa 1.3 To determine length of unknown side in 3 given right triangles

```

1 clc,clear
2 //example 1.3
3 //To determine length of unknown side in 3 given
  right triangles
4
5 //Triangle ABC

```

```

6 AB=5 //given
7 AC=4 //given
8 a=sqrt(AB^2- AC^2) //by pythagoras theorem
9 printf('Triangle ABC: a=%f units \n',a)
10
11 //Triangle DEF
12 DE=2 //given
13 EF=1 //given
14 e=sqrt(DE^2- EF^2) //by pythagoras theorem
15 printf(' Triangle DEF: e=%f units = sqrt(%f) units\n
        ',e,e^2)
16
17 //Triangle XYZ
18 XZ=1 //given
19 YZ=1 //given
20 z=sqrt(XZ^2+YZ^2) //by pythagoras theorem
21 printf(' Triangle XYZ: z=%f units = sqrt(%f) units\n
        ',z,z^2)

```

Scilab code Exa 1.4 To determine height of the top of ladder touching the wall

```

1 clc ,clear
2 //example 1.4
3 //To determine height of the top of ladder touching
  the wall
4
5 ladder = 17 //length of ladder or hypotenuse in feet
6 base = 8 //distance between lower tip of ladder and
  wall in feet
7 //Using pythagoras theorem
8 h=sqrt(ladder^2 - base^2) //required height
9 printf('Required height of top of ladder in contact

```

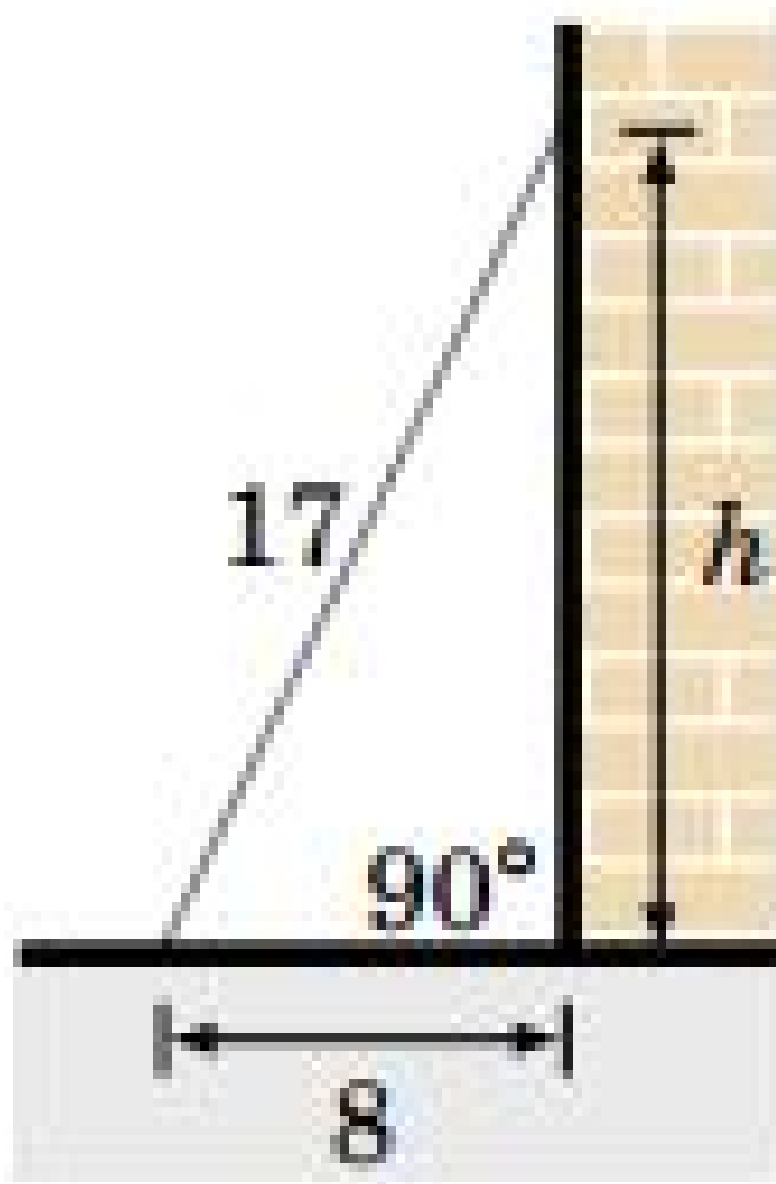


Figure 1.3: To determine height of the top of ladder touching the wall

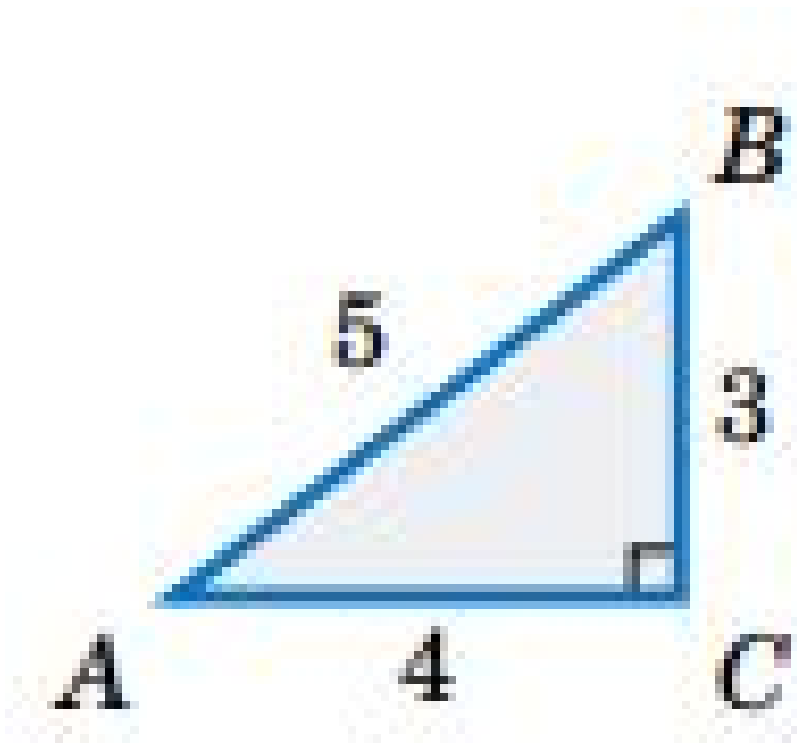


Figure 1.4: To find values of all trigonometric functions for angles A and B

```
with wall = %.0 f ft ',h)
```

Scilab code Exa 1.5 To find values of all trigonometric functions for angles A and B

```
1 clc, clear
2 //example 1.5
3 //To find values of all trigonometric functions for
  angles A and B
```



```

4
5 //Angle at vertex A
6 opposite = 3;
7 adjacent = 4;
8 hypotenuse=5;
9
10 sin_A = opposite / hypotenuse;
11 cos_A = adjacent / hypotenuse;
12 tan_A = opposite / adjacent;
13 csc_A = hypotenuse/opposite;
14 sec_A = hypotenuse/adjacent;
15 cot_A = adjacent / opposite;
16 printf('ANGLE A')
17 printf('\nsin(A)= %.1f ; cos(A)= %.2f; tan(A)=
    %.2f;\n',sin_A,cos_A,tan_A)
18 printf('csc(A)= %.3f ; sec(A)= %.2f; cot(A)= %.2f
    ;',csc_A,sec_A,cot_A)
19
20 //Angle at vertex B
21 opposite = 4;
22 adjacent = 3;
23 hypotenuse=5;
24
25 sin_B = opposite / hypotenuse;
26 cos_B = adjacent / hypotenuse;
27 tan_B = opposite / adjacent;
28 csc_B = hypotenuse/opposite;
29 sec_B = hypotenuse/adjacent;
30 cot_B = adjacent / opposite;
31 printf('\n\nANGLE B')
32 printf('\nsin(B)= %.1f ; cos(B)= %.2f; tan(B)=
    %.2f;\n',sin_B,cos_B,tan_B)
33 printf('csc(B)= %.2f ; sec(B)= %.2f; cot(B)= %.2
    f;',csc_B,sec_B,cot_B)

```

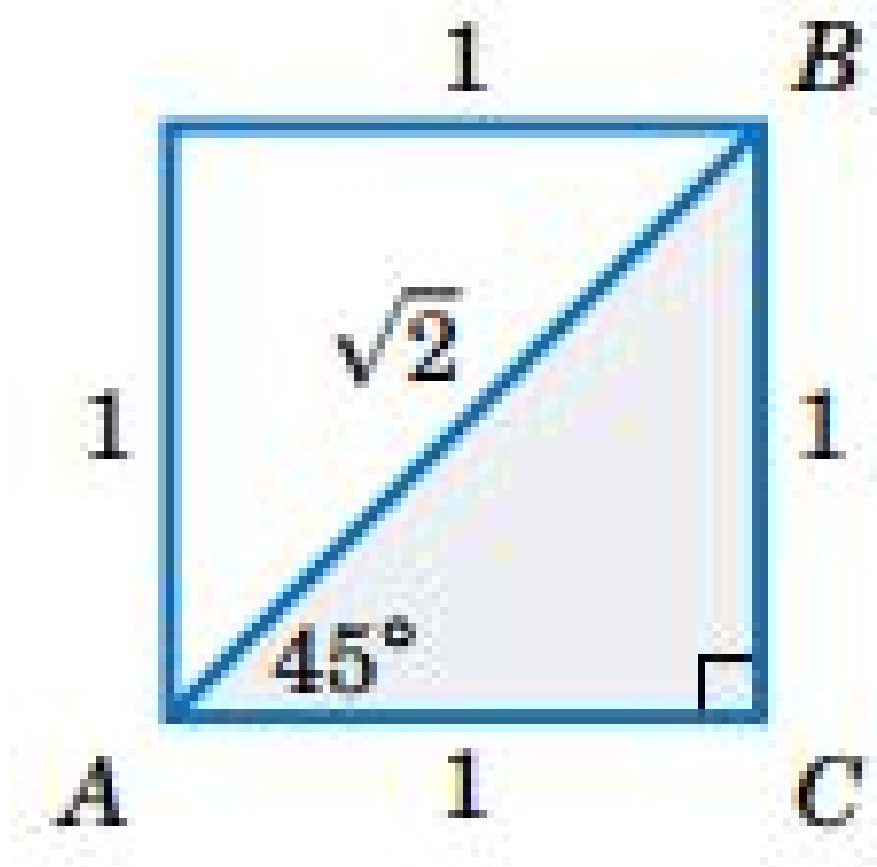


Figure 1.5: To find values of all trigonometric functions for 45 degree

Scilab code Exa 1.6 To find values of all trigonometric functions for 45 degree

```
1  clc, clear
2  //example 1.6
3  //To find values of all trigonometric functions for
   45 degree
4
5  //Consider a square of side 1 and divide it half
   diagonally
6  //ABC is now an isosceles triangle
7  //angle A and B are now equal and = 45 degree
8
9  AC=1;
10 BC=1;
11 AB=sqrt(AC^2+BC^2) //by pythagoras theorem
12 c=AB //we denote AB by c as its opposite to C
13
14 //consider angle BAC=45 degree
15 opposite = BC;
16 adjacent = AC;
17 hypotenuse = c;
18 sin_45 = opposite / hypotenuse;
19 cos_45 = adjacent / hypotenuse;
20 tan_45 = opposite / adjacent;
21 csc_45 = hypotenuse/opposite;
22 sec_45 = hypotenuse/adjacent;
23 cot_45 = adjacent / opposite;
24
25 printf('ANGLE = 45 degree')
26 printf(' \nsin(45)= %.4f ; cos(45)= %.4f; tan(45)=
   %.2f; \n', sin_45, cos_45, tan_45)
27 printf(' csc(45)= %.4f ; sec(45)= %.4f; cot(45)= %
   .2f; ', csc_45, sec_45, cot_45)
```

Scilab code Exa 1.7 To find values of all trigonometric functions for 60 degree

```
1  clc, clear
2  //example 1.7
3  //To find values of all trigonometric functions for
   60 degree
4
5  //take an equilateral triangle of side 2 and divide
   it by half
6  //all 3 angles of equilateral triangle are same as
   60 degree
7  //the bisector of angle is also the perpendicular
   bisector of opposite side
8  // Thus, A=60 B=30 C=90 in new triangle as shown in
   figure
9
10 AB = 2; c=AB;
11 AC = AB/2; b=AC;
12 a=sqrt(c^2-b^2)//pythagoras theorem
13
14 //For angle A=60 degree
15 opposite = a;
16 adjacent = b;
17 hypotenuse = c;
18 sin_60 = opposite / hypotenuse;
19 cos_60 = adjacent / hypotenuse;
20 tan_60 = opposite / adjacent;
21 csc_60 = hypotenuse/opposite;
22 sec_60 = hypotenuse/adjacent;
23 cot_60 = adjacent / opposite;
24 printf('ANGLE = 60 degree')
```

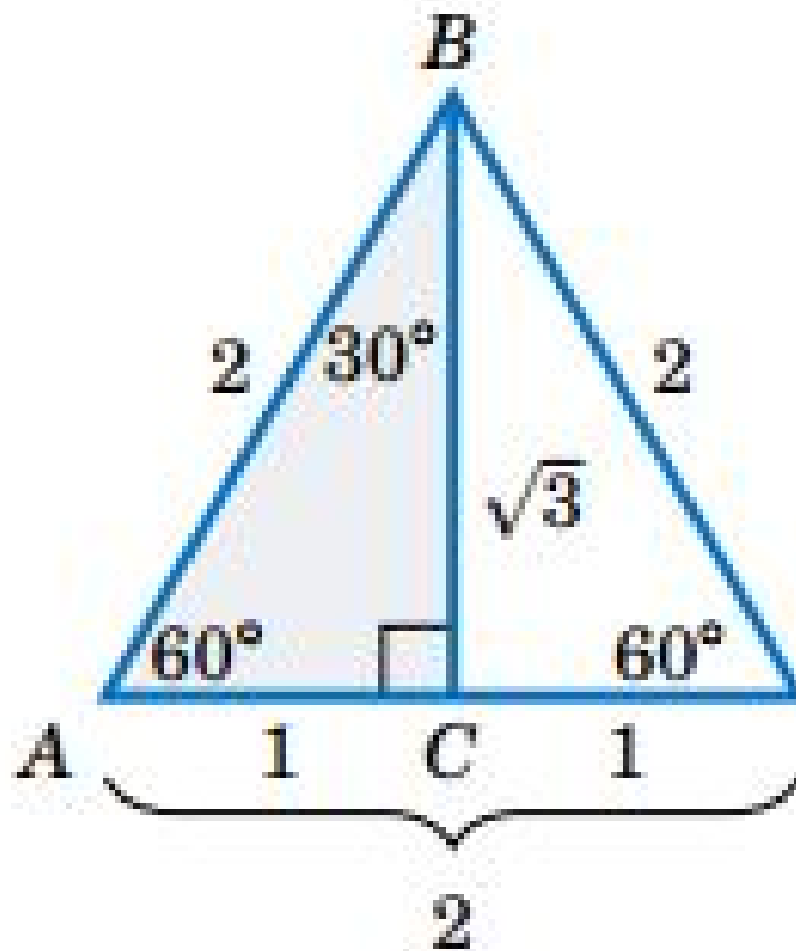


Figure 1.6: To find values of all trigonometric functions for 60 degree

```

25 printf('\nsin(60)= %.4f ; cos(60)= %.4f;    tan(60)=
    %.4f;\n',sin_60,cos_60,tan_60)
26 printf('csc(60)= %.4f ; sec(60)= %.4f;    cot(60)= %
    .4f;',csc_60,sec_60,cot_60)
27
28 //For angle ABC=30 degree
29 opposite = b;
30 adjacent = a;
31 hypotenuse = c;
32 sin_30 = opposite / hypotenuse;
33 cos_30 = adjacent / hypotenuse;
34 tan_30 = opposite / adjacent;
35 csc_30 = hypotenuse/opposite;
36 sec_30 = hypotenuse/adjacent;
37 cot_30 = adjacent / opposite;
38 printf('\n\nANGLE = 30 degree ')
39 printf('\nsin(30)= %.4f ; cos(30)= %.4f;    tan(30)=
    %.4f;\n',sin_30,cos_30,tan_30)
40 printf('csc(30)= %.4f ; sec(30)= %.4f;    cot(30)= %
    .4f;',csc_30,sec_30,cot_30)

```

Scilab code Exa 1.8 To find all trigonometric functions when sine functions is given

```

1  clc,clear
2  //example 1.8
3  //To find all trigonometric functions when sine
    functions is given
4
5  sin_A=2/3 //given
6  //since sine function is opposite/hypotenuse and
7  //T-ratios are defined interms of ratio of sided of
    right triangle

```

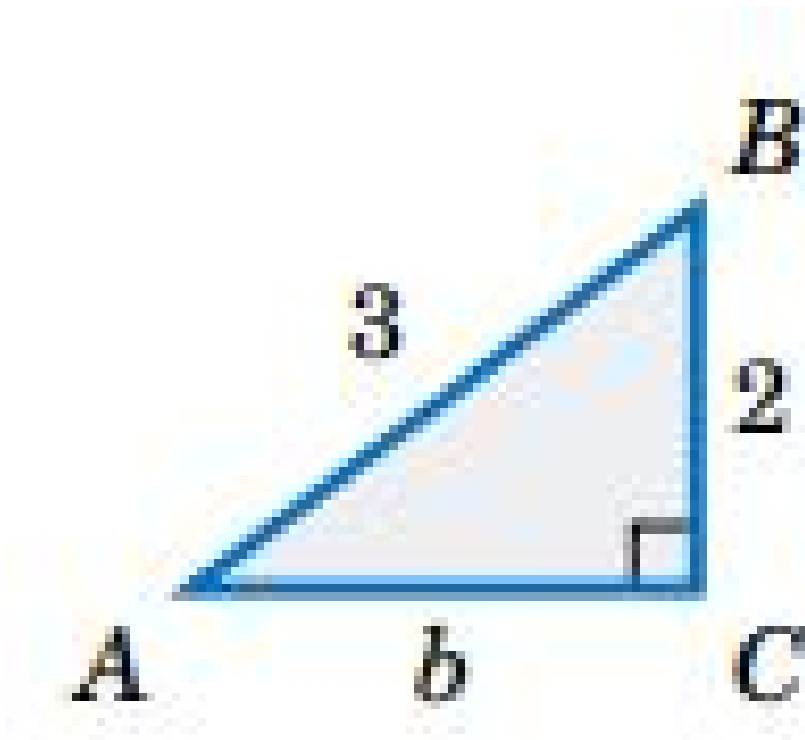


Figure 1.7: To find all trigonometric functions when sine functions is given



Figure 1.8: To convert given function into function of angle less than 45

```

8  opposite=2;
9  hypotenuse=3;
10 BC = opposite;
11 AB = hypotenuse;
12 b = sqrt(hypotenuse^2- opposite^2) //by pythagoras
    theorem
13 adjacent = b;
14
15 cos_A = adjacent / hypotenuse;
16 tan_A = opposite / adjacent;
17 csc_A = hypotenuse/opposite;
18 sec_A = hypotenuse/adjacent;
19 cot_A = adjacent / opposite;
20
21 printf('for ANGLE A')
22 printf('\nsin(A)= %.4f ; cos(A)= %.4f;    tan(A)= %
    .4f;\n',sin_A ,cos_A ,tan_A)
23 printf('csc(A)= %.4f ; sec(A)= %.4f;    cot(A)= %.4f
    ;',csc_A ,sec_A ,cot_A)

```

Scilab code Exa 1.9 To convert given function into function of angle less than 45

```
1 clc,clear
2 //example 1.9
3 //To convert given function into function of angle
  less than 45
4
5 //(a) sin 65
6 angle = 65 ;
7 complement_angle = 90- 65 ;
8 //cofunction of sine is cosine
9 printf('(a) sin(%f)= cos (%f)\n',angle ,
  complement_angle)
10
11 //(b) cos 78
12 angle = 78;
13 complement_angle = 90- 78 ;
14 //cofunction of cosine is sine
15 printf('(b) cos(%f)= sin (%f)\n',angle ,
  complement_angle)
16
17 //(c) tan 59
18 angle = 59 ;
19 complement_angle = 90- 59 ;
20 //cofunction of tan is cot
21 printf('(c) tan(%f)= cot (%f)\n',angle ,
  complement_angle)
```

Scilab code Exa 1.10 To find sine cosine and tangent functions for 75 degree

```
1 clc,clear
```

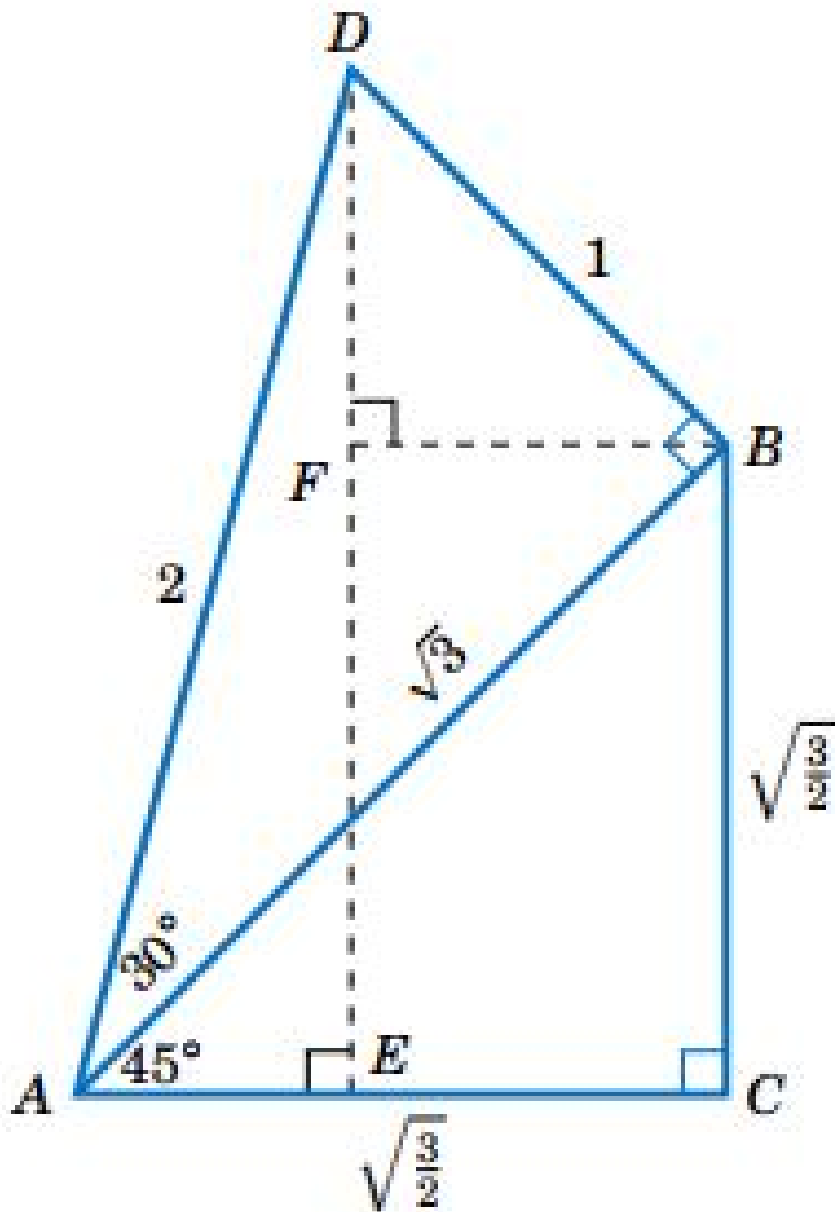


Figure 1.9: To find sine cosine and tangent functions for 75 degree

```

2 //example 1.10
3 //To find sine , cosine and tangent functions for 75
  degree
4
5 //triangle_ADB , angle_BAD = 30
6 AB=sqrt(3);BD=1;
7 AD=sqrt(AB^2+BD^2); //pythagoras theorem
8
9 //angle_DAB + angle_CAB = 75
10 //triangle_ABC , angle_BAC = 45
11 //pythagoras theorem and 45 degrees
12 AC=AB/sqrt(2);BC=AC;
13
14 angle_BAC = 45 ; angle_DAB = 30 ;
15 angle_DAE = angle_BAC + angle_DAB ;//required angle
16 angle_ADE = 90 - angle_DAE ;//complement of DAE
17 angle_ADB = 90 - angle_DAB ;//complement of DAB
18
19 //Draw BF perpendicular to DE
20 angle_BDF = angle_ADB - angle_ADE;
21 angle_DBF = 90 - angle_BDF; //complement of BDF
22 //By pythagoras theorem and 45 degree
23 DF=sqrt(BD/2);FB=DF;
24
25 EC=FB;//parallel sides of rectangle
26 FE= BC; //parallel sides of rectangle
27 DE=DF+FE;//from the figure
28 AE=AC-EC;//from the figure
29
30 sin_DAE = DE/AD;
31 cos_DAE = AE/AD;
32 tan_DAE = DE/AE;
33 csc_DAE = AD/DE;
34 sec_DAE = AD/AE;
35 cot_DAE = AE/DE;
36
37 printf( ' sin (%d)=%f\n' , angle_DAE , sin_DAE );
38 printf( ' cos (%d)=%f\n' , angle_DAE , cos_DAE );

```

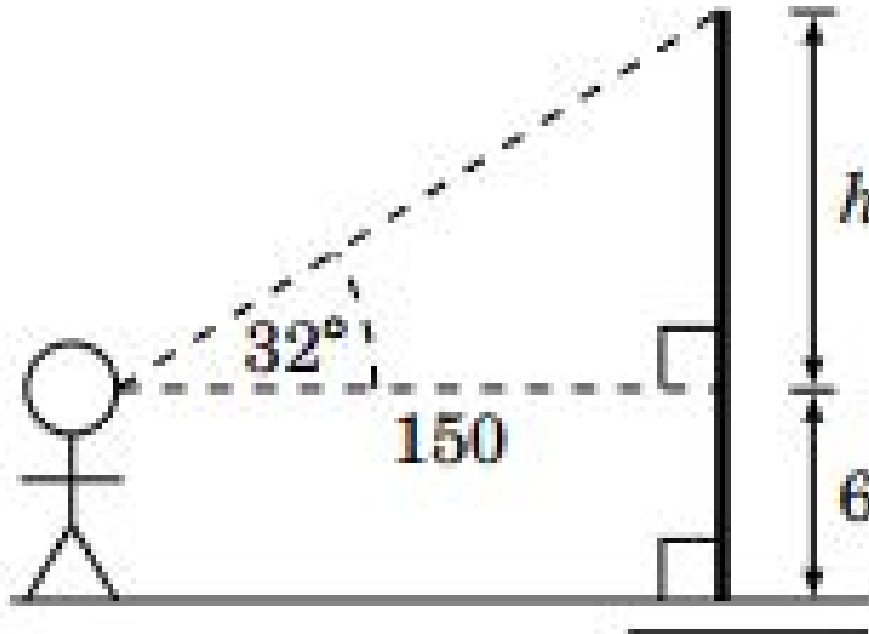


Figure 1.10: To find the height of the flagpole

```

39 printf('tan(%d)=%f\n', angle_DAE, tan_DAE);
40 printf('csc(%d)=%f\n', angle_DAE, csc_DAE);
41 printf('sec(%d)=%f\n', angle_DAE, sec_DAE);
42 printf('cot(%d)=%f\n', angle_DAE, cot_DAE);

```

Scilab code Exa 1.11 To find the height of the flagpole

```

1  clc, clear
2  //example 1.11
3  //To find the height of the flagpole
4
5  //consider the attached figure
6  d=150 //distance of person from flagpole in feet

```

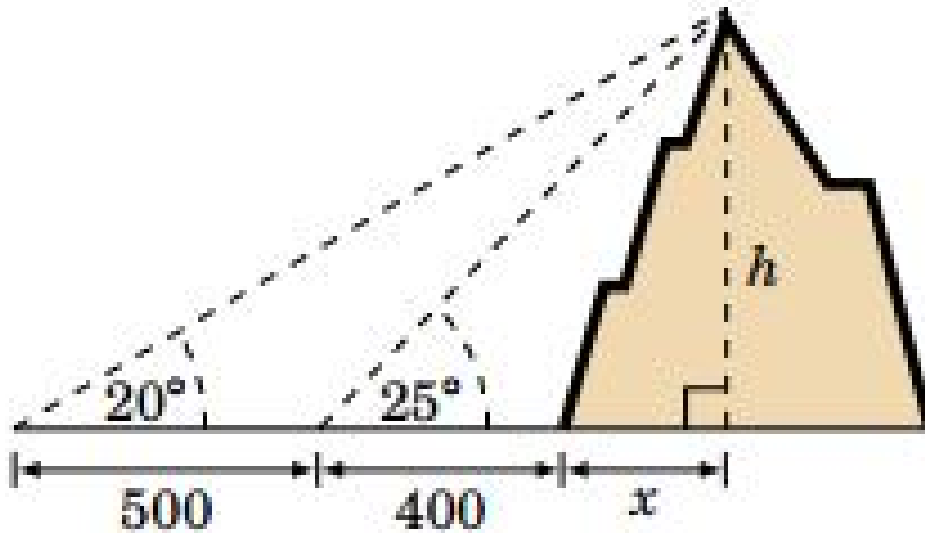


Figure 1.11: To find the height of mountain

```

7 angle_ele = 32 //angle of elevation in degree
8 height_eyes =6 //height of man's eyes
9 h= d*tand(angle_ele)
10 height_flagpole = height_eyes + h
11 printf('Required height of flagpole = %.0f ft ',
        height_flagpole)

```

Scilab code Exa 1.12 To find the height of mountain

```

1 clc,clear
2 //Example 1.12
3 //To find the height of mountain
4
5 //from the figure

```

```

6 //h is height of mountain in degree
7 //x is distance from base of mountain to the point
  under top of mountain
8
9 d1=400 //initial ditance from base of mountain in
  feet
10 d2=500 //final ditance from base of mountain in feet
11 theta1=25 //initial angle of elevation in degrees
12 theta2=20 //final angle of elevation in degrees
13
14 //from the figure
15 //h= (x+d1) * tand(theta1)
16 //h= (x+d2) * tand(theta2)
17 //eliminating h and solving for x
18 x=((d1+d2)*tand(theta2) - d1*tand(theta1))/(tand(
  theta1)-tand(theta2))
19 //substituting x in expression for h
20 h= (x+d1) *tand(theta1)
21 printf('Height of mountain = %.0f feet ',h)

```

Scilab code Exa 1.13 To find the horizontal distance from blimp to house

```

1 clc, clear
2 //Example 1.13
3 //To find the horizontal distance from blimp to
  house
4
5 //consider the figure attached
6 angle_dep = 24 //angle of depression in degrees
7 theta = angle_dep //angle of elevation
8 height_blimp = 4280 //height of blimp from ground in
  feet
9 x = height_blimp / tand(theta) //required distance

```

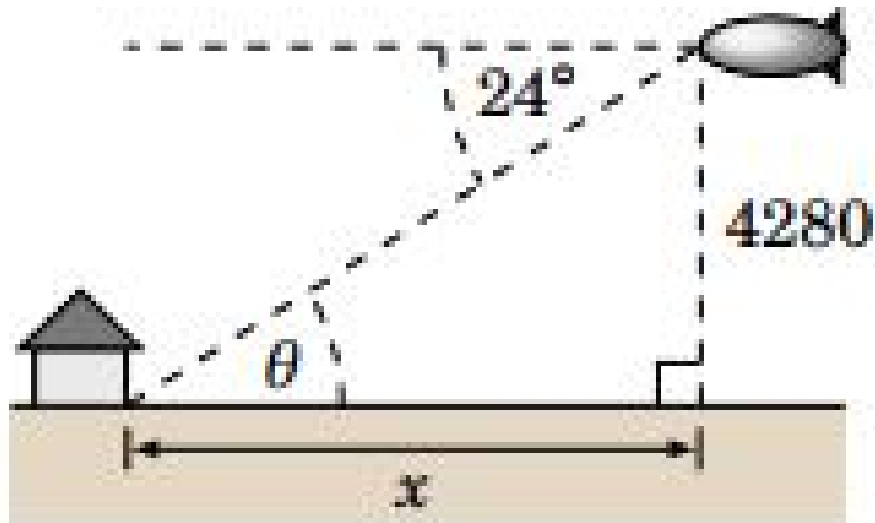


Figure 1.12: To find the horizontal distance from blimp to house

```

in feet
10
11 printf('The house is %.0f ft far from blimp along
the ground',x)

```

Scilab code Exa 1.14 To estimate radius of earth when angle of depression is known

```

1 clc,clear
2 //Example 1.14
3 //To estimate radius of earth when angle of
depression is known
4
5 angle_dep = 2.23 //angle of depression in degrees

```

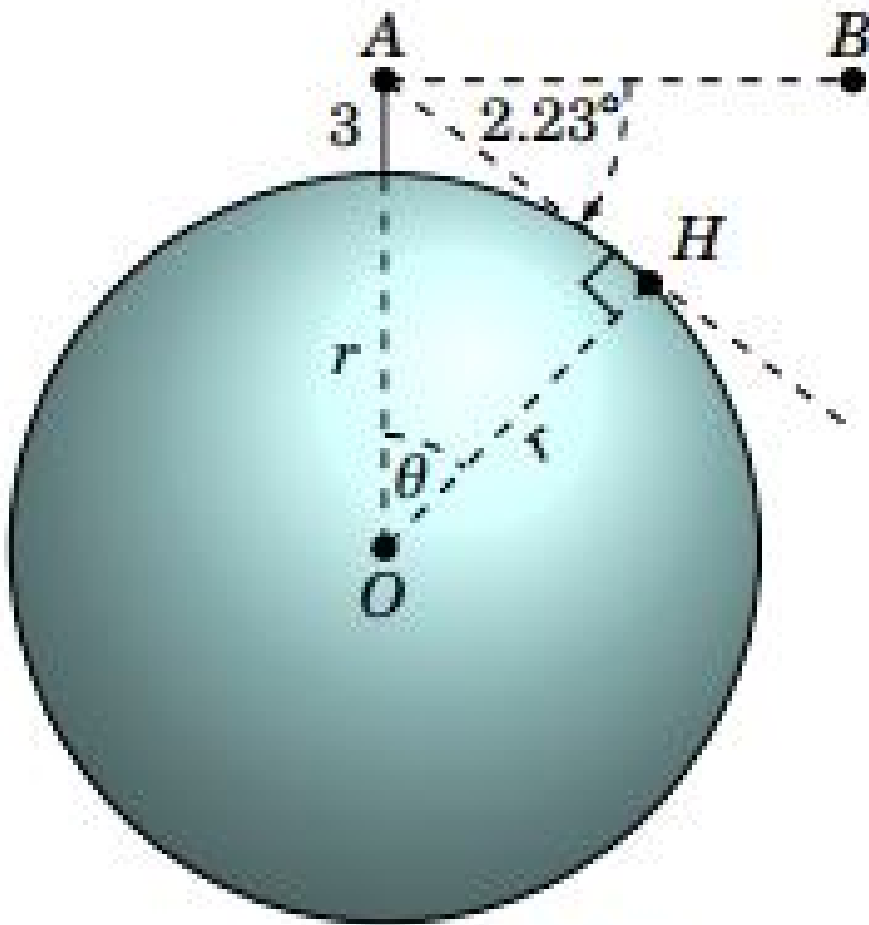


Figure 1.3.1

Figure 1.13: To estimate radius of earth when angle of depression is known


```

6 //In the figure ,
7 //r is the radius of earth
8 //A represent the top of the mountain
9 //H be the ocean horizon in the line of sight from A
10 //O be the center of the earth
11 //B is a point on the horizontal line of sight from
    A
12
13 angle_OAH = 90 - angle_dep ;
14 theta = 180 - 90 - angle_OAH ;
15 height=3 //height of mountain
16 //r is radius of earth to be determined
17
18 //distance from top of mountain from centre = r +
    height
19 // cosd(theta)= r/r+height... solving further
20 r = height*cosd(theta)/(1-cosd(theta)) ;
21 printf('Radius of earth as calculated = %.1f miles\n
    ',r)

```

Scilab code Exa 1.15 To find the distance from centre of earth to sun

```

1 clc ,clear
2 //Example 1.15
3 // To find the distance from centre of earth to sun
4
5 alpha = 0.00244; // equitorial paralalx in degree
6 OA = 3956.6; //radius of earth
7 angle_OAB = 90;
8
9 OB = OA / sind(alpha) ;
10 printf('Distance is obtained as %.0f miles = %.0f
    million miles ',OB,OB/10^6)

```

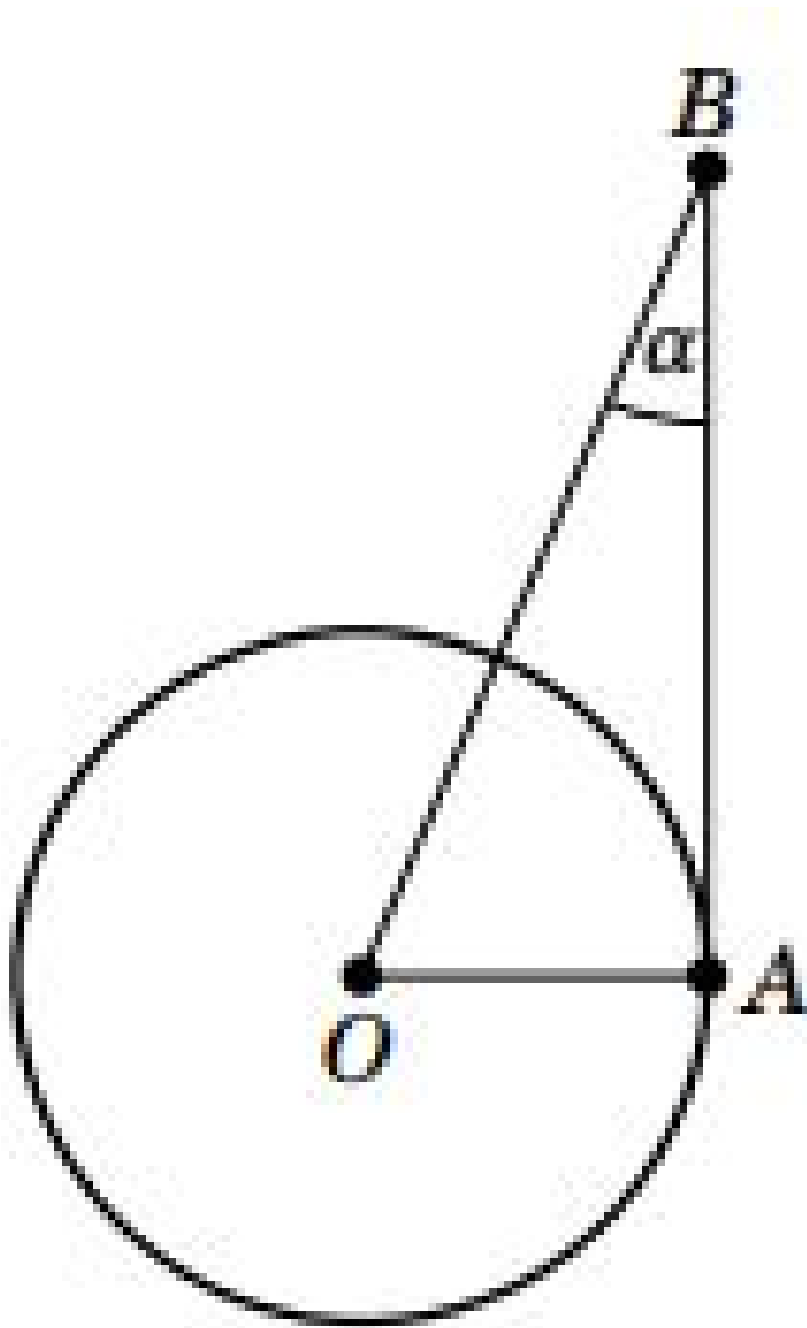


Figure 1.14: To find the distance from centre of earth to sun

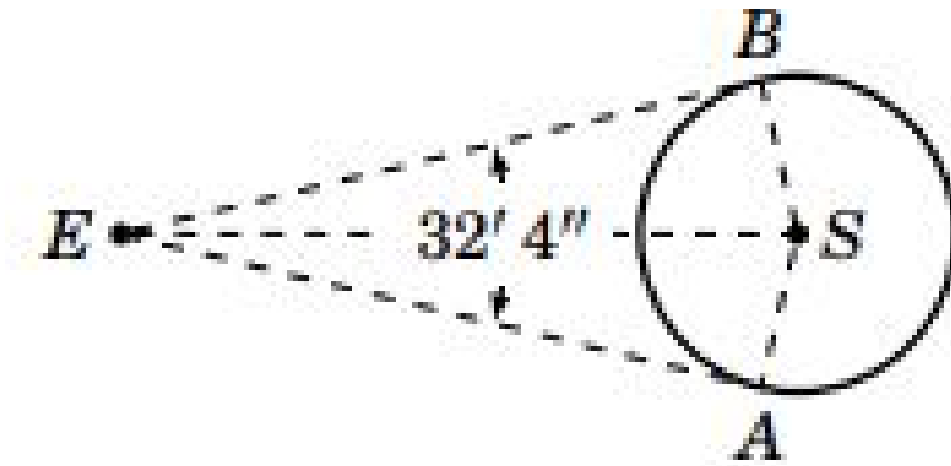


Figure 1.15: To determine the radius of sun

Scilab code Exa 1.16 To determine the radius of sun

```

1  clc,clear
2  //Example 1.16
3  // To determine the radius of sun
4
5  angle_AEB =0 +(32/60)+ (4/60)/60//converting to
   degrees
6
7  //Triangle BES and AES are similar
8  //BS=AS as they are radius
9  //ES is common to both triangles
10 //angle_EBS=angle_ABS =90 as tangents are
    perpendicular to radius
11 // angle_AES = angle_BES
12 angle_AES= angle_AEB /2;

```

```

13 angle_BES= angle_AEB /2;
14
15 //to find ditance from sun to centre of earth
16 //obtained from previous example
17 alpha = 0.00244; // equitorial paralalx in degree
18 OA = 3956.6 ;//radius of earth
19 angle_OAB = 90 ;//radius perpendicular to tangent
20 OB = OA / sind(alpha) ;
21
22 //ES is from earth surface to sun centre
23 //centre of earth to sun is OB
24 //we initially treated sun as point
25 //that ditance is distance between their centres
26 radius_earth=3956.6 ;//in miles
27 ES = OB - radius_earth ;//in miles
28 AS=ES * sind(angle_AES) ;//in miles
29 printf('Required radius of sun = %.0f miles \n',AS)
30 printf('Answer might vary due to approximations in
    book and scilab precision ')

```

Scilab code Exa 1.17 To determine the diameter of larger roller

```

1  clc , clear
2  //Example 1.17
3  //To find the diameter of larger roller
4
5  //since radius perpendicular to tangent
6  angle_ODA=90;
7  angle_PEC=90
8  angle_OAD=37 ;//by symmetry
9  ED=1.38 ;//given
10 //since DOA is right triangle , DOA and OAD are
    complementary angles

```

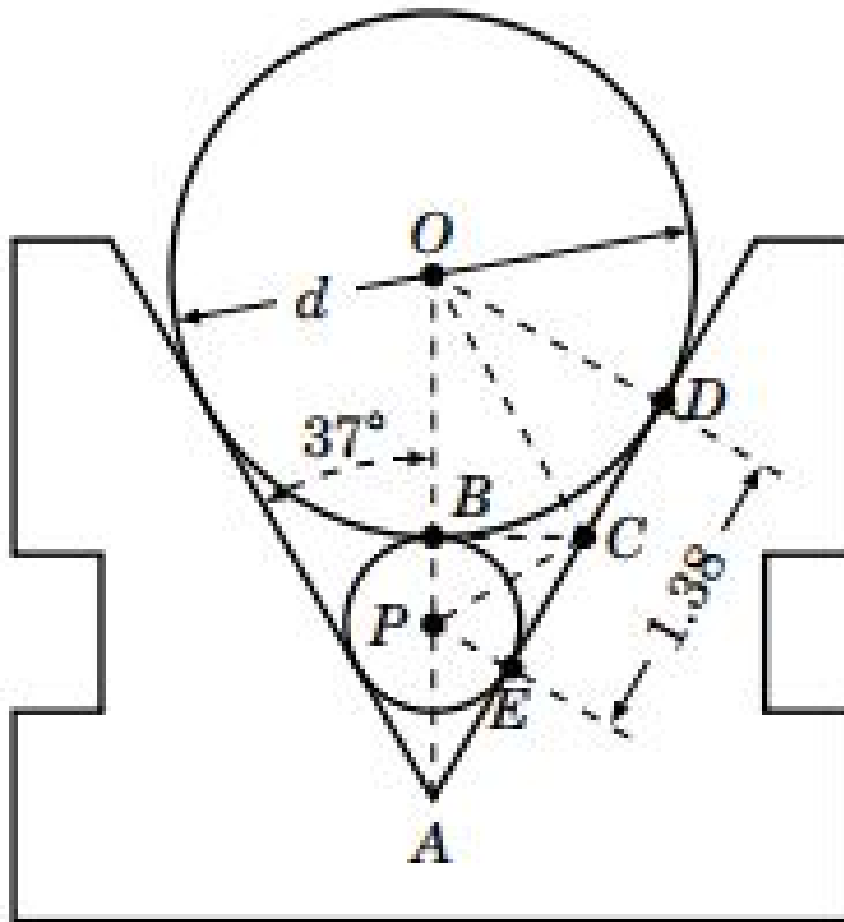


Figure 1.16: To determine the diameter of larger roller

```

11 angle_DOA=90 - angle_OAD ;
12
13 //since radius perpendicular to tangent
14 angle_OBC=90;
15 angle_PBC=90;
16
17 //since ODA and ODC are right triangle ,
18 //OD = OB as radius and BC=DC by pythagoras
19 //OBC and ODC are now congruent
20 //angle_BOC = angle_DOC
21 //angle_BOC + angle_DOC =(90-angle_OAD)
22 angle_BOC= (90-angle_OAD)/2;
23 angle_DOC= (90-angle_OAD)/2;
24
25 //BP=EP as radius
26 //since radius perpendicular to tangent
27 angle_PBC=90;
28 angle_PEC=90;
29 //Thus ,BPC and EPC are congruent triangles
30 //Therefore ,BC=DC and BC+DC = ED
31 BC = ED /2;
32 DC = ED /2;
33 OB = BC / tand(angle_BOC); //radius of large roller
34 diameter= 2* OB ;
35 printf('Diameter of larger roller = %.3f units ',
        diameter)

```

Scilab code Exa 1.19 To solve the right triangle with given information

```

1  clc , clear
2  //Example 1.19
3  //To solve the right triangle with given information
4

```

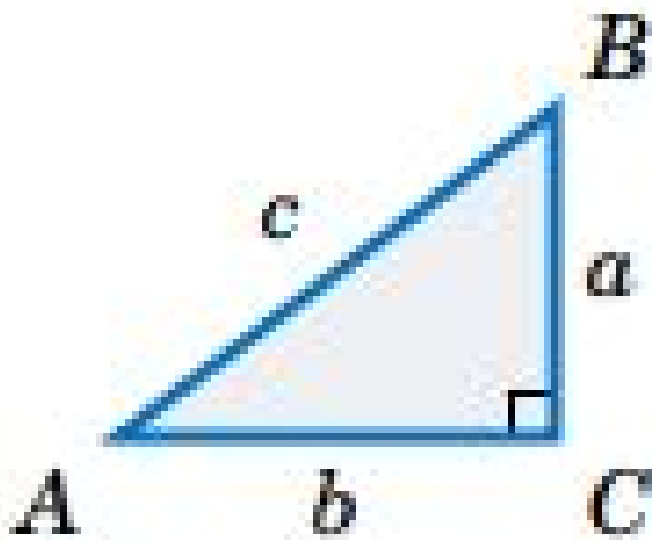


Figure 1.3.3

Figure 1.17: To solve the right triangle with given information

```

5 //part(a)
6 c=10 ;//side opposite to vertex C
7 A=22 ;//Angle at vertex A
8 a=c*sind(A);
9 b=c*cosd(A) ;
10 B=90 - A ;//since C is 90, A and B are complimentary
11 printf('(a)a= %.2f units ; b= %.2f units; B = %.0f
    degree\n',a,b,B)
12
13 //part(b)
14 b=8 ;//side opposite to vertex B
15 A=40 ;//Angle at vertex A
16 a=b*tand(A);
17 c=b/cosd(A) ;
18 B=90 - A ;//since C is 90, A and B are complimentary
19 printf('(b)a= %.2f units ; c= %.2f units; B = %.0f
    degree\n',a,c,B)
20
21 //part(c)
22 a=3 ;//side opposite to vertex A
23 b=4 ;//side opposite to vertex B
24 c=sqrt(a^2+b^2) ;//by pythagoras theorem
25 A = atand(a/b) ;//angle at vertex A
26 B=90 - A ;//since C is 90, A and B are complimentary
27 printf('(c)c=%.0f units ; A= %f degree; B = %f
    degree',c,A,B)

```

Scilab code Exa 1.20 To find values of all trigonometric values of given angle of 120

```

1 clc,clear
2 //Example 1.20
3 //To find values of all trigonometric values of

```

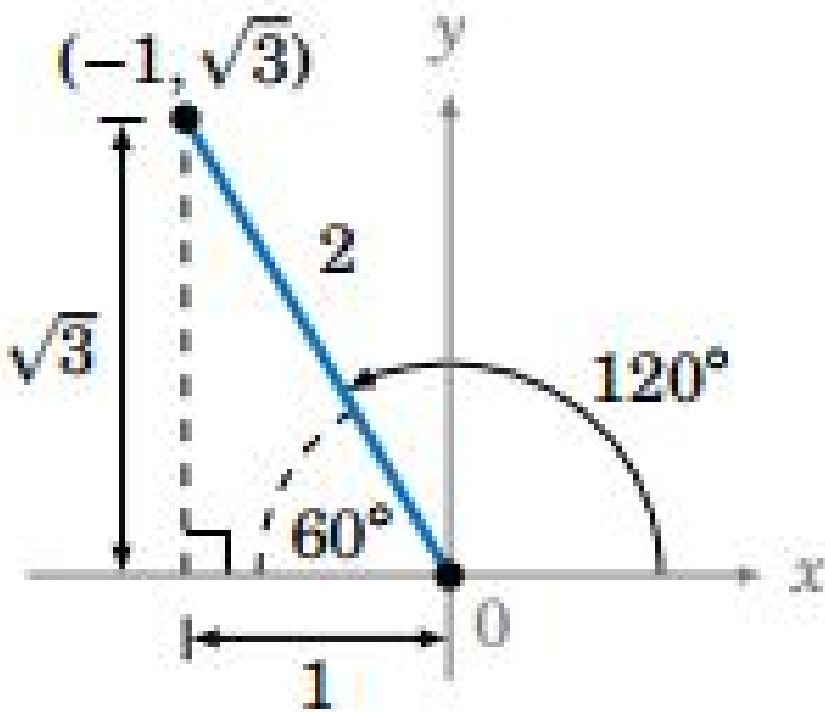



Figure 1.18: To find values of all trigonometric values of given angle of 120

```

        given angle of 120
4
5 theta=120; //given angle in degree
6 //Consider a point (-1,sqrt(3)) in 2nd quadrant
7 //This point can be used on terminal side of 120
8 //Thus for a basic right angled triangle formed in
    second quadrant
9 adjacent = 1;
10 opposite = sqrt(3);
11 //by pythagoras theorem
12 hypotenuse = sqrt(adjacent^2 + opposite^2);
13
14 //since its third quadrant
15 x=-adjacent;
16 y= opposite;
17 r=hypotenuse;
18
19 sin_120 =y/r ;
20 cos_120 =x/r ;
21 tan_120 =y/x ;
22 csc_120 =r/y ;
23 sec_120 =r/x ;
24 cot_120 =x/y ;
25
26 printf('\nsin(%d)= %f ; cos(%d)= %f ; tan(%d)= %f ;'
    ,theta,sin_120,theta,cos_120,theta,tan_120)
27 printf('\ncsc(%d)= %f ; sec(%d)= %f ; cot(%d)= %f ;'
    ,theta,csc_120,theta,sec_120,theta,cot_120)

```

Scilab code Exa 1.21 To find values of all trigonometric values of given angle of 225

```
1 clc,clear
```

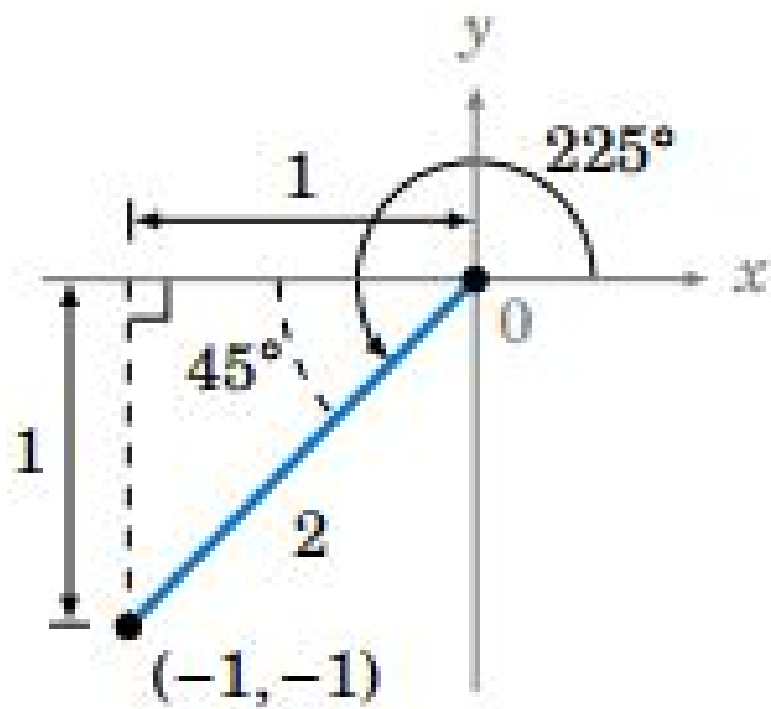


Figure 1.19: To find values of all trigonometric values of given angle of 225

```

2 //Example 1.21
3 //To find values of all trigonometric values of
   given angle of 225
4
5 theta=225 ;//given angle in degree
6 //Consider a point (-1,-1) in 3rd quadrant
7 //This point can be used on terminal side of 225
8 //Thus for a basic right angled triangle formed in 3
   rd quadrant
9 adjacent = 1 ;
10 opposite = 1 ;
11 //by pythagoras theorem
12 hypotenuse = sqrt(adjacent^2 + opposite^2) ;
13
14 //since its third quadrant
15 x=-adjacent ;
16 y=-opposite ;
17 r=hypotenuse ;
18
19 sin_225 =y/r ;
20 cos_225 =x/r ;
21 tan_225 =y/x ;
22 csc_225 =r/y ;
23 sec_225 =r/x ;
24 cot_225 =x/y ;
25
26 printf('\nsin(%d)= %f ; cos(%d)= %f ; tan(%d)= %f ;'
   ,theta,sin_225,theta,cos_225,theta,tan_225)
27 printf('\ncsc(%d)= %f ; sec(%d)= %f ; cot(%d)= %f ;'
   ,theta,csc_225,theta,sec_225,theta,cot_225)

```

Scilab code Exa 1.22 To find values of all trigonometric values of given angle of 330

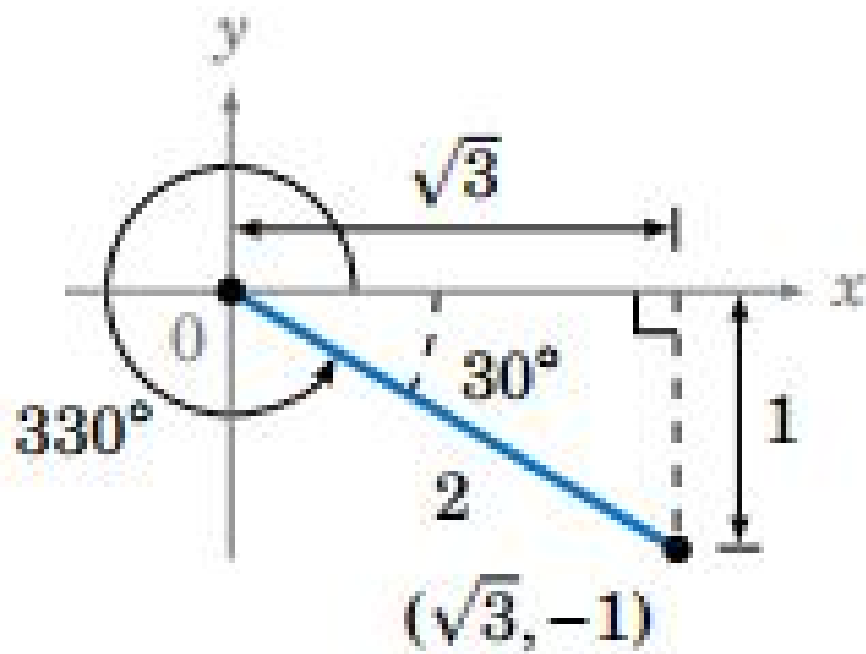


Figure 1.20: To find values of all trigonometric values of given angle of 330

```

1  clc,clear
2  //Example 1.22
3  //To find values of all trigonometric values of
   given angle of 330
4
5  theta=330 ; //given angle in degree
6  //Consider a point (sqrt(3),-1) in 4th quadrant
7  //This point can be used on terminal side of 330
8  //Thus for a basic right angled triangle formed in 4
   th quadrant
9  adjacent = sqrt(3);
10 opposite = 1 ;
11 hypotenuse = sqrt(adjacent^2 + opposite^2);
12 //by pythagoras theorem
13
14 //since its 4th quadrant
15 x=adjacent ;
16 y=-opposite ;
17 r=hypotenuse ;
18
19 sin_330 =y/r ;
20 cos_330 =x/r ;
21 tan_330 =y/x ;
22 csc_330 =r/y ;
23 sec_330 =r/x ;
24 cot_330 =x/y ;
25
26 printf(' \nsin(%d)= %f ; cos(%d)= %f ; tan(%d)= %f ;'
   ,theta,sin_330,theta,cos_330,theta,tan_330)
27 printf(' \ncsc(%d)= %f ; sec(%d)= %f ; cot(%d)= %f ;'
   ,theta,csc_330,theta,sec_330,theta,cot_330)

```

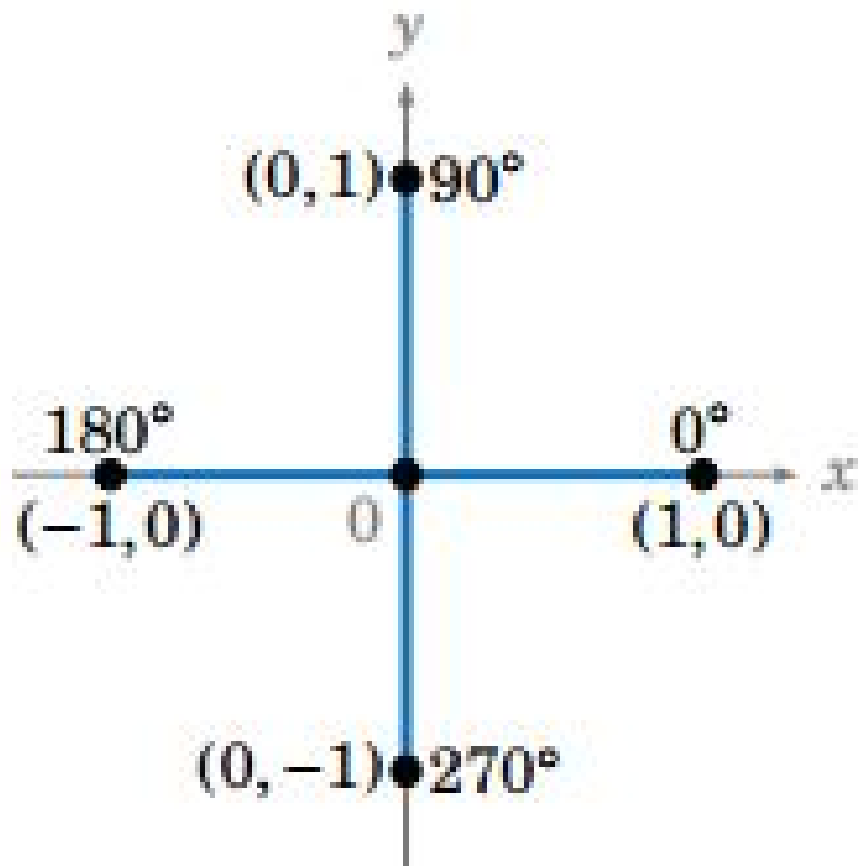


Figure 1.21: To find trigonometric ratios of 0 90 180 and 270 degrees

Scilab code Exa 1.23 To find trigonometric ratios of 0 90 180 and 270 degrees

```
1  clc,clear
2  //Example 1.23
3  //To find trigonometric functions of various angles
4  //Note: Undefined ratios are commented to avoid
      divide by zero error
5
6  //zero degrees
7  //consider a point (1,0)
8  //Line segment joining (0,0) and (1,0) can be
      treated as triangle
9
10 x=1//base
11 y=0//height
12 r=1 //hypotenuse
13 sin_0 = y/r;
14 cos_0 = x/r;
15 tan_0 = y/x;
16 //csc_0 =r/y;
17 sec_0 = r/x;
18 //cot_0=x/y;
19 printf(' \nZERO DEGREES:\n ')
20 printf(' sin(0)= %f;\n ', sin_0)
21 printf(' cos(0)= %f;\n ', cos_0)
22 printf(' tan(0)= %f;\n ', tan_0)
23 printf(' csc(0)= undefined = (1/0);\n ')
24 printf(' sec(0)= %f;\n ', sec_0)
25 printf(' cot(0)= undefined = (1/0);\n ')
26
27 //90 degrees
28 //consider a point (0,1)
29 //Line segment joining (0,0) and (0,1) can be
      treated as triangle
30
31 x=0//base
32 y=1//height
```



```

33 r=1 //hypotenuse
34 sin_90 = y/r;
35 cos_90 = x/r;
36 //tan_90 = y/x;
37 csc_90 =r/y;
38 //sec_90 = r/x;
39 cot_90=x/y;
40 printf( '\n90 DEGREES:\n' )
41 printf( 'sin(90)= %f;\n',sin_90)
42 printf( 'cos(90)= %f;\n',cos_90)
43 printf( 'tan(90)= undefined = (1/0);\n' )
44 printf( 'csc(90)= %f;\n',csc_90)
45 printf( 'sec(90)= undefined = (1/0);\n' )
46 printf( 'cot(90)= %f;\n',cot_90)
47
48 //180 degrees
49 //consider a point (-1,0)
50 //Line segment joining (0,0) and (-1,0) can be
    treated as triangle
51
52 x=-1//base
53 y=0//height
54 r=1 //hypotenuse
55 sin_180 = y/r;
56 cos_180 = x/r;
57 tan_180 = y/x;
58 //csc_180 =r/y;
59 sec_180 = r/x;
60 //cot_180=x/y;
61 printf( '\n180 DEGREES:\n' )
62 printf( 'sin(180)= %f;\n',sin_180)
63 printf( 'cos(180)= %f;\n',cos_180)
64 printf( 'tan(180)= %f;\n',tan_180)
65 printf( 'csc(180)= undefined = (1/0);\n' )
66 printf( 'sec(180)= %f;\n',sec_180)
67 printf( 'cot(180)= undefined = (-1/0);\n' )
68
69

```

```

70 //270 degrees
71 //consider a point (0,-1)
72 //Line segment joining (0,0) and (0,-1) can be
    treated as triangle
73
74 x=0//base
75 y=-1//height
76 r=1 //hypotenuse
77 sin_270 = y/r;
78 cos_270 = x/r
79 //tan_90 = y/x;
80 csc_270 =r/y;
81 //sec_90 = r/x;
82 cot_270=x/y;
83 printf( '\n270 DEGREES:\n' )
84 printf( 'sin(270)= %f;\n',sin_270)
85 printf( 'cos(270)= %f;\n',cos_270)
86 printf( 'tan(270)= undefined = (-1/0);\n' )
87 printf( 'csc(270)= %f;\n',csc_270)
88 printf( 'sec(270)= undefined = (1/0);\n' )
89 printf( 'cot(270)= %f;\n',cot_270)

```

Scilab code Exa 1.24 To determine reference angle and angle between 0 to 360 with same terminal side as given angle

```

1  clc,clear
2  //Example 1.24
3  //To determine reference angle and angle ( 0 to 360
    )with same terminal side as given angle
4
5  theta = 928 ;//given angle in degrees
6
7  //The while loop works for ALL VALUES OF theta

```

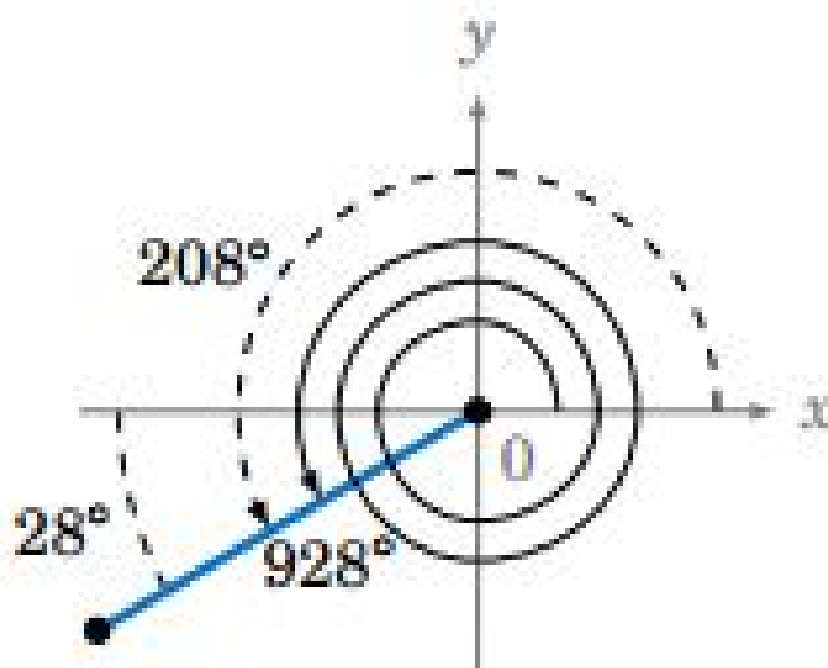


Figure 1.22: To determine reference angle and angle between 0 to 360 with same terminal side as given angle

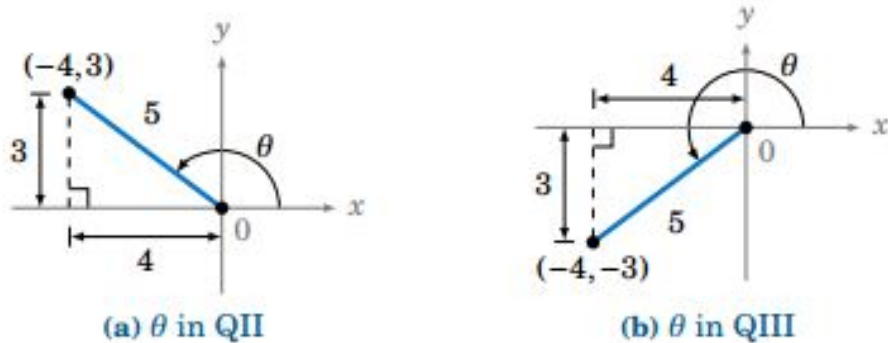


Figure 1.23: To find sin theta and tan theta when cos theta is given

```

8 //It keeps subtracting 360 till a value in (0 to
  360) is obtained
9 result = theta ;
10 while 1==1,
11     if result<360 then
12         printf('(a)Required angel between 0 and 360
           is %.0f degree',result);
13         break
14     end
15     result = result - 360 ;
16 end
17
18 //928 and 208 has same terminal side in 3rd quadrant
19 //so their reference angle is same
20 ref_angle_928 = result - 180 ; //required reference
  angle
21 printf('\n(b)Reference angel for %.0f is %.0f degree
  ',theta,ref_angle_928)

```

Scilab code Exa 1.25 To find sin theta and tan theta when cos theta is given

```
1 clc,clear
2 //Example 1.25
3 //To find sin_theta and tan_theta when cos_theta is
   given
4
5 cos_theta = -4/5;
6 adjacent =4 ; hypotenuse =5 ;
7 opposite = sqrt(hypotenuse ^2 - adjacent ^2) //by
   pythagoras theorem
8
9 //minus sign of cos_theta implies 2nd or 3rd
   quadrant
10 //Possibility 1 : 2nd quadrant
11 x= -adjacent ;
12 y= opposite ;
13 r= hypotenuse ;
14 sin_theta = y/r ;
15 tan_theta = y/x ;
16 printf('POSSIBILITY 1:Theta in 2nd quadrant\n')
17 printf('sin(theta)= %.2f ; tan(theta) = %.2f; \n\n',
   ,sin_theta,tan_theta)
18
19 //Possibility 2 : 3rd quadrant
20 x=-adjacent ;
21 y=-opposite ;
22 r=hypotenuse ;
23 sin_theta = y/r ;
24 tan_theta = y/x ;
25 printf('POSSIBILITY 2:Theta in 3rd quadrant\n')
26 printf('sin(theta)= %.2f ; tan(theta) = %.2f; ',
   sin_theta,tan_theta)
```

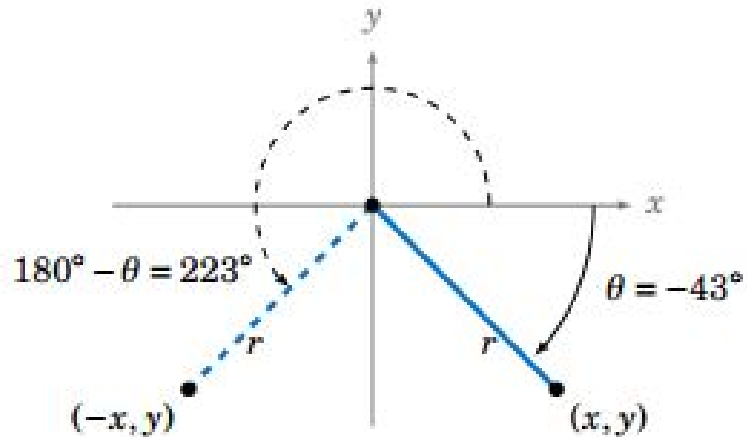


Figure 1.24: To find all the angles with a given sine function value

Scilab code Exa 1.27 To find all the angles with a given sine function value

```

1  clc, clear
2  //Example 1.27
3  //To find all the angles with a given sine function
   value
4
5  sin_theta = -0.682;
6  theta=asind(sin_theta);
7  //This results -43 degree which isnt in 0 to 360
   range
8  //And theta exists in 4th quadrant
9  //Angles in 1st and 2nd quadrant have +ve sine
   values
10
11 theta1 = 180 - theta ;//reflection of theta in 3rd
   quadrant

```

```
12 theta2 = 360 + theta ;//both theta n theta 2 have
    same trigonometric values
13 printf('Required angles are %.0f and %.0f degrees ',
    theta1,theta2)
```

Chapter 2

General Triangles

Scilab code Exa 2.1 To solve the triangle when one side and 2 angles are given

```
1 //Example 2.1
2 //To solve the triangle when one side and 2 angles
  are given
3 clc, clear
4
5 a=10 //side opposite to vertex A
6 A=41 //angle at vertex A
7 C=75 //angle at vertex C
8
9 B=180- (A+C)
10 b=a*sind(B)/sind(A) //law of sines
11 c=a*sind(C)/sind(A) //law of sines
12 printf('Angle B is %.0f degrees\n length of side b
  is %.1f units\n length of side c is %.1f units',B
  ,b,c)
```

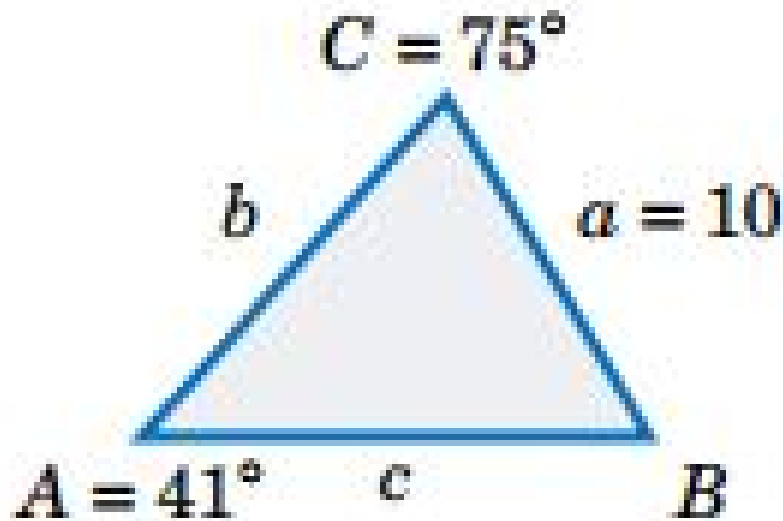


Figure 2.1: To solve the triangle when one side and 2 angles are given



Figure 2.2: To solve the triangle when 2 sides and one opposite angle is given

Scilab code Exa 2.2 To solve the triangle when 2 sides and one opposite angle is given

```
1 //Example 2.2
2 //To solve the triangle when 2 sides and one
   opposite angle is given
3 clc,clear
4
5 a=18 //side oposite to vertex A
6 A=25 //angle at vertex A
7 b=30 //side opposite to vertex B
8
9 sin_B=(b/a)*sind(A) //law of sines
10
11 //case 1
12 B=asind(sin_B) //law of sines
13 C=180-(A+B)
14 c=a*sind(C)/sind(A) //law of sines
15 printf('1st possible solution set\nAngle at B =%.1f
   degree\nAngle at C=%.1f degree\nlength of side c=
   %.0f units\n',B,C,c)
16
17 //case 2
18 B=180 - asind(sin_B) //law of sines
19 C=180-(A+B)
20 c=a*sind(C)/sind(A) //law of sines
21 printf(' \n\n2nd possible solution set\nAngle at B =%.
   .1f degree\nAngle at C=%.1f degree\nlength of
   side c=%.1f units\n',B,C,c)
```

Scilab code Exa 2.3 To solve the triangle when 2 sides and opposite angle is given

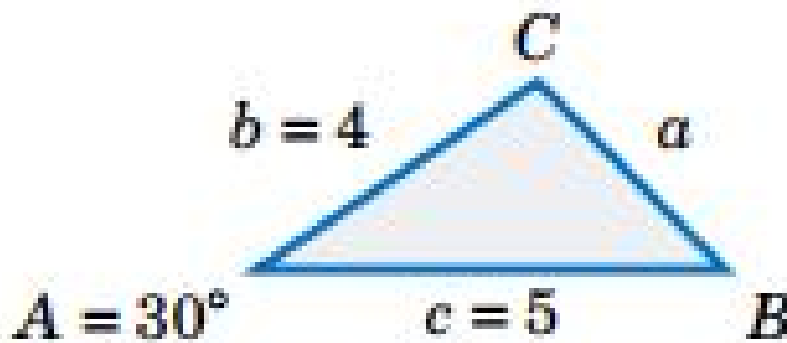


Figure 2.3: To solve the triangle when 2 sides and angle between them is given

```

1 //Example 2.3
2 //To solve the triangle when 2 sides and opposite
  angle is given
3 clc,clear
4
5 a=5 //side oposite to vertex A
6 A=30 //angle at vertex A
7 b=12 //side opposite to vertex B
8
9 sin_B=(b/a)*sind(A) //law of sines
10 printf("sin(B)=%f. But magnitude of sin(B) should
  be less than 1\nHence,there is no solution",sin_B
  )

```

Scilab code Exa 2.4 To solve the triangle when 2 sides and angle between them is given

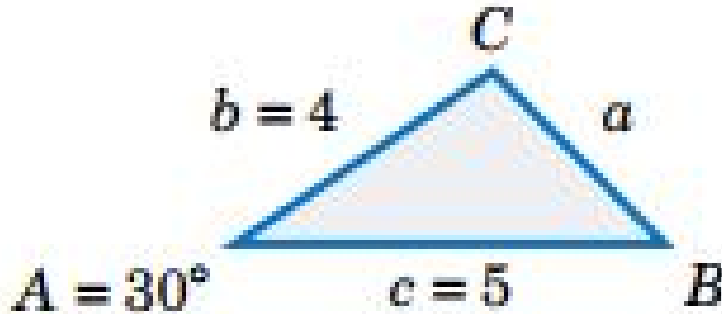


Figure 2.4: To solve the triangle when 2 sides and angle between them is given

```

1 //Example 2.4
2 //To solve the triangle when 2 sides and angle
  between them is given
3 clc,clear
4
5 c=5 //side oposite to vertex C
6 A=30 //angle at vertex A
7 b=4 //side opposite to vertex B
8
9 printf('By law of sines:\n')
10 printf('a/sin(30) = 4/sin(B) = 5 / sin(C)\n')
11 printf(' \nEach of the equations has 2 unknowns. ')
12 printf(' \nFor eg: To obtain a , we can use 4/sin(B)
  =5/sin(C). Next we obtain B interms of C and put
  back.\n')
13 printf('Now we have a in terms of C which is unknown
  \n')
14 printf('Hence it is IMPOSSIBLE to solve this by law
  of sines ')

```

Scilab code Exa 2.5 To solve the triangle when 2 sides and angle between them is given

```
1 //Example 2.5
2 //To solve the triangle when 2 sides and angle
   between them is given
3 clc,clear
4
5 c=5 //side oposite to vertex C
6 A=30 //angle at vertex A
7 b=4 //side opposite to vertex B
8
9 a = sqrt( b^2 + c^2 -2*b*c*cosd(A) ) //from law of
   cosines
10 printf('Length of a= %.2f units\n',a)
11 cos_B = (c^2+a^2-b^2)/(2*c*a) //from law of cosines
12 B=acosd(cos_B)
13 printf('Angle B=%.1f degrees\n',B)
14 C=180-(A+B)
15 printf('Angle C=%.1f degrees\n',C)
```

Scilab code Exa 2.6 To solve the triangle when 3 sides are given

```
1 //Example 2.6
2 //To solve the triangle when 3 sides are given
3 clc,clear
4
5 c=4 //side oposite to vertex C
6 a=2 //side opposite to vertex A
7 b=3 //side opposite to vertex B
```

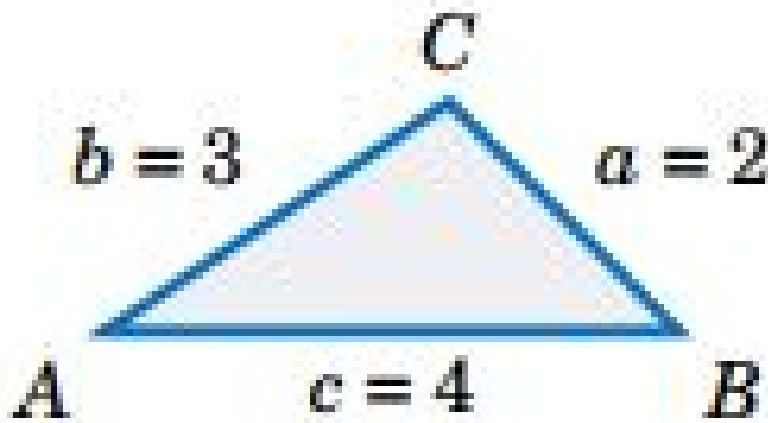


Figure 2.5: To solve the triangle when 3 sides are given

```

8
9 cos_B = (c^2+a^2-b^2)/(2*c*a) //from law of cosines
10 B=acosd(cos_B)
11 printf('Angle B=%0.1f degrees\n',B)
12 cos_C = (b^2+a^2-c^2)/(2*b*a) //from law of cosines
13 C=acosd(cos_C)
14 printf('Angle C=%0.1f degrees\n',C)
15
16 A=180-(C+B)
17 printf('Angle A=%0f degrees ',A)

```

Scilab code Exa 2.7 To determine solution of a triangle when 3 sides are given

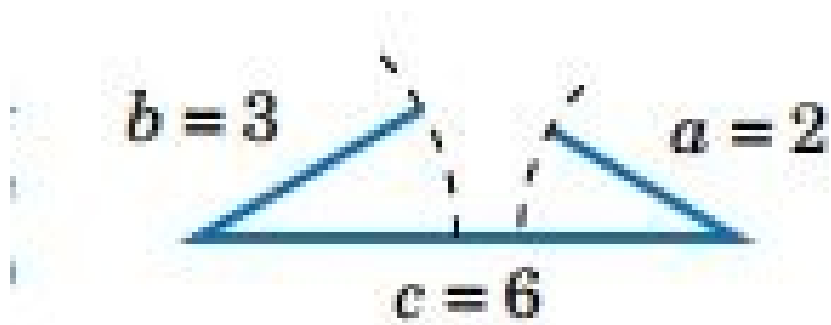
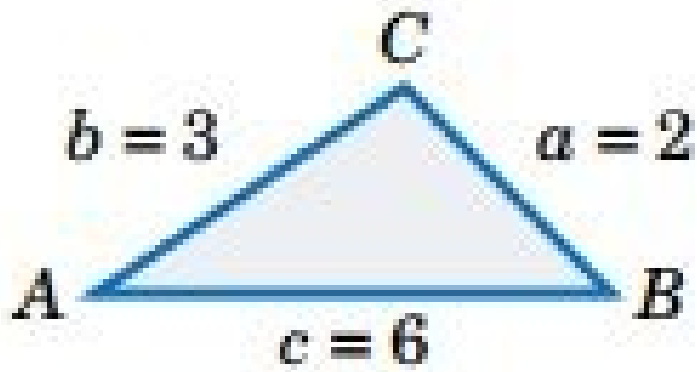


Figure 2.6: To determine solution of a triangle when 3 sides are given

```

1 //Example 2.7
2 //To determine solution of a triangle when 3 sides
   are given
3 clc,clear
4
5 c=6 //side oposite to vertex C
6 a=2 //side opposite to vertex A
7 b=3 //side opposite to vertex B
8
9 cos_A = (b^2+c^2-a^2)/(2*c*b) //from law of cosines
10 printf('cos(A)=%.3f as calculated\n',cos_A)
11 printf('But magnitude of cos(A) should always be
   less than 1. Hence NO SOLUTION exists\n\n')
12
13 printf('Note: We observe that a+b < c. But sum of
   any 2 sides should always exceed third side.')
14 printf('\\nHence this triangle is impossible.')

```

Scilab code Exa 2.8 To solve the triangle when 2 sides and opposite angle is given

```

1 //Example 2.8
2 //To solve the triangle when 2 sides and opposite
   angle is given
3 clc,clear
4
5 a=18 //side oposite to vertex A
6 A=25 //angle at vertex A
7 b=30 //side opposite to vertex B
8
9 //using law of cosines solving for c
10 c_polynomial=[1 -54.38 576]
11 root_c=roots(c_polynomial)
12
13 //case 1

```



```

14 c=root_c(1)
15 cos_B = (c^2+a^2-b^2)/(2*c*a) //from law of cosines
16 B= (180/%pi)*acos (cos_B)
17 C=180-(A+B)
18 printf('1st possible answer set\nAngle B=%0.1f degree
        \nAngle C=%0.1f degree\nlength of c=%0.0f units\n\n
        ',B,C,c)
19
20 //case 2
21 c=root_c(2)
22 cos_B = (c^2+a^2-b^2)/(2*c*a) //from law of cosines
23 B=(180/%pi)*acos(cos_B)
24 C=180-(A+B)
25 printf('2nd possible answer set(which is not solved
        in book)\nAngle B=%0.1f degree\nAngle C=%0.1f
        degree\nlength of c=%0.0f units\n',B,C,c)

```

Scilab code Exa 2.10 To solve the triangle when 2 sides and included angle is given

```

1 //Example 2.10
2 //To solve the triangle when 2 sides and included
  angle is given
3 clc,clear
4
5 a=5 //side oposite to vertex a
6 b=3 //side opposite to vertex b
7 C=96 //angle at vertex C
8
9 ApB=180-C //A + B
10 //using law of tangents
11 AmB =2* atand( tand(ApB/2)*(a-b)/(a+b) ) //A-B
12

```

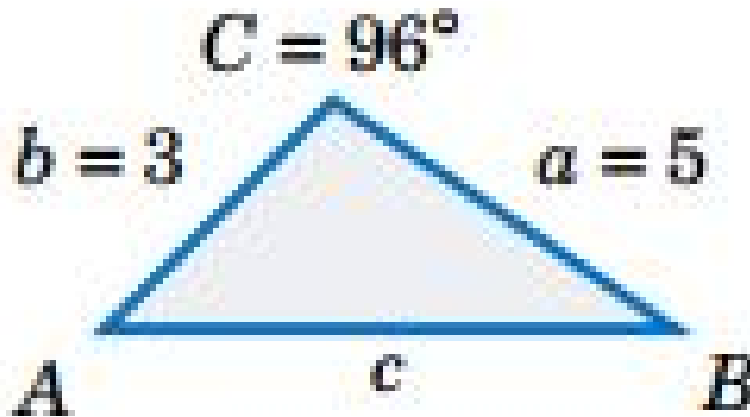


Figure 2.7: To solve the triangle when 2 sides and included angle is given

```

13 //solving for A and B using AmB and ApB
14 A= (AmB + ApB)/2
15 B= ApB - A
16
17 c=a*sind(C)/sind(A) //law of sines
18 printf('Angle A= %.1f degree\nAngle B=%.1f degree\
        nlength of c=%.2f units ',A,B,c)

```

Scilab code Exa 2.11 To check the solution of triangle using Mollweide equation

```

1 //Example 2.11
2 //To check the solution of triangle using Mollweide
  equation
3 clc,clear
4

```

```

5 c=6.09 //side oposite to vertex C
6 a=5 //side opposite to vertex A
7 b=3 //side opposite to vertex B
8
9 A=54.7 //angle at vertex A
10 B=29.3 //angle at vertex B
11 C=96 //angle at vertex C
12
13 LHS = (a-b)/c
14 RHS = sind((A-B)/2)/cosd(C/2)
15 printf(' LHS = (a-b)/c = %.4f\n',LHS)
16 printf(' RHS = sin((A-B)/2)/cos(C/2) = %.4f\n\n',
RHS)
17
18 printf('Small difference in LHS and RHS is due to
rounding off.\ni.e.Mollweides equation is holding
true.\n')
19 printf('THE SOLUTION OF TRIANGLE IS CORRECT')

```

Scilab code Exa 2.12 To determine if a triangle can be formed with given dimension

```

1 //Example 2.12
2 //To determine if a triangle can be formed with
given dimension
3 clc,clear
4
5 c=9 //side oposite to vertex C
6 a=6 //side opposite to vertex A
7 b=7 //side opposite to vertex B
8
9 A=55 //angle at vertex A
10 B=60 //angle at vertex B
11 C=65 //angle at vertex C
12 printf('Sum of angles=180\n')

```

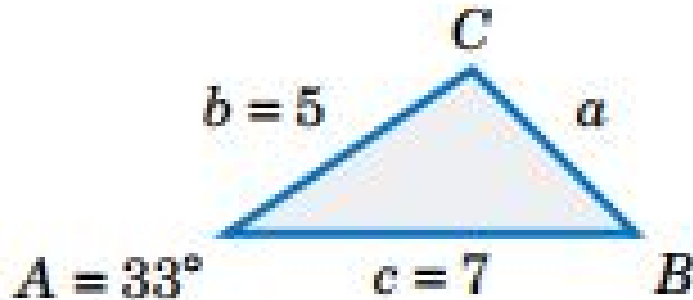


Figure 2.8: To determine area of triangle when 2 sides and an angle is given

```

13 printf('Smallest and largest sides are opposite to
        smallest and largest angle respectively\n\n')
14
15 LHS = (a+b)/c
16 RHS = cosd((A-B)/2)/sind(C/2)
17 printf(' LHS = (a+b)/c = %.2f\n', LHS)
18 printf(' RHS = cos((A-B)/2)/sin(C/2) = %.2f\n\n',
        RHS)
19
20 printf('As we can see, LHS is not equal to RHS.\ni.e
        .Mollweides equation is not holding true.\n')
21 printf('THE TRIANGLE IS NOT POSSIBLE WITH GIVEN
        DIMENSIONS')

```

Scilab code Exa 2.13 To determine area of triangle when 2 sides and an angle is given

```
1 //Example 2.13
```

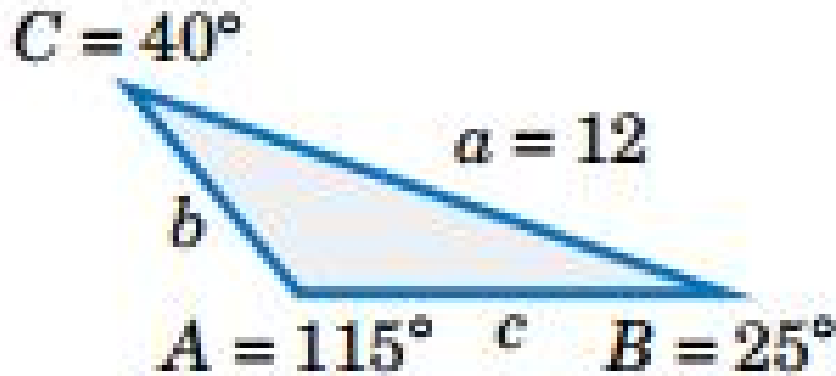


Figure 2.9: To determine area of triangle when 3 angles and a side is given

```

2 //To determine area of triangle when 2 sides and an
  angle is given
3 clc,clear
4
5 c=7 //side oposite to vertex C
6 A=33 //angle at vertex A
7 b=5 //side opposite to vertex B
8
9 area_K = b*c*sind(A)/2
10 printf('Area of triangle ABC = %.2f square units',
  area_K)

```

Scilab code Exa 2.14 To determine area of triangle when 3 angles and a side is given

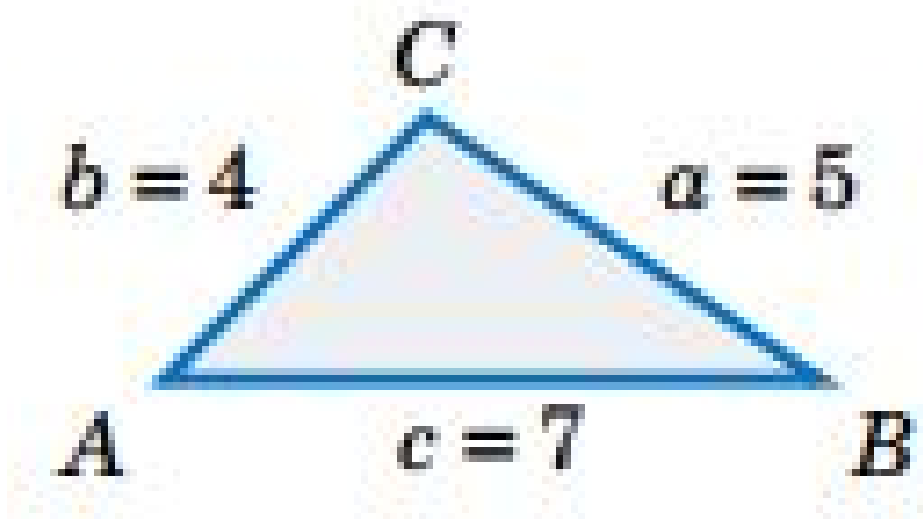


Figure 2.10: To determine area of triangle when 3 sides are given

```

1 //Example 2.14
2 //To determine area of triangle when 3 angles and a
  side is given
3 clc,clear
4
5 A=115 //angle at vertex A
6 a=12 //side opposite to vertex A
7 B=25 //angle at vertex B
8 C=40 //angle at vertex C
9
10 area_K = a^2*sind(B)*sind(C)/(2*sind(A))
11 printf('Area of triangle ABC = %.2f square units',
  area_K)

```

Scilab code Exa 2.15 To determine area of triangle when 3 sides are given

```
1 //Example 2.15
2 //To determine area of triangle when 3 sides are
   given
3 clc,clear
4
5 c=7 //side oposite to vertex C
6 a=5 //side opposite to vertex A
7 b=4 //side opposite to vertex B
8
9 s= (a+b+c)/2 //semi perimeter
10 area_K = sqrt(s*(s-a)*(s-b)*(s-c)) //using herons
   formula
11 printf('Area of triangle ABC = %.2f square units',
   area_K)
```

Scilab code Exa 2.16 To determine area of triangle when 3 sides are given

```
1 //Example 2.16
2 //To determine area of triangle when 3 sides are
   given
3 clc,clear
4
5 c=0.0000029 //side oposite to vertex C
6 a=1000000 //side opposite to vertex A
7 b=999999.9999979 //side opposite to vertex B
8
9 s= (a+b+c)/2 //semi perimeter
10 area_K = sqrt(s*(s-a)*(s-b)*(s-c)) //using herons
   formula
11 printf('Area of triangle ABC = %.3f square units\n\n
   ',area_K)
12
13 printf('Note:\n')
```

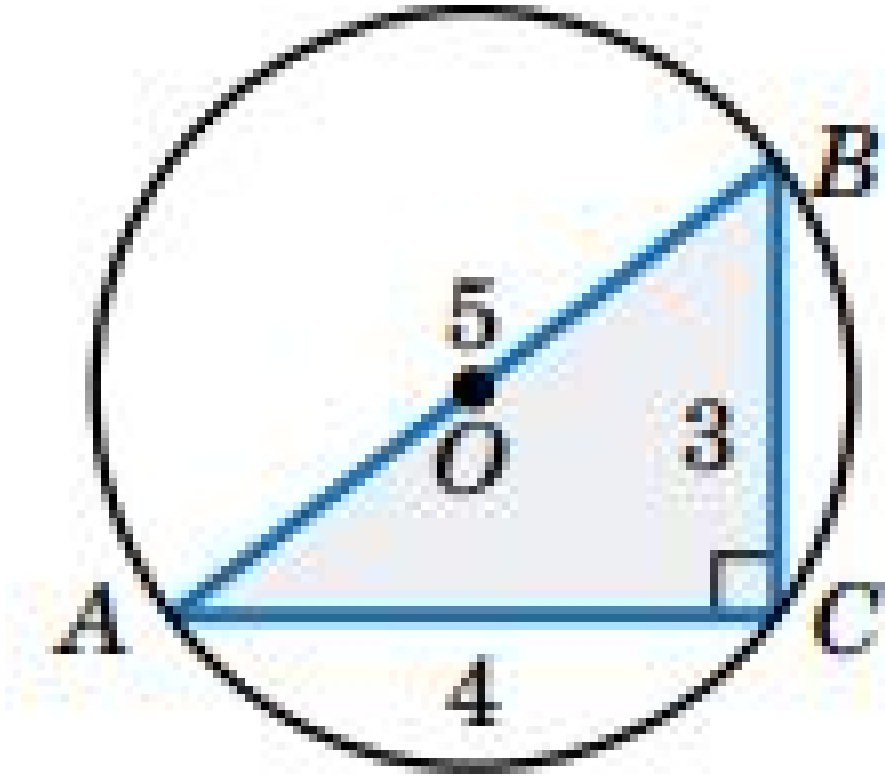


Figure 2.11: To find radius of circumscribed circle for triangle ABC

```

14 printf('In calculators like TI-83 plus, due to
    rounding off etc s will be 1000000\n')
15 printf('Therefore (s-a) is zero. And area will be
    zero according to herons formula\n')
16 printf('Due to large number of digits in scilab,(s-a
    ) is not zero. Thus, area is non-zero above.')
```

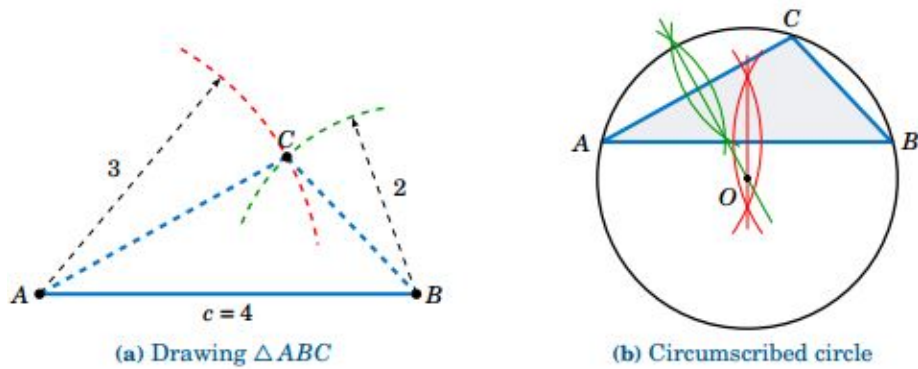


Figure 2.12: To find the radius of circumscribed circle for triangle ABC

Scilab code Exa 2.17 To find radius of circumscribed circle for triangle ABC

```

1 //Example 2.17
2 //To find radius of circumscribed circle for
  triangle ABC
3 clc, clear
4
5 c=5//side oposite to vertex C
6 a=3//side opposite to vertex A
7 b=4//side opposite to vertex B
8
9 cos_A = (c^2+b^2-a^2)/(2*c*b) //from law of cosines
10 A= acosd(cos_A)
11 diameter=(a/sind(A))
12 radius = diameter/2
13 printf('Radius of circumscribed circle = %.1f units
  \n',radius)
14 printf(' \nNote : \n Diameter is same as AB i.e. c...
  So centre of circle is mipoint of AB')
```

Scilab code Exa 2.18 To find the radius of circumscribed circle for triangle ABC

```
1 //Example 2.18
2 //To find the radius of circumscribed circle for
   triangle ABC
3 clc,clear
4
5 c=4 //side oposite to vertex C
6 a=2 //side oposite to vertex A
7 b=3 //side oposite to vertex B
8
9 cos_A = (c^2+b^2-a^2)/(2*c*b) //from law of cosines
10 A= acosd(cos_A)
11 diameter=(a/sind(A))
12 radius = diameter/2
13 printf('Radius of circumscribed circle = %.2f units
   \n\n',radius)
14
15 //To draw the triangle
16 printf('NOTE:\nPROCEDURE TO DRAW THE TRIANGLE ABC\n'
   )
17 printf('Use a ruler to draw the longest side AB of
   length c = 4.\n')
18 printf('Use a compass to draw arcs of radius 3 and 2
   centered at A and B respectively.\n')
19 printf('The intersection of the arcs is the vertex C
   .\n\n')
20
21 //To draw the circumscribed circle
22 printf('PROCEDURE TO DRAW CIRCUMSCRIBED CIRCLE\n')
23 printf('Draw the perpendicular bisectors of AB and
   AC.\n')
24 printf('Their intersection is the center O of the
```

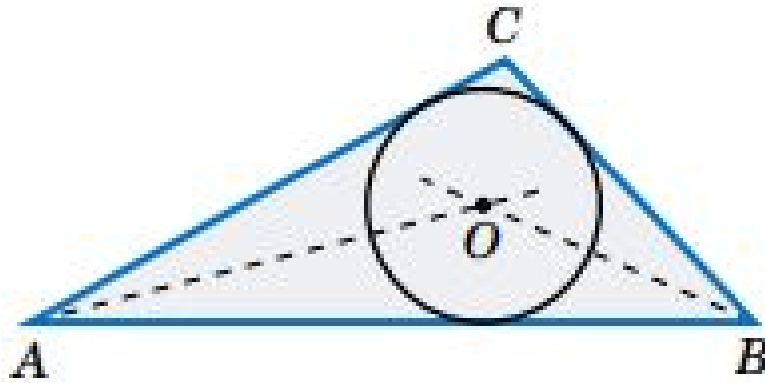


Figure 2.13: To determine radius of inscribed circle ABC

```

circle.\n')
25 printf('Use a compass to draw the circle centered at
    O which passes through A.')

```

Scilab code Exa 2.19 To determine radius of inscribed circle ABC

```

1 //Example 2.19
2 //To determine radius of inscribed circle ABC
3 clc,clear
4
5 c=4 //side opposite to vertex C
6 a=2 //side opposite to vertex A
7 b=3 //side opposite to vertex B
8
9 s= (a+b+c)/2 //semi perimeter
10 radius_r = sqrt((s-a)*(s-b)*(s-c)/s)

```

```
11 printf('Radius of inscribed circle is %.3f units=  
    sqrt(5/12)units ',radius_r)  
12 printf('\n\nNote:To obtain inscribed circle:\n(1)  
    Intersect perpendicular bisectors of A and B\n')  
13 printf('(2)Point of intersection is the centre of  
    circle\n')  
14 printf('(3)The radius is 0.645 as caculated above\n'  
    )  
15 printf('(4)Using a compass draw a circle with this  
    centre\n')
```

Chapter 3

Identities

Scilab code Exa 3.8 To determine values of functions of sum of 2 angles when functions of 2 angles are given

```
1  clc, clear
2  //Example 3.8
3  //To determine values of functions of sum of 2
   angles when functions of 2 angles are given
4
5  sin_A = 4/5 ;
6  cos_A = 3/5 ;
7
8  sin_B = 12/13 ;
9  cos_B = 5/13 ;
10
11 //Apb refers to A plus B
12 sin_ApB = sin_A*cos_B + cos_A*sin_B ;
13 cos_ApB = cos_A*cos_B - sin_A*sin_B ;
14 tan_ApB = sin_ApB / cos_ApB ;
15
16 printf('sin(A+B) = %f\n', sin_ApB) ;
17 printf('cos(A+B) = %f\n', cos_ApB) ;
18 printf('tan(A+B) = %f\n', tan_ApB) ;
```

Chapter 4

Radian Measure

Scilab code Exa 4.1 To convert a degree measure to radians

```
1 clc, clear
2 //Example 4.1
3 //To convert a degree measure to radians
4
5 deg=18 //degree measure
6 radian=deg*(%pi/180) //radian measure
7 printf('Radian measure is %f rad\n(or)\n',radian)
8 printf('Radian measure is (pi/%.0f)rad ',1/(radian/
    %pi))
```

Scilab code Exa 4.2 To convert a radian measure to degree

```
1 clc, clear
2 //Example 4.2
3 //To convert a radian meeasure to degree
4
5 radian=%pi/9 //radian measure
6 deg=radian/(%pi/180) //degree measure
7 printf('Degree measure is %.0f degree ',deg)
```

Scilab code Exa 4.3 To determine length of the intercepted arc

```
1 clc,clear
2 //Example 4.3
3 //To determine length of the intercepted arc
4
5 r=2 //radius of circle
6 theta=1.2 //central angle in radian
7
8 s=r*theta //length of arc
9 printf('Length of arc intercepted = %.1f cm',s)
```

Scilab code Exa 4.4 To determine length of the arc intercepted

```
1 clc,clear
2 //Example 4.4
3 //To determine length of the arc intercepted
4
5 r=10 //radius of circle
6 theta=41*(%pi/180) //central angle in radian
7
8 s=r*theta //length of arc
9 printf('Length of arc intercepted = %.2f ft',s)
```

Scilab code Exa 4.5 To determine angle in radians and degrees

```
1 clc,clear
2 //Example 4.5
3 //To determine angle in radians and degrees
```

```

4
5 r=5 //radius of circle
6 s=2 //length of arc
7 theta = s/r //central angle in radian
8 printf('Measure of central angle = %.2f rad\n',theta
)
9 printf('Measure of central angle = %.2f degree',
theta*(180/%pi))

```

Scilab code Exa 4.6 To determine the length of the rope

```

1 clc,clear
2 //Example 4.6
3 //To determine the length of the rope
4
5 d=8 //distance between places in feet
6 r=2 //radius of cylinder in feet
7 //from the figure
8 DA=d/2, BE=r
9 DE=3 //distance from centre of container to wall
10
11 AE=sqrt(DE^2 + DA^2) //pythagoras theorem
12 AB=sqrt(AE^2 - BE^2) //pythagoras theorem
13
14 //all angles below are in radians
15 angle_AED = atan((d/2)/DE)
16 angle_AEB = acos(BE/AE)
17 angle_BEC = %pi - (angle_AED + angle_AEB)
18 arc_BC = BE*angle_BEC //length of arc BC
19 L = 2*(AB + arc_BC) //length of rope
20 printf('Length of the rope = %.1f ft',L)

```

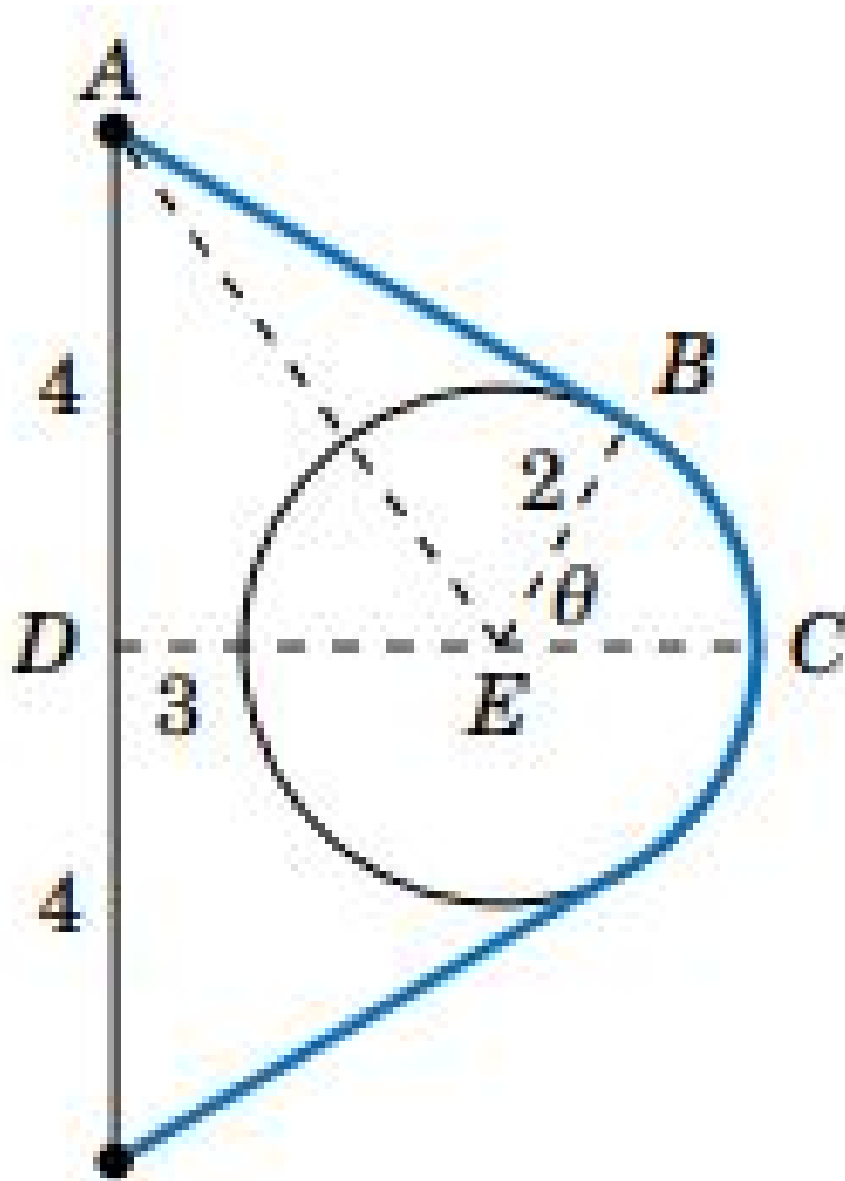


Figure 4.1: To determine the length of the rope

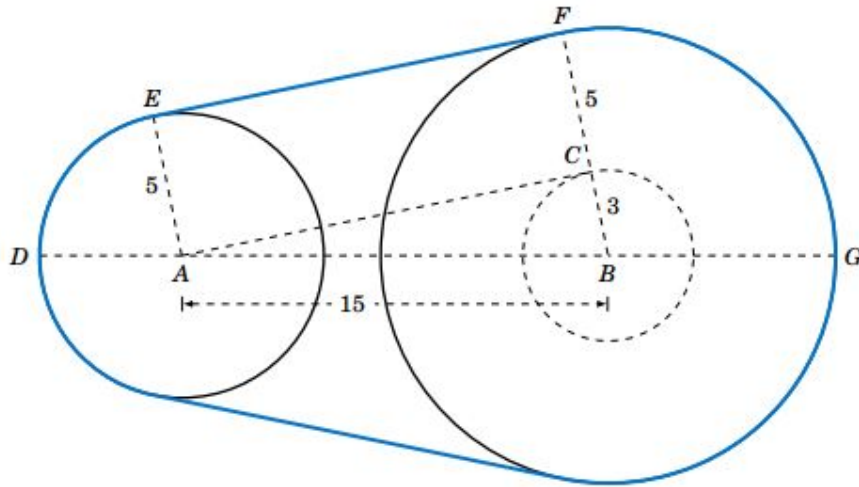


Figure 4.2: To determine the length of the belt around the pulleys

Scilab code Exa 4.7 To determine the length of the belt around the pulleys

```

1  clc, clear
2  //Example 4.7
3  //To determine the length of the belt around the
   pulleys
4
5  AE= 5 //radius of first pulley in cm
6  BF= 8 //radius of second pulley in cm
7  AB=15 //distance between centre of pulleys in cm
8
9  //from the figure
10 CF=AE //parallel side of rectangle ACFE
11 BC= BF- CF
12 AC = sqrt(AB^2 - BC^2) //by pythagoras theorem

```

```

13 EF=AC //parallel side of rectangle ACEF
14
15 angle_EAC = %pi/2
16 angle_BAC = asin(BC/AB)
17 angle_DAE = %pi - angle_EAC - angle_BAC
18 angle_ABC = angle_DAE //AE and BF are parallel
19 angle_GBF= %pi - angle_ABC
20
21 arc_DE=AE*angle_ABC //length of arc DE
22 arc_FG=BF*angle_GBF //length of arc FG
23 L=2*(arc_DE + EF + arc_FG) //length of belt
24 printf('Length of belt around pulley = %f cm',L)

```

Scilab code Exa 4.8 To find the area of sector of circle

```

1 clc ,clear
2 //Example 4.8
3 //To find the area of sector of circle
4
5 theta= %pi/5 //angle in radian
6 r=4 //radius in cm
7 A=r*r*theta/2 //Area of sector
8 printf('Area of sector = %.1f*pi cm^2\n(or)\n',A/%pi
9 )
9 printf('Area of sector = %f cm^2',A)

```

Scilab code Exa 4.9 To determine area of sector of a circle

```

1 clc ,clear
2 //Example 4.9
3 //To determine area of sector of a circle
4
5 theta= 117*(%pi/180) //angle in radian

```

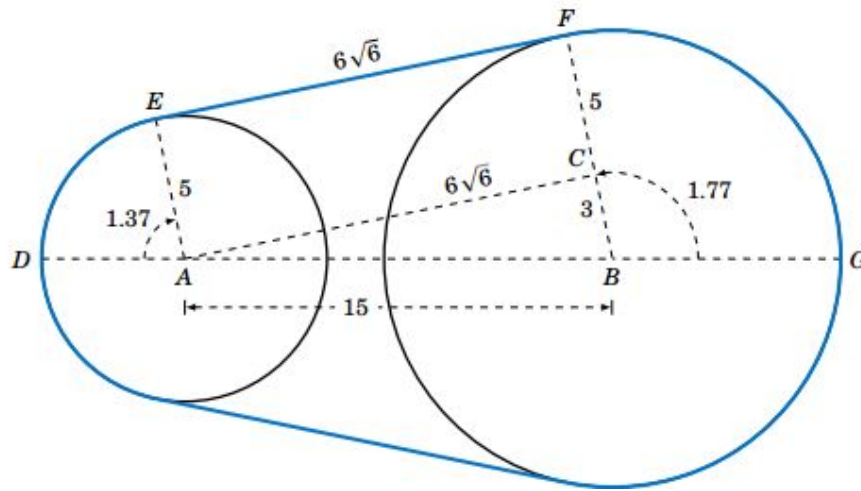


Figure 4.3: To determine area inside belt pulley system

```

6 r=3.5 //radius in m
7 A=r*r*theta/2 //Area of sector
8 printf('Area of sector = %.2f m^2 ',A)

```

Scilab code Exa 4.10 To determine area of sector of circle

```

1 clc,clear
2 //Example 4.10
3 //To determine area of sector of circle
4
5 s=6 //arc length in cm
6 r=9 //radius in cm
7 A=r*s/2 //Area of sector
8 printf('Area of sector = %.0f cm^2\n\n',A)
9 printf('Note: Angle subtended by arc = %f rad ',s/r)

```

Scilab code Exa 4.11 To determine area insude belt pulley system

```
1  clc, clear
2  //Example 4.11
3  //To determine area insude belt pulley system
4
5  AE= 5 //radius of first pulley
6  BF= 8 //radius of second pulley
7  AB=15 //distance between centre of pulleys
8
9  //from the figure
10 CF=AE
11 BC= BF- CF
12 AC = sqrt(AB^2 - BC^2)
13 //from the figure
14 angle_EAC = %pi/2
15 angle_BAC = asin(BC/AB)
16 angle_DAE = %pi - angle_EAC - angle_BAC
17 angle_ABC = angle_DAE //AE and BF are parallel
18 angle_GBF= %pi - angle_ABC
19
20 area_DAE = AE^2*angle_DAE/2 //area of sector DAE
21 area_GBF = BF^2*angle_GBF/2 //area of sector GBF
22 area_AEFC = AE*AC //area of rectangle AEFC
23 area_ABC = AC*BC/2 //area of triangle ABC
24
25 area_K=2*(area_DAE + area_AEFC + area_ABC + +
    area_GBF )
26 printf('Area enclosed by belt pulley system = %.2f
    cm^2',area_K)
27 printf('\\n\\nNote: answer differs from book due to
    approximations by them')
```

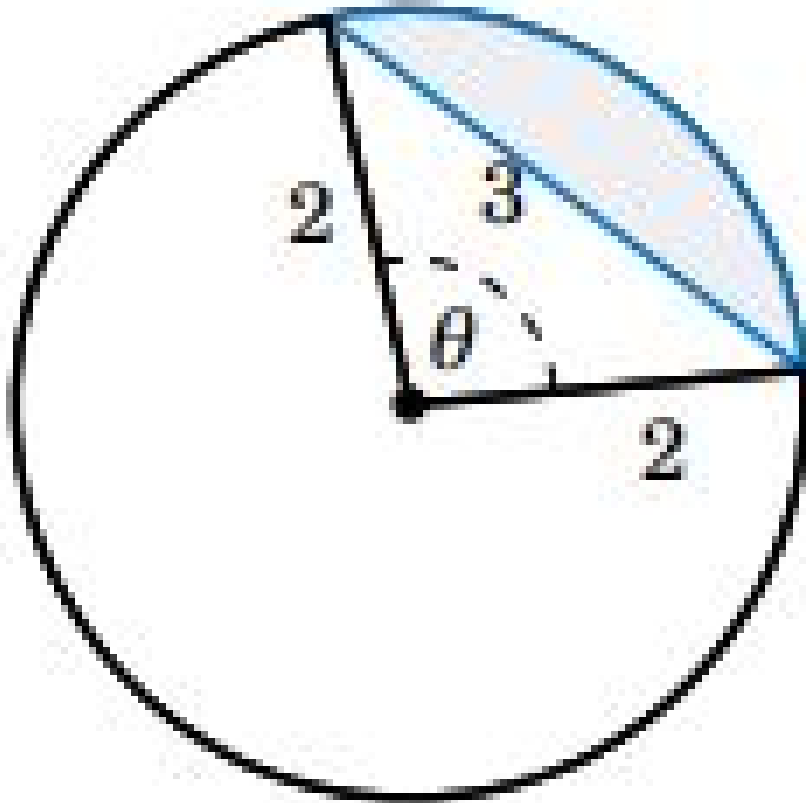


Figure 4.4: To determine area of segment formed by a chord in circle

Scilab code Exa 4.12 To determine area of segment formed by a chord in circle

```
1 clc , clear  
2 //Example 4.12
```

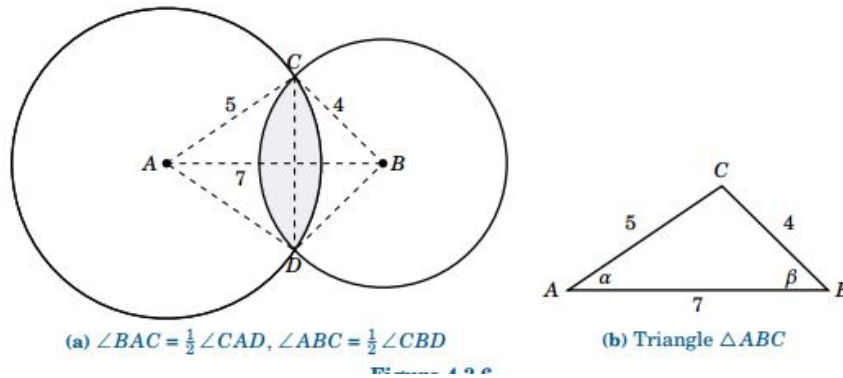


Figure 4.5: To determine area of intersection of 2 circles

```

3 //To determine area of segment formed by a chord in
  circle
4
5 radius = 2
6 chord = 3
7 //Use law of cosines
8 cos_theta = (radius^2+radius^2-chord^2)/(2*radius*
  radius)
9 theta=acos(cos_theta) //subtended central angle in
  radians
10
11 area_K=radius^2* (theta-sin(theta))/2
12 printf('Required area of segment = %.3f square units
  ',area_K)

```

Scilab code Exa 4.13 To determine area of intersection of 2 circles

```

1 clc , clear
2 //Example 4.13
3 //To determine area of intersection of 2 circles

```

```

4
5 d=7 //distance between centres in cm
6 r1= 5 //radius of first circle in cm
7 r2= 4 //radius of second circle in cm
8
9 //use law of cosines
10 cos_alpha=(d^2+ r1^2 - r2^2 ) /(2*d*r1)
11 cos_beeta=(d^2+ r2^2 - r1^2 ) /(2*d*r2)
12
13 //from the geometry of the figure
14 //all the angles below are in radians
15 alpha= acos(cos_alpha)
16 beeta= acos(cos_beeta)
17 angle_BAC = alpha
18 angle_ABC = beeta
19 angle_CAD =2* angle_BAC
20 angle_CBD =2* angle_ABC
21
22 //required area = area at segment CD in circle at A
    and at B
23 area_K = r1^2*(angle_CAD-sin(angle_CAD))/2 + r2
    ^2*(angle_CBD-sin(angle_CBD))/2
24 printf('Area of intersection of 2 circles = %.2f cm
    ^2',area_K)

```

Scilab code Exa 4.14 To find linear and angular speed of a moving object

```

1 clc,clear
2 //Example 4.14
3 //To find linear and angular speed of a moving
    object
4
5 t=0.5 //time in second
6 r= 3 //radius in m of the circle
7 theta = %pi/3 // central angle in radian

```



```

8 w = theta/t //angular speed in rad /sec
9 v=w*r//linear speed in m/sec
10
11 printf('Angular speed= %f radian/sec\n',w)
12 printf('Linear speed = %f m/sec ',v)
13
14 printf('\n\n(or)\n\nAngular speed= %f*pi radian/sec\n
        n ',w/%pi)
15 printf('Linear speed = %f*pi m/sec ',v/%pi)

```

Scilab code Exa 4.15 To find linear and angular speed of a moving object

```

1 clc , clear
2 //Example 4.15
3 //To find linear and angular speed of a moving
  object
4
5 t=2.7 //time in second
6 r= 2 //radius in ft of the circle
7 s=35 //distance in feet
8
9 v=s/t //linear speed in ft/sec
10 w=v/r //angular speed in rad /sec
11
12 printf('Linear speed = %.2f ft/sec\n',v)
13 printf('Angular speed= %.2f radian/sec\n',w)

```

Scilab code Exa 4.16 To find the central angle swept by a moving object

```

1 clc , clear
2 //Example 4.16
3 //To find the central angle swept by a moving object
4

```

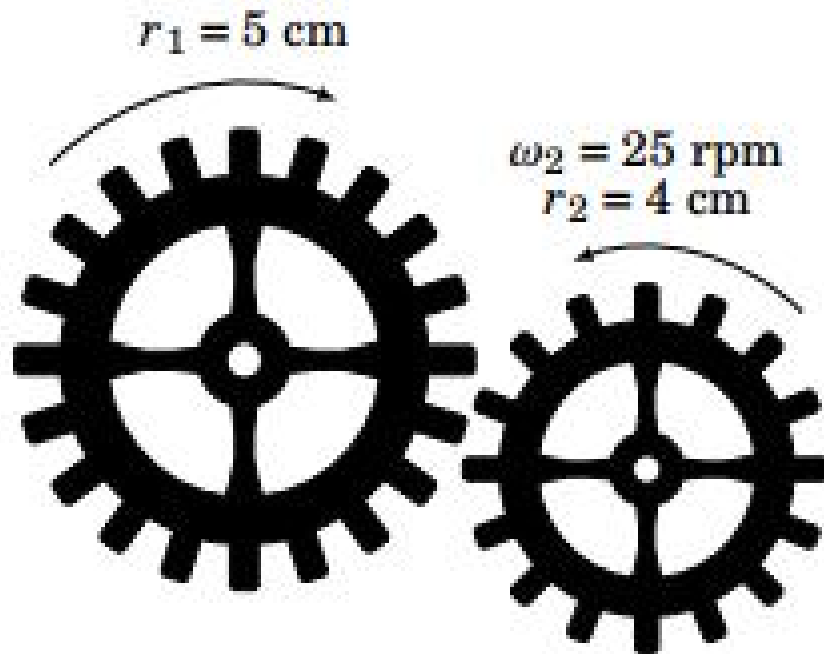


Figure 4.6: To find the angular speed of larger gear interlocked with smaller gear

```

5 t=3.1 //time in second
6 v= 10 //linear speed in m/sec
7 r= 4 //radius in m of the circle
8 s=v*t //distance in m
9
10 theta = s/r //central angle swept
11 printf('central angle swept = %.2f radian ',theta)

```

Scilab code Exa 4.17 To find the angular speed of larger gear interlocked with smaller gear

```
1 clc,clear
2 //Example 4.17
3 //To find the angular speed of larger gear
   interlocked with smaller gear
4
5 r1=5 //radius of larger gear
6 r2=4 //radius smaller gear
7 w2=25 //angular speed of smaller gear
8
9 // Imagine a particle on outer radii of each gear
10 //At any time, for every rotation, circular
   displacement of each particle is same
11 // (or)  $s_1=s_2$  implies  $v_1*t=v_2*t$ 
12 //  $v_1= v_2$  implies  $w_1*r_1=w_2*r_2$ 
13
14 w1=(w2*r2)/r1 //angular speed of larger gear
15 printf('Angular speed of larger gear= %.0f rpm ',w1)
```

Chapter 5

Graphing and inverse functions

Scilab code Exa 5.1 To sketch the graph of minus $\sin x$ in a given interval

```
1 //Example 5.1
2 //To sketch the graph of minus  $\sin x$  in a given
   interval
3 clear,clc;
4
5 x = linspace(-0,2*%pi,50);
6 y = -sin(x) ;
7 set(gca(),"grid",[5 5]);
8 plot(x,y);
9 xlabel("$0 \le x \le 2\pi$", "fontsize",4,"color","red"
   );
10 ylabel("$y(x)=-\sin(x)$", "fontsize",4,"color","red");
11 title("Example 5.1", "color","blue", "fontsize",9);
```

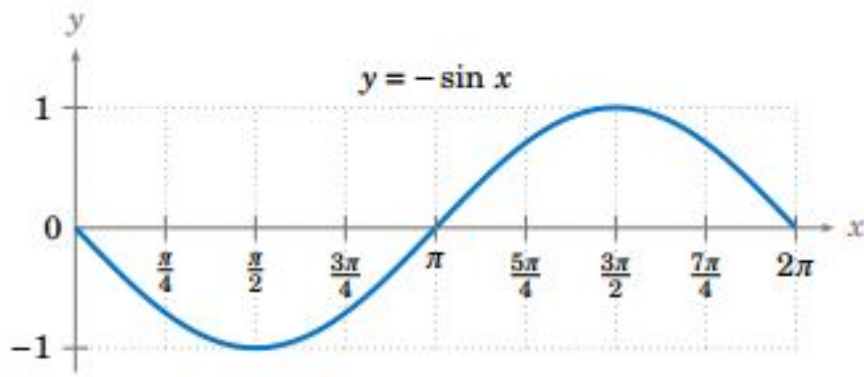


Figure 5.1: To sketch the graph of minus sinx in a given interval

Example 5.1

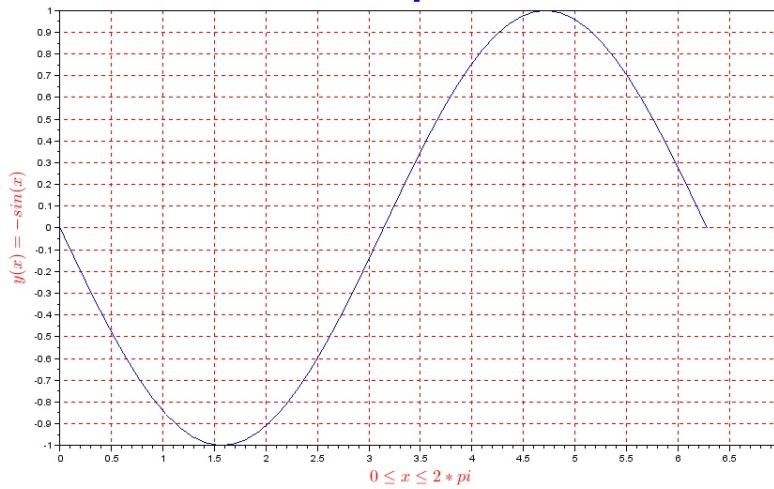


Figure 5.2: To sketch the graph of minus sinx in a given interval

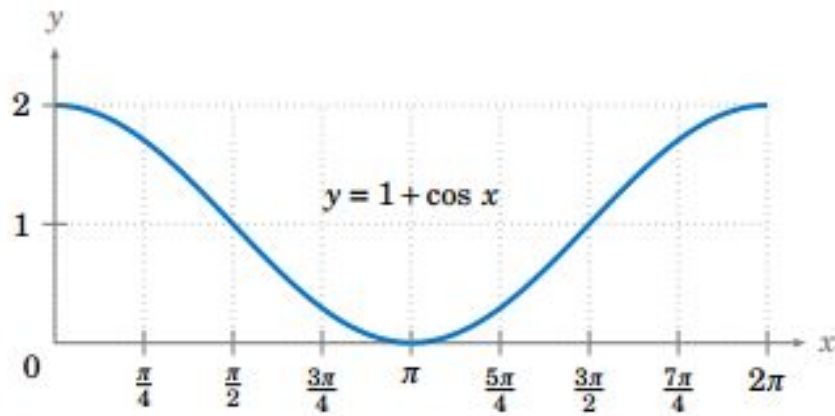


Figure 5.3: To sketch the graph of given function of in given interval

Scilab code Exa 5.2 To sketch the graph of given function of in given interval

```

1 //Example 5.2
2 //To sketch the graph of function of 1+cos(x) in
  given interval
3 clear,clc;
4
5 x = linspace(-0,2*pi,50);
6 y = 1+cos(x) ;
7 set(gca(),"grid",[5 5]);
8 plot(x,y);
9 xlabel("$0 \le x \le 2\pi$","fontsize",4,"color","red"
  );
10 ylabel("$y(x)=1+\cos(x)$","fontsize",4,"color","red")
  ;
11 title("Example 5.2","color","blue","fontsize",9);

```

Example 5.2

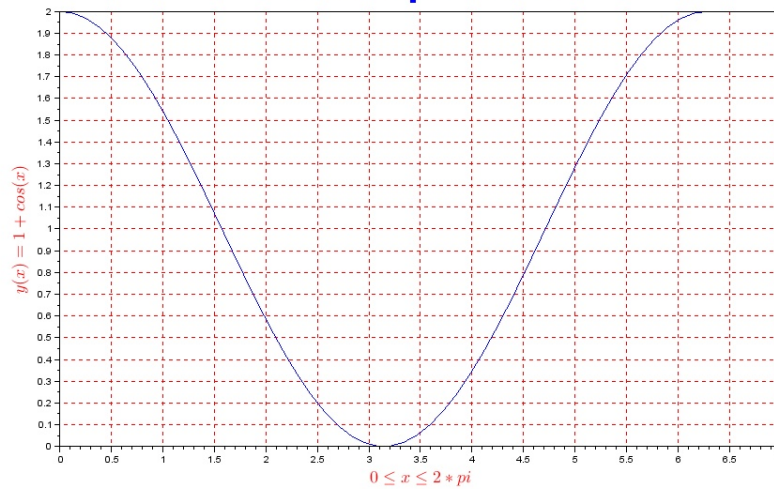


Figure 5.4: To sketch the graph of given function of in given interval

Scilab code Exa 5.4 To determine the period of given sinusoidal function

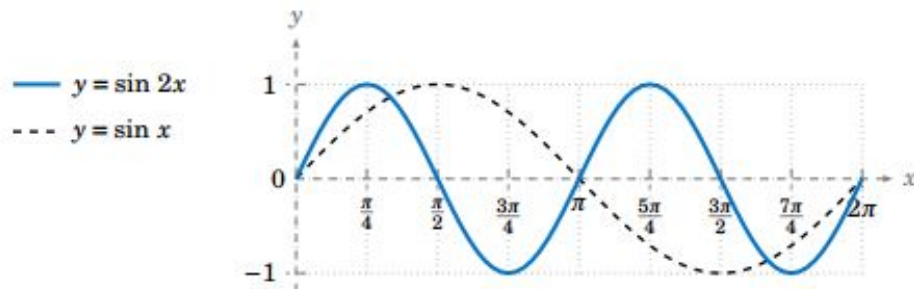


Figure 5.5: To determine the period of given sinusoidal function

```

1 //Example 5.4
2 //To determine the period of given sinusoidal
   function
3 clear,clc;
4
5 multiple = 2; //multiplicity of angle
6 period_sinx = 2*pi ;//period of sin(x) in radians
7 required_period = period_sinx / multiple;
8 printf('Required period is %f radians',
   required_period);
9
10 //Note that sin 2x goes twice as fast as sin x
   .
11 //While sin x takes a full 2*pi radians to go
   through an entire cycle
12 //sin 2x goes through an entire cycle in just pi
   radians
13
14 x = linspace(-0,2*pi,100);
15 y = sin(2*x) ;
16 z = sin(x) ;
17 set(gca(),"grid",[4 4]);
18 plot(x,y,'r-');
19 plot(x,z,'b-');
20 xlabel("$0 \le x \le 2\pi$","fontsize",4,"color","red"
   );
21 ylabel("$y(x)=\sin(2x)$","fontsize",4,"color","red");
22 title("Example 5.4","color","blue","fontsize",9);
23 legend(["sin(2x)";"sin(x)"]);

```

Scilab code Exa 5.5 To determine the period of 2 given cosine functions

Example 5.4

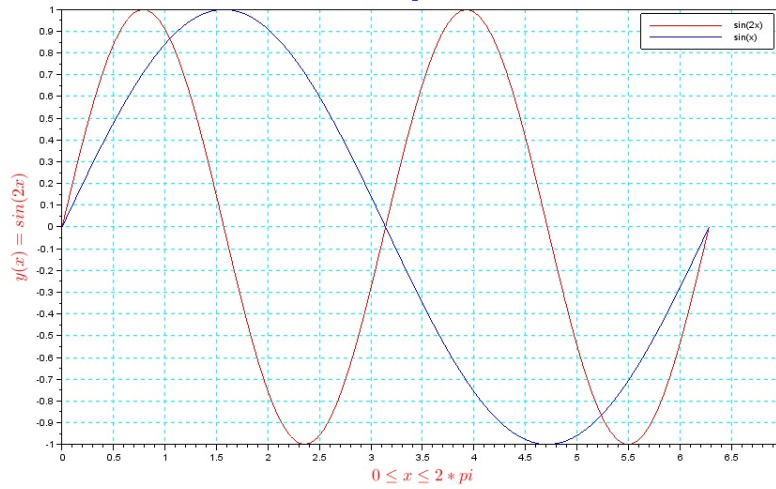


Figure 5.6: To determine the period of given sinusoidal function

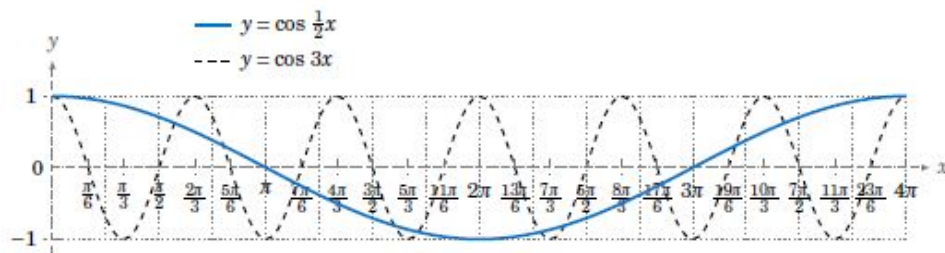


Figure 5.7: To determine the period of 2 given cosine functions

```

1 //Example 5.5
2 //To determine the period of 2 given cosine
   functions
3 clear,clc;
4
5 //y=cos(3*x)
6 multiple = 3; //multiplicity of angle
7 period_cosx = 2*%pi; //period of sin(x) in radians
8 required_period = period_cosx / multiple;
9 printf('Period of cos(3*x)is %f radians\n',
   required_period);
10
11 //y=cos(0.5*x)
12 multiple = 1/2; //multiplicity of angle
13 period_cosx = 2*%pi; //period of sin(x) in radians
14 required_period = period_cosx / multiple;
15 printf('Period of cos(x/2)is %f radians ',
   required_period);
16
17 x = linspace(-0,4*%pi,200);
18 y = cos(3*x) ;
19 z = cos(x/2) ;
20 set(gca(),"grid",[4 4]);
21 plot(x,y,'r-');
22 plot(x,z,'b-');
23 xlabel("$0 \le x \le 4*pi$","fontsize",4,"color","red"
   );
24 title("Example 5.5","color","blue","fontsize",9);
25 legend(["y = cos(3x)";"y = cos(x/2)"]);

```

Example 5.5

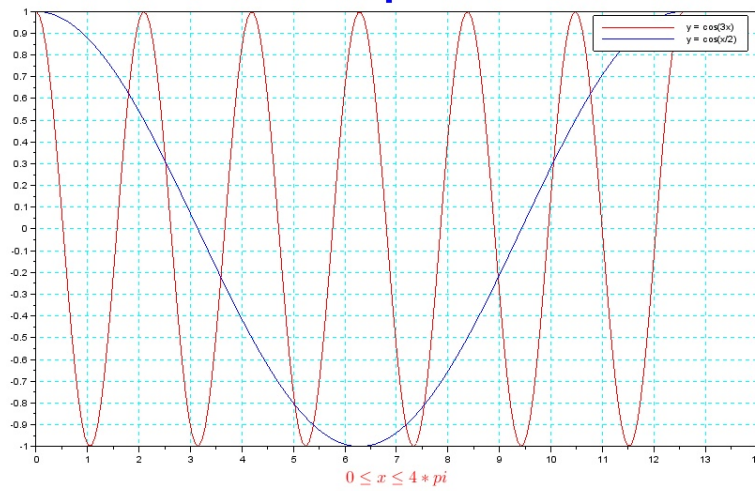


Figure 5.8: To determine the period of 2 given cosine functions

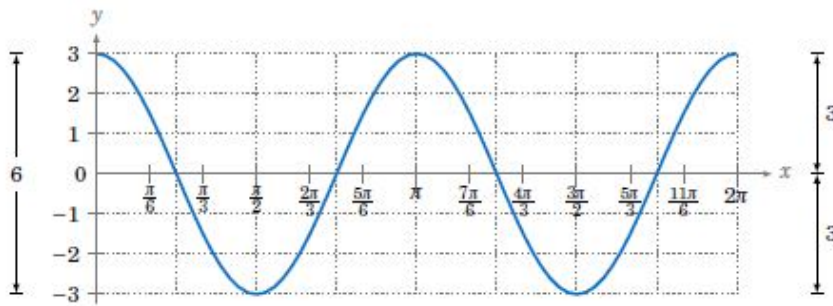


Figure 5.9: To determine the amplitude and period of given function

Scilab code Exa 5.6 To determine the amplitude and period of given function

```
1 //Example 5.6
2 //To determine the amplitude and period of given
  function
3 clear,clc;
4
5 x = linspace(-0,4*pi,200);
6 y = 3*cos(2*x) ; //given function
7 amplitude = y/cos(2*x);
8 printf('Amplitude = %f',amplitude);
9
10 multiple = 2; //multiplicity of angle
11 period_cosx=2*pi; //period od cos(x)
12 period_required = period_cosx / multiple;
13 printf('\nPeriod = %f radians ',period_required);
14
15 x = linspace(-0,2*pi,50);
16 y = 3*cos(2*x) ;
17 set(gca(),"grid",[5 5]);
18 plot(x,y);
19 xlabel("$0 \le x \le 2\pi$","fontsize",4,"color","red"
  );
20 ylabel("$y(x)=3\cos(2x)$","fontsize",4,"color","red"
  );
21 title("Example 5.6","color","blue","fontsize",9);
```

Scilab code Exa 5.7 To find amplitude and period of given composite function

Example 5.6

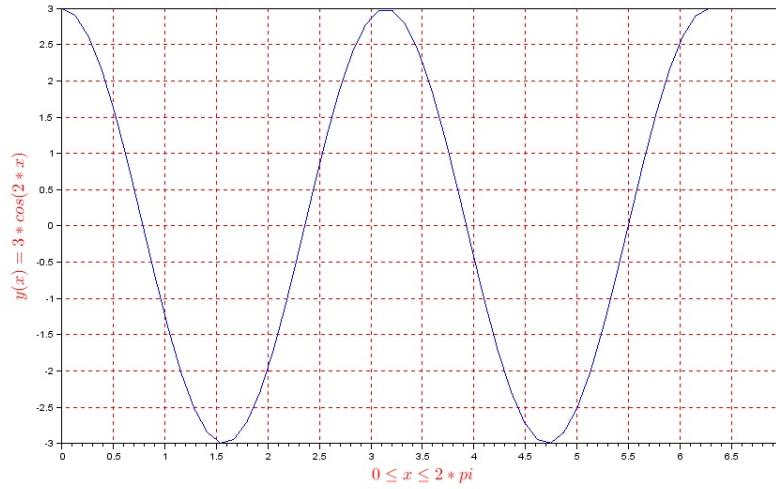


Figure 5.10: To determine the amplitude and period of given function

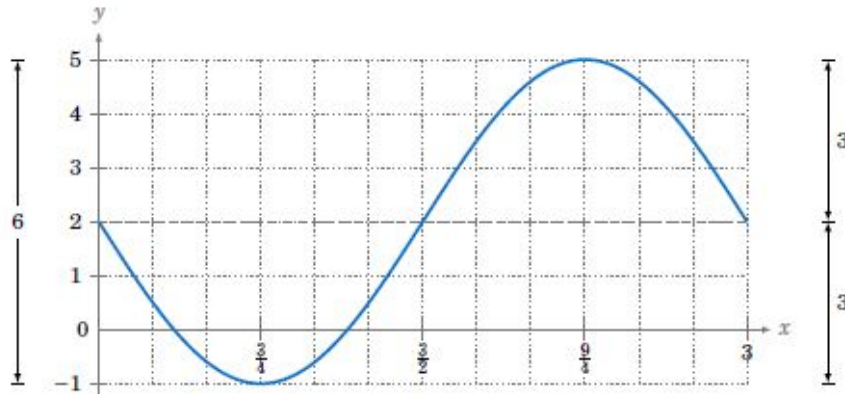


Figure 5.11: To find amplitude and period of given composite function

```

1 //Example 5.7
2 //To find amplitude and period of given composite
  function
3 clear,clc;
4
5 x = linspace(0,3,200);
6 y1=2 ;//1st part of given function
7 amplitude1=y1 ;//amplitude numerically same for
  constant function
8 y2= -3*sin((2*pi/3)*x); //second part of given
  function
9 amplitude2 = abs(y2/sin((2*pi/3)*x)) ;//amplitude
  of part 2
10 //Note: adding 2 doesnt change amplitude
11 //It just causes the upward shift of graph
12 maax =amplitude1 + amplitude2; //altered maximum due
  to adding of 2
13 minn =amplitude1 - amplitude2;//altered minimum due
  to adding of 2
14 amplitude = (maax-minn)/2;//required amplitude
15 printf('Amplitude = %f',amplitude);
16
17 multiple=2*pi/3 ;//multiplicity of angle
18 period_sinx=2*pi;//period of sin_x
19 period_required = period_sinx/ multiple;
20 printf('\nRequired period is %f radians',
  period_required);
21
22 x = linspace(0,3,200);
23 y = 2 -3*sin((2*pi/3)*x)
24 set(gca(),"grid",[5 5]);
25 plot(x,y);
26 xlabel("$0 \le x \le 3$","fontsize",4,"color","red");
27 ylabel("$y(x)= 2 -3*\sin((2*pi/3)*x)$","fontsize",4,
  "color","red");
28 title("Example 5.7","color","blue","fontsize",9);

```

Example 5.7

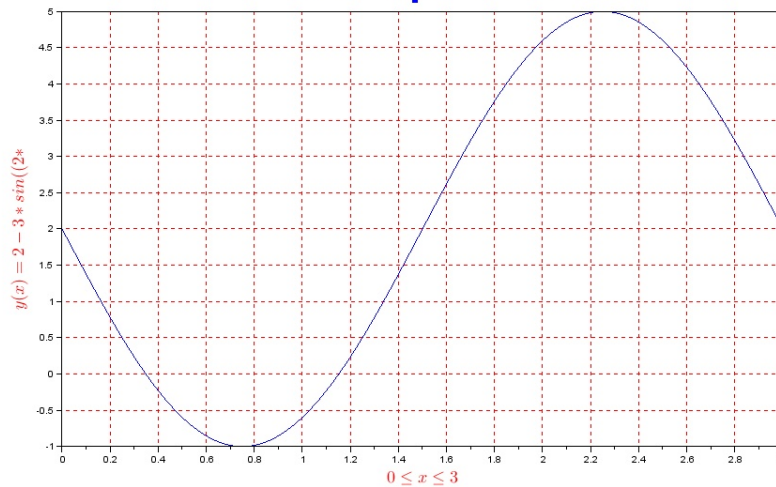


Figure 5.12: To find amplitude and period of given composite function

Scilab code Exa 5.8 To find the amplitude and period of given function

```
1 //Example 5.8
2 //To find the amplitude and period of given function
3 clear,clc;
4
5 //Period
6 printf('PERIOD:\n')
7 printf('This isnt a periodic function as x^2 is
   linearly related to x \n')
8 printf('and hence period doesnt exist\n')
9
```

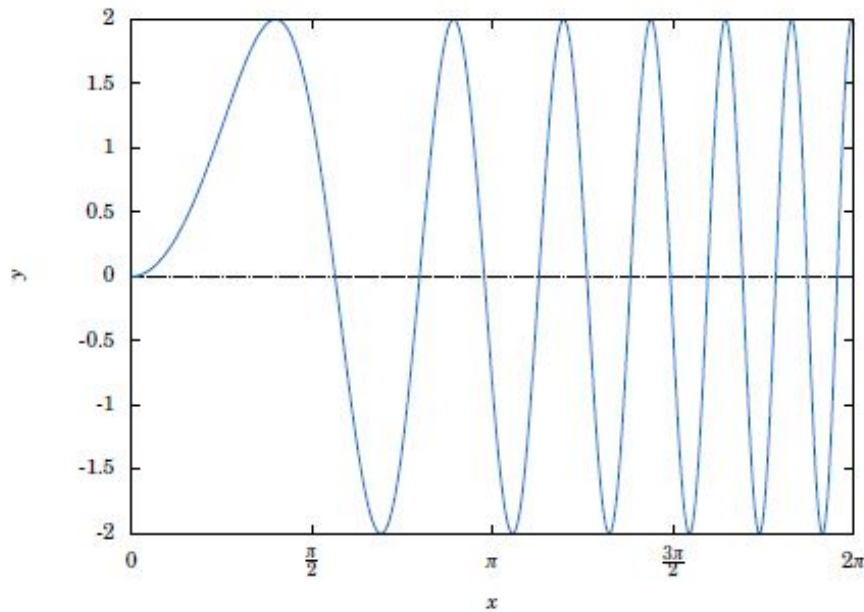


Figure 5.13: To find the amplitude and period of given function

```

10 //Amplitude
11 x = linspace(0,2*%pi,200);
12 y = 2*sin(x^2);
13 amplitude= y/sin(x^2);
14 printf('AMPLITUDE:\n')
15 printf('Amplitude exists unlike period\n')
16 printf('Because sine component of the given function
    never exceeds 1\n')
17 printf('Function value is always less than constant
    factor adjacent to sine\n')
18 printf('Hence amplitude is the constant factor
    multiplied with sine component\n\n')
19 printf('Amplitude = %f as calculated\n',amplitude)
20
21
22 x = linspace(0,2*%pi,200);
23 y = 2*sin(x^2) ;
24 set(gca(),"grid",[5 5]);

```


Example 5.8

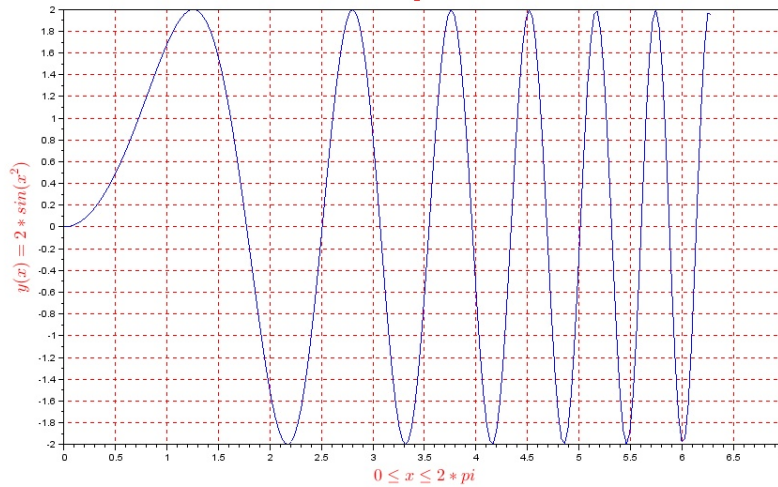


Figure 5.14: To find the amplitude and period of given function

```
25 plot(x,y, 'b');
26 xlabel("$0 \le x \le 2 * pi$", "fontsize", 4, "color", "red"
    );
27 ylabel("$y(x)= 2 * sin(x^2)$", "fontsize", 4, "color", "
    red");
28 title("Example 5.8", "color", "red", "fontsize", 9);
```

Scilab code Exa 5.9 To find the amplitude and period of given function

```
1 //Example 5.9
2 //To find the amplitude and period of given function
3 clear, clc;
4
```

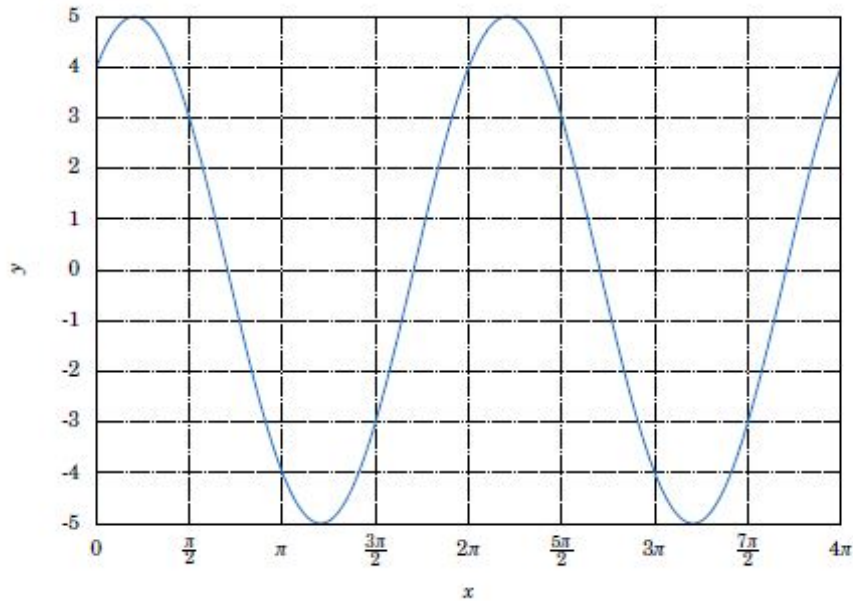


Figure 5.15: To find the amplitude and period of given function

```

5 //amplitude
6 x = linspace(-0,4*pi,200);
7 y1=3*sin(x); //1st part of given function
8 amplitude1=y1/sin(x); //amplitude of part 1
9 y2= 4*cos(x); //second part of given function
10 amplitude2 =y2/(cos(x)); //amplitude of part 2
11
12 //given function is a composition of 2 functions
13 //Using trigonometric identities , merge them into 1
14 //the amplitude of resultant is the required
    amplitude
15 //In this case the merged function can be sine or
    cos
16 //merging sine and cos into sine ,
17 amplitude = sqrt(amplitude1^2 + amplitude2^2);
18 printf('Amplitude = %f',amplitude);
19
20 //period

```

Example 5.9

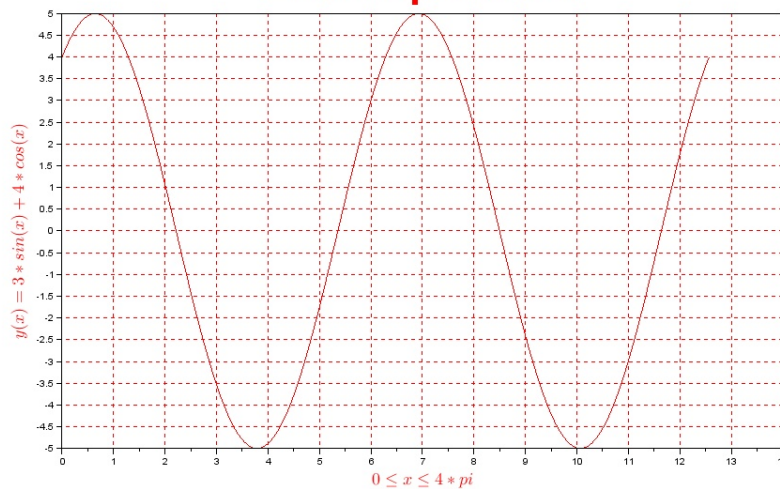


Figure 5.16: To find the amplitude and period of given function

```
21 period_cosx=2*pi ;//period of cos(x) is 2 pi
22 period_sinx=2*pi ;//period of sin(x) is 2 pi
23 locm = 2*pi; //lcm of period_sinx and period_cosx
24 printf('\nRequired period is %f radians',locm);
25 x = linspace(0,4*pi,200);
26 y = 3*sin(x) +4*cos(x);
27 set(gca(),"grid",[5 5]);
28 plot(x,y,'r');
29 xlabel("$0 \le x \le 4 * pi$","fontsize",4,"color","red"
);
30 ylabel("$y(x)= 3 * sin(x) +4 * cos(x)$","fontsize",4,"
color","red");
31 title("Example 5.9","color","red","fontsize",9);
```

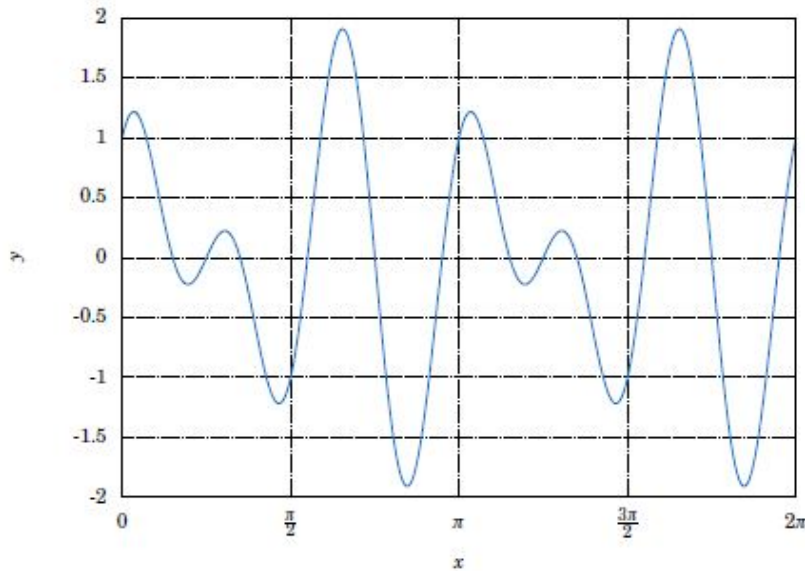


Figure 5.17: To find the period of given function

Scilab code Exa 5.10 To find the period of given function

```

1 //Example 5.10
2 //To find the period of given function
3 clear,clc;
4
5 x = linspace(-0,2*%pi,200);
6 y1=cos(6*x); //1st part of given function
7 multiple1=6;//multiplicity of angle
8 period_cosx=2*%pi ;//period of cos(x) is 2 pi
9 period1= period_cosx/ multiple1;
10 printf('Note: Period of cos(%d*x)= %f radians\n',
        multiple1,period1);
11 y2= sin(4*x); //second part of given function
12 multiple2=4; //multiplicity of angle

```

```

13 period_sinx=2*pi ;//period of sin(x) is 2 pi
14 period2= period_sinx/multiple2;
15 printf('Period of sin(%d*x)= %f radians\n',multiple2
        ,period2);
16
17 locm = %pi ;//LCM of period1 and period 2
18 period = locm ;//final period
19 printf('\nRequired period is %f radians ',period);
20 x = linspace(0,2*pi,200);
21 y = cos(6*x)+ sin(4*x);//given function
22 set(gca(),"grid",[5 5]);
23 plot(x,y,'r');
24 xlabel("$0 \le x \le 2\pi$","fontsize",4,"color","red"
        );
25 ylabel("$y(x)= \sin(4*x) +\cos(6*x)$","fontsize",4,"
        color","red");
26 title("Example 5.10","color","red","fontsize",9);

```

Scilab code Exa 5.11 To find the amplitude phase shift and period of given function

```

1 //Example 5.11
2 //To find the amplitude phase shift and period of
   given function
3 clear,clc;
4
5 x = linspace(-0,2*pi,200);
6 deviation = %pi; //deviation from multiples of x
7 y = 3*cos(2*x- deviation) ;//given function
8 amplitude = y/ cos(2*x- %pi) ;
9 printf('Amplitude = %f\n',amplitude);

```

Example 5.10

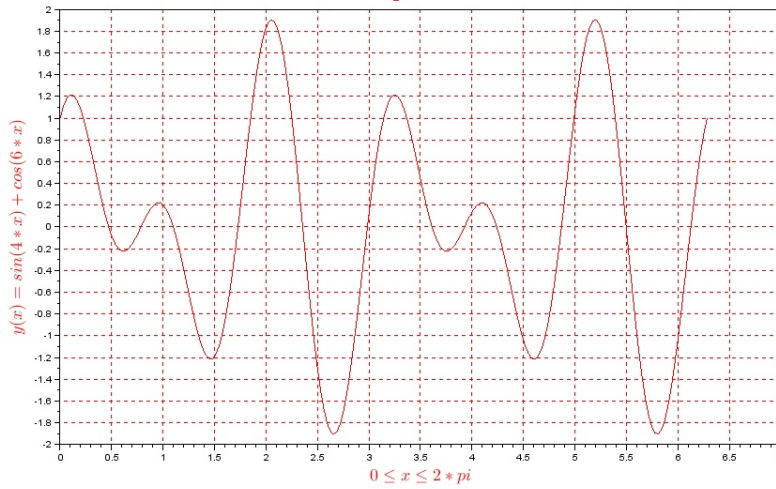


Figure 5.18: To find the period of given function

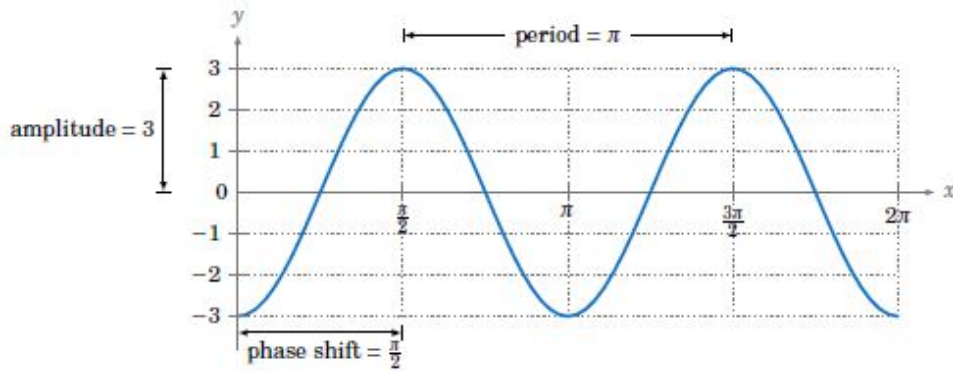


Figure 5.19: To find the amplitude phase shift and period of given function

```

10 multiple = 2; //multiplicity of angle
11 period_cosx = 2*%pi; //period of sin(x) in radians
12 required_period = period_cosx / multiple;
13 printf('Required period = %f radians\n',
        required_period);
14 phase_shift = deviation / multiple;
15 printf('Phase shift = %f radians ',phase_shift);
16
17 x = linspace(-0,2*%pi,200);
18 y = 3*cos(2*x- %pi) ;
19 set(gca(),"grid",[5 5]);
20 plot(x,y);
21 xlabel("$0 \le x \le 2\pi$","fontsize",4,"color","red"
        );
22 ylabel("$y(x)=3\cos(2x- \pi)$","fontsize",4,"color",
        "red");
23 title("Example 5.11","color","blue","fontsize",9);

```

Scilab code Exa 5.12 To find the amplitude phase shift and period of given function

```

1 //Example 5.12
2 //To find the amplitude phase shift and period of
   given function
3 clear,clc;
4
5 x = linspace(-%pi/6,4*%pi/3,200);
6 deviation = -%pi/2; //deviation from multiples of x
7 y = -2*sin(3*x- deviation) ;// given function
8 amplitude = abs(y/(sin(3*x- deviation))) );
9 printf('Amplitude = %f\n',amplitude);

```

Example 5.11

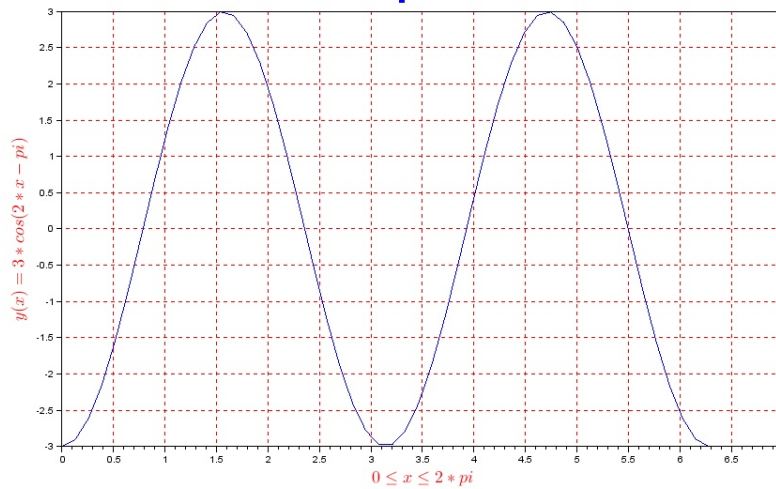


Figure 5.20: To find the amplitude phase shift and period of given function

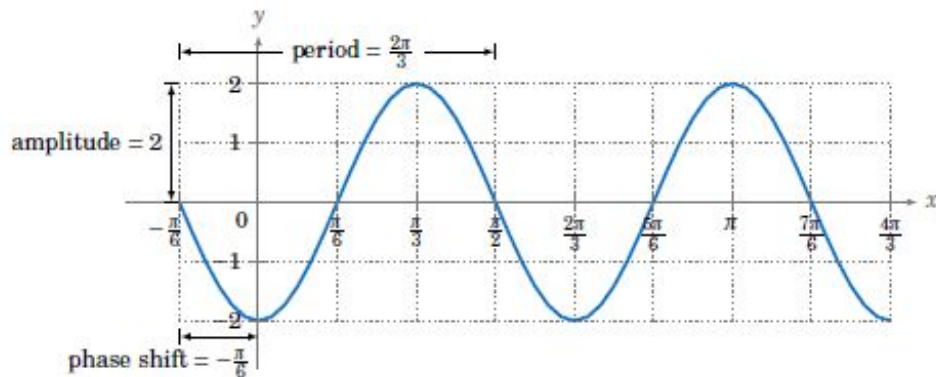


Figure 5.21: To find the amplitude phase shift and period of given function

Example 5.12

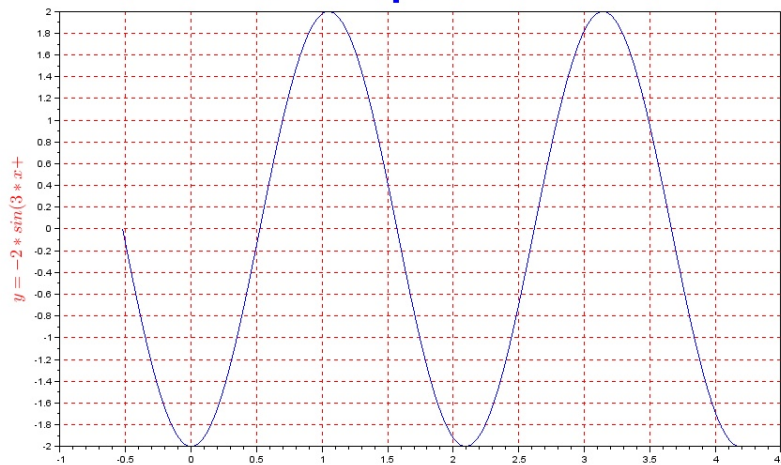


Figure 5.22: To find the amplitude phase shift and period of given function

```
10 multiple = 3; //multiplicity of angle
11 period_sinx = 2*pi ;//period of sin(x) in radians
12 required_period = period_sinx / multiple;
13 printf('Required period = %f radians\n',
        required_period);
14 phase_shift = deviation / multiple;
15 printf('Phase shift = %f radians ',phase_shift);
16
17 x = linspace(-pi/6,4*pi/3,200);
18 y = -2*sin(3*x+ pi/2) ;
19 set(gca(),"grid",[5 5]);
20 plot(x,y);
21 ylabel("$y = -2*sin(3*x+ pi/2)$","fontsize",4,"color",
        "red");
22 title("Example 5.12","color","blue","fontsize",9);
```

Scilab code Exa 5.13 To determine inverse sine function of a given value

```
1 clc,clear;  
2 //Example 5.13  
3 //To determine inverse sine function of a given  
   value  
4  
5 given = sin(%pi/4); //given value  
6 answer= asin(given); //final answer  
7  
8 printf('Required answer is %f radians',answer);  
9 printf('\\n\\nOR \\n\\n(pi/4)*%f radians ',answer*(4/%pi)  
   );
```

Scilab code Exa 5.14 To determine inverse sine function of a given value

```
1 clc,clear;  
2 //Example 5.14  
3 //To determine inverse sine function of a given  
   value  
4  
5 given = sin(5*%pi/4); //given value  
6 answer= asin(given); //final answer  
7  
8 printf('Required answer is %f radians',answer);  
9 printf('\\n\\nOR \\n\\n(pi/4)*%f radians ',answer*(4/%pi)  
   );
```

Scilab code Exa 5.15 To determine inverse cosine function of a given value

```

1 clc,clear;
2 //Example 5.15
3 //To determine inverse cosine function of a given
  value
4
5 given = cos(%pi/3); //given value
6 answer= acos(given); //final answer
7
8 printf('Required answer is %f radians',answer);
9 printf('\\n\\nOR \\n\\n(pi/3)*%f radians',answer*(3/%pi)
  );

```

Scilab code Exa 5.16 To determine inverse cosine function of a given value

```

1 clc,clear;
2 //Example 5.16
3 //To determine inverse cosine function of a given
  value
4
5 given = cos(4*%pi/3); //given value
6 answer= acos(given); //final answer
7
8 printf('Required answer is %f radians',answer);
9 printf('\\n\\nOR \\n\\n(pi/3)*%f radians',answer*(3/%pi)
  );

```

Scilab code Exa 5.17 To determine inverse tan function of a given value

```

1 clc,clear;
2 //Example 5.17
3 //To determine inverse tan function of a given value
4
5 given = tan(%pi/4); //given value

```

```

6 answer= atan(given); //final answer
7
8 printf('Required answer is %f radians',answer);
9 printf('\n\nOR \n\n(pi/4)*%f radians',answer*(4/%pi)
);

```

Scilab code Exa 5.18 To determine inverse tan function of a given value

```

1 clc,clear;
2 //Example 5.18
3 //To determine inverse tan function of a given value
4
5 given = tan(%pi); //given value
6 answer= atan(given); //final answer
7
8 printf('Required answer is %f radians',answer);

```

Scilab code Exa 5.19 To determine exact value of given expression involving inverse trigonometric functions

```

1 clc,clear;
2 //Example 5.19
3 //To determine exact value of given expression
  involving inverse trigonometric functions
4
5 expression= cos(asin(-1/4)); //given expression
6
7 printf('Value of given expression is %f radians',
  expression);

```

Chapter 6

Additional Topics

Scilab code Exa 6.3 To solve the given equation

```
1 clc, clear
2 //Example 6.3
3 //To solve the given equation
4
5 sec_theta = 1/2
6 cos_theta = 1 / sec_theta
7 printf('cos(theta) = %f as calculated\n',cos_theta)
8 printf('But value of cos function can never exceed
   unity\n')
9 printf('Thus, NO SOLUTION exists')
```

Scilab code Exa 6.4 To solve the given equation

```
1 clc, clear
2 //Example 6.4
3 //To solve the given equation
4
5 //Given equation is cos_theta = tan_theta
```

```

6 //simplifyfing given equation , we get
7 //((sin_theta)^2 + sin_theta - 1 = 0
8 //Solve for sin_theta as follows
9 p=[1 1 -1]
10 sin_theta= roots(p)
11 printf('Values of sin(theta) after simplifying and
        solving = %f and %f\n',sin_theta(1),sin_theta(2))
12 printf('Eliminate %f as sin_theta cant be below -1',
        sin_theta(1))
13
14 //Since sin_theta is +ve, 2 solutions exist. in 1st
        and 2nd quadrant
15 theta_1=asin(sin_theta(2)); //in 1st quadrant
16 theta_2=%pi-asin(sin_theta(2));//the reflection in 2
        nd quadrant
17
18 printf('\n\nSOLUTIONS:\n')
19 printf('%f radians\n%f radians ',theta_1,theta_2)
20
21 printf('\n\nGENERAL SOLUTIONS:\n')
22 printf('%f + integer multiples of 2pi \n',theta_1)
23 printf('%f + integer multiples of 2pi \n',theta_2)

```

Scilab code Exa 6.9 To find the result of basic operations on 2 given complex numbers

```

1 clc,clear
2 //Example 6.9
3 //To find the result of basic operations on 2 given
        complex numbers
4
5 z1 = complex(-2,3)
6 z2 = complex(3,4)
7
8 summ = z1+z2

```

```

9 difference = z1-z2
10 product = z1*z2
11 ratio = z1/z2
12 mag_z1= abs(z1) //modulus of z1
13 mag_z2= abs(z2)//modulus of z2
14 //printf('Note: Please go through complex nos scilab
    syntaxes to comprehend this example code\n\n')
15 printf('z1 + z2 = %.0f + %.0f*i\n',real(summ),imag(
    summ))
16 printf('z1 - z2 = %.0f + %.0f*i\n',real(difference),
    imag(difference))
17 printf('z1 * z2 = %.0f + %.0f*i\n',real(product),
    imag(product))
18 printf('z1 / z2 = %f + %f*i\n',real(ratio),imag(
    ratio))
19 printf('|z1|= sqrt(%.0f)= %f \n',mag_z1^2,mag_z1)
20 printf('|z2| = %.0f',mag_z2)

```

Scilab code Exa 6.10 To represent given complex number in trigonometric form

```

1 clc,clear
2 //Example 6.10
3 //To represent given complex number in trigonometric
    form
4
5 z=-2 + -1*i ;//given number
6 x=real(z) ;//real part
7 y=imag(z) ;//imaginary part
8
9 //theta is in third quadrant as x and y are -ve
10 theta=180 + atand(y/x);
11 r=sqrt(x^2+y^2) ;//modulus of z
12 printf('z= %f + i* %f can be written as: \n',real(z)
    ),imag(z))

```

```
13 printf('z = sqrt(%.0f)*(cos(%.1f)+i*sin(%.1f))',r^2,
        theta,theta)
```

Scilab code Exa 6.11 To determine product and ratio of complex numbers using formula

```
1  clc,clear
2  //Example 6.11
3  //To determine product and ratio of complex numbers
   using formula
4
5  //given values
6  z1 = 6*(cosd(70)+ %i*sind(70));
7  z2 = 2*(cosd(31)+ %i*sind(31));
8
9  //arguements of complex numbers
10 theta1=phasemag(z1);
11 theta2=phasemag(z2);
12 //modulus of complex numbers
13 r1=abs(z1);
14 r2=abs(z2);
15 theta_1p2 =theta1 + theta2 ;//theta1 + theta 2
16 theta_1m2 =theta1 - theta2 ;//theta1 - theta 2
17 //according to the formula used in book
18 product = r1*r2*(cosd(theta_1p2)+%i*sind(theta_1p2))
   ;
19 ratio = (r1/r2)*(cosd(theta_1m2)+%i*sind(theta_1m2))
   ;
20
21 printf('z1*z2 = %.0f*(cos(%.0f)+i*sin(%.0f))\n',r1*
        r2,phasemag(product),phasemag(product))
22 printf('z1/z2 = %.0f*(cos(%.0f)+i*sin(%.0f))\n',r1/
        r2,phasemag(ratio),phasemag(ratio))
```

Scilab code Exa 6.12 To find higher powers of complex number using demoiivre theorem

```
1 clc, clear
2 //Example 6.12
3 //To find higher powers of complex number using
   demoiivre theorem
4
5 z= complex(1,1);
6 r= abs(z); //modulus of z
7 theta=phasesmag(z) ; //arguement of z
8 power=10;
9 //using demoiivre formula
10 answer= (r^power)*(cosd(theta*power)+%i*sind(theta*
   power));
11 //printf('(1+i)^10 = (%.0f)*(cos(%.0f)+ i*sin(%.0f))
   ',r^power,theta*power,theta*power);
12 printf(' \n %.0f + %.0f*i ',real(answer),imag(answer))
   ;
13 printf(' \n(OR) \n %.0f*i ',imag(answer));
```

Scilab code Exa 6.13 To determine the cube roots of i

```
1 clc, clear
2 //Example 6.13
3 //To determine the cube roots of i
4
5 z=%i //given complex number
6 //modulii for cuberoots
7 r1=abs(z)^(1/3)
8 r2=abs(z)^(1/3)
9 r3=abs(z)^(1/3)
```

```

10
11 //arguments for cuberoots
12 theta1= (phasemag(z)+360*0)/3
13 theta2= (phasemag(z)+360*1)/3
14 theta3= (phasemag(z)+360*2)/3
15
16 cube_root_1 = r1 *(cosd(theta1)+ %i*sind(theta1))
17 cube_root_2 = r2 *(cosd(theta2)+ %i*sind(theta2))
18 cube_root_3 = r3 *(cosd(theta3)+ %i*sind(theta3))
19
20 printf('cuberoot 1: %f + %f*i\n',real(cube_root_1),
        imag(cube_root_1))
21 printf('cuberoot 2: %f + %f*i\n',real(cube_root_2),
        imag(cube_root_2))
22 printf('cuberoot 3: %f + %f*i\n',real(cube_root_3),
        imag(cube_root_3))

```

Scilab code Exa 6.15 To convert from polar to cartesian coordinates

```

1  clc , clear
2  //Example 6.15
3  //To convert from polar to cartesian coordinates
4
5  //part(a)
6  r=2 ;
7  theta=30 ;
8  x=r*cosd(theta) ;
9  y=r*sind(theta) ;
10 printf(' (a) (x,y)= (%f,%f)\n',x,y) ;
11
12 //part(b)
13 r=3 ;
14 theta=3*%pi/4 ;
15 x=r*cos(theta) ;
16 y=r*sin(theta) ;

```

```

17 printf(' (b) (x,y)= (%f,%f)\n',x,y) ;
18
19 //part(c)
20 r=-1 ;
21 theta=5*pi/3 ;
22 x=r*cos(theta) ;
23 y=r*sin(theta) ;
24 printf(' (c) (x,y)= (%f,%f) ',x,y) ;

```

Scilab code Exa 6.16 To convert from cartesian to polar coordinates

```

1  clc,clear
2  //Example 6.16
3  //To convert from cartesian to polar coordinates
4
5  //part(a)
6  x=3 ;
7  y=4 ;
8
9  //53.13 is in same quadrant as(3,4)
10 r=sqrt(x^2+y^2) ;
11 theta=atand(y/x) ;
12 printf('PART A\n(r,theta)= %f,%f',r,theta) ;
13 printf('\nOR\n') ;
14 r=-sqrt(x^2+y^2) ;
15 //tan theta is +ve in 3rd quadrant
16 //so 180 + 53.33 is also a permissible value
17 theta=180 + atand(y/x) ;
18 printf('(r,theta)= %f,%f',r,theta) ;
19
20 //part(b)
21 x=-5 ;
22 y=-5 ;
23
24 //225 is in same quadrant as(-5,-5)

```

```

25 //tan theta is +ve in 3rd quadrant
26 r=sqrt(x^2+y^2) ;
27 theta=180+ atand(y/x) ;
28 printf('\n\nPART B\n(r, theta)= %f,%f',r,theta) ;
29 printf('\nOR\n') ;
30 r=-sqrt(x^2+y^2) ;
31 theta= atand(y/x) ;
32 printf('(r, theta)= %f,%f',r,theta) ;

```

Scilab code Exa 6.17 To express an equation in polar coordinates

```

1  clc,clear
2  //Example 6.17
3  //to express an equation in polar coordinates
4
5  RHS=9 ;
6  //Note that LHS is basically an equation of circle
7  //But at any instant , it is numerically same as 9
8  LHS_numerically=RHS ;
9  r=sqrt(LHS_numerically) ;
10
11 printf('The equation in terms of polar coordinates
    is : r =%.0f',r)

```

Scilab code Exa 6.19 To express an equation in polar coordinates

```

1  clc,clear
2  //Example 6.19
3  //to express an equation in polar coordinates
4
5  //Given equation is : y=x
6  y_by_x =1; //ratio of y and x
7  tan_theta = y_by_x;

```

```
8 theta=atand(tan_theta); //azimuth angle
9
10 printf('The given equation in polar coordinates is :
        theta = %.0f degree\n',theta)
11 printf('\nNote: Polar form is same regardless of
        value of r ')
```

Chapter 8

Appendix B

Scilab code Exa 8.1 To plot the function of sin x

```
1 //Example 8.1
2 //To plot the function of sin(x)
3 clear,clc;
4
5 x = linspace(-0,2*%pi,50);
6 y = sin(x) ;
7
8 //For grid, uncomment below line
9 //set(gca(),"grid",[5 5]);
10
11 printf('NOTE:\nTo enable the grid , check the code')
12 plot(x,y,'r');
13 xlabel("$0\le x\le 2*pi$","fontsize",4,"color","red"
14 );
15 ylabel("$y(x)=sin(x)$","fontsize",4,"color","red");
16 title("Example 8.1","color","blue","fontsize",9);
17 legend("sin(x)");
```

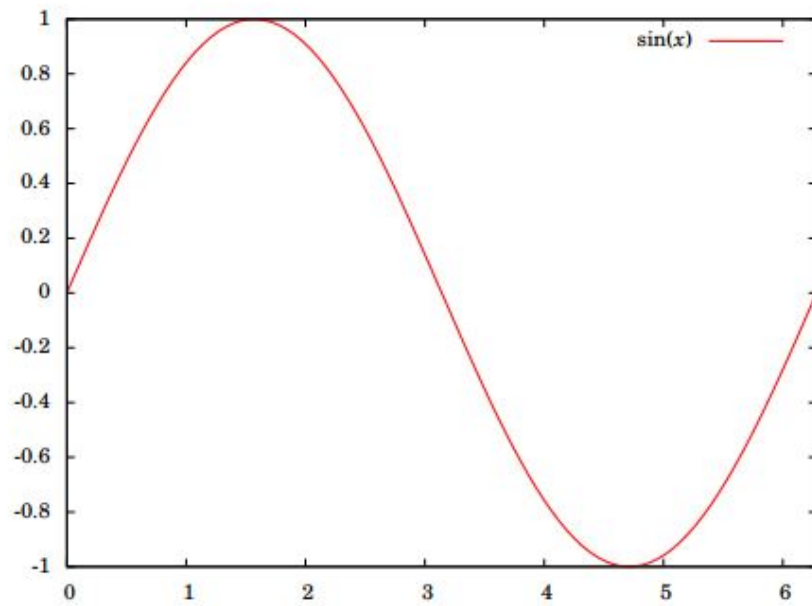


Figure 8.1: To plot the function of $\sin x$

Example 8.1

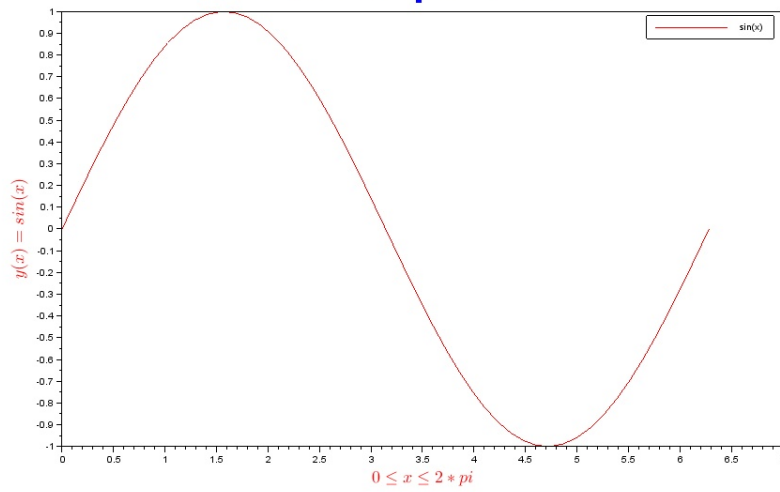


Figure 8.2: To plot the function of $\sin x$