

Scilab Textbook Companion for
Modern Digital And Analog Communication
System
by B. P. Lathi¹

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Book Description

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Scilab numbering policy used in this document and the relation to the above book.

Exa Example (Solved example)

Eqn Equation (Particular equation of the above book)

AP Appendix to Example(Scilab Code that is an Appednix to a particular Example of the above book)

For example, Exa 3.51 means solved example 3.51 of this book. Sec 2.3 means a scilab code whose theory is explained in Section 2.3 of the book.

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Chapter 2

INTRODUCTION TO SIGNALS

Scilab code Exa 2.1 problem1

```
1 clc;  
2 //page no 17  
3 //prob 2.1 b]  
4 //Assuming SI unit for all quantities  
5 // the given signal does not tend to zero as  $t \rightarrow \infty$ .  
   However it is periodic & therefore its power  
   exist. therefore averaging the sq. of the signal  
   over infinitely large interval is similar to  
   averaging it to over one time period  
6 t0=-1;t1=1;  
7 y=integrate('t^2','t',t0,t1);  
8 disp(+'watt',y/2,'power of signal');
```

Scilab code Exa 2.3b problem3b

```
1 // page no.26
```



```

2 //exa no.2.3b
3 t=[-3:.0082:1];
4 m1=(0-1)/(-3-(-1)); //slope for -3<t<-1
5 c1=(0-m1*(-3)); //intercept for pt(-3,0)
6 u(t<=-1)=[(m1*t(t<=-1))+c1]';
7 m2=(1-0)/(-1-1); //slope for -1<t<1
8 c2=(0-m2*1) //intercept for pt(1,0)
9 u(t>-1)=[(m2*t(t>-1))+c2]';
10 subplot(221)
11 plot2d(t,u) //original signal
12 subplot(222)
13 plot2d(2*t,u) //expansion of signal

```

Scilab code Exa 2.4 problem4

```

1 clc;
2 //page27
3 //problem 2.4
4 t=(-5:-1);
5 subplot(221)
6 plot2d(t,(%e)^t/2);
7 xtitle ( " Original signal " , " Time " , "g(t) " );
8 t=-t;
9 subplot(222)
10 plot2d(t,(%e)^-t/2);
11 xtitle ( " Time inverted signal" , " time " , "g(-t)
    " );

```

Scilab code Exa 2.5 problem5

```

1 clc;
2 //Assuming SI units for all quantities
3 //page no 33

```

```

4 //exa 2.5a
5 //approximation of square signal to sine signal with
  minimum energy
6 t=[0:.1:2*%pi];
7 t0=0;t1=2*%pi;
8 y=integrate('(sin(t))^2','t',t0,t1);
9 disp('+joule',y('$'),'energy of sine signal=');
10 //to calculate value of c
11 t2=0;t3=%pi;
12 g=integrate('sin(t)','t',t2,t3);
13 t4=%pi;t5=2*%pi;
14 h=integrate('-sin(t)','t',t4,t5);
15 disp((g($)+h($))/%pi,"value of c=");

```

Scilab code Exa 2.6a problem6a

```

1 clc;
2 //Assuming SI units for all quantities
3 //given signal is x(t)=1
4 //energy of signal x(t)
5 t0=0;t1=5;
6 x=1;
7 y=integrate('x^2','t',t0,t1);
8 disp('+joule',y,'energy of signal x(t)=')
9 //to find correlation coefficient we have to
  calculate the energies of different given signals
10 //1st signal g1(t)=1
11 g1=1;
12 e1=integrate('g1^2','t',t0,t1);
13 disp('+joule',e1,'energy of signal');
14 //correltion coefficient
15 c1=integrate('g1*x','t',t0,t1);
16 disp('+joule',c1/sqrt(y*e1),'correlation coefficient
  =');

```

Scilab code Exa 2.6b problem6b

```
1  clc;  
2  //Assuming SI units for all quantities  
3  //given signal is  $x(t)=1$   
4  //energy of signal  $x(t)$   
5  t0=0;t1=5;  
6  x=1;  
7  y=integrate('x^2','t',t0,t1);  
8  disp(+'joule',y,'energy of signal  $x(t)=$ ');  
9  //to find correlation coefficient we have to  
   calculate the energies of different given signals  
10 g2=.5;  
11 e2=integrate('g2^2','t',t0,t1);  
12 disp(+'joule',e2,'energy of signal');  
13 //correltion coefficient  
14 c2=integrate('g2*x','t',t0,t1);  
15 disp(c2/sqrt(y*e2),'correlation coefficient=');
```

Scilab code Exa 2.6c problem6c

```
1  clc;  
2  //Assuming SI units for all quantities  
3  //given signal is  $x(t)=1$   
4  //energy of signal  $x(t)$   
5  t0=0;t1=5;  
6  x=1;  
7  y=integrate('x^2','t',t0,t1);  
8  disp(+'joule',y,'energy of signal  $x(t)=$ ');  
9  //to find correlation coefficient we have to  
   calculate the energies of different given signals  
10 g3=-1;
```

```

11 e3=integrate('g3^2','t',t0,t1);
12 disp('+joule',e3,'energy of signal');
13 //correltion coefficient
14 c3=integrate('g3*x','t',t0,t1);
15 disp(c3/sqrt(y*e3),'correlation coefficient=');

```

Scilab code Exa 2.6d problem6d

```

1 clc;
2 //Assuming SI units for all quantities
3 //given signal is x(t)=1
4 //energy of signal x(t)
5 t0=0;t1=5;
6 x=1;
7 y=integrate('x^2','t',t0,t1);
8 disp('+joule',y,'energy of signal x(t)=');
9 //to find correlation coefficient we have to
   calculate the energies of different given signals
10 e4=integrate('((%e)^(-t/5))^2','t',t0,t1);
11 disp('+joule',e4('$'),'energy of signal');
12 //correltion coefficient
13 c4=integrate('((%e)^(-t/5))*x','t',t0,t1);
14 disp(c4($)/sqrt(y*e4),'correlation coefficient=');

```

Scilab code Exa 2.6e problem2e

```

1 clc;
2 //Assuming SI units for all quantities
3 //given signal is x(t)=1
4 //energy of signal x(t)
5 t0=0;t1=5;
6 x=1;
7 y=integrate('x^2','t',t0,t1);

```

```

8 disp(+ 'joule ',y, 'energy of signal x(t)=');
9 //to find correlation coefficient we have to
  calculate the energies of different given signals
10 e5=integrate('((%e)^(-t))^2','t',t0,t1);
11 disp(+ 'joule ',e5, 'energy of signal');
12 //correltion coefficient
13 c5=integrate('((%e)^(-t))*x','t',t0,t1);
14 disp(c5/sqrt(y*e5), 'correlation coefficient=');

```

Scilab code Exa 2.6f problem6f

```

1 clc;
2 //Assuming SI units for all quantities
3 //given signal is x(t)=1
4 //energy of signal x(t)
5 t0=0;t1=5;
6 x=1;
7 y=integrate('x^2','t',t0,t1);
8 disp(+ 'joule ',y, 'energy of signal x(t)=');
9 //to find correlation coefficient we have to
  calculate the energies of different given signals
10 e6=integrate('(sin(2*%pi*t))^2','t',t0,t1);
11 disp(+ 'joule ',e6, 'energy of signal');
12 //correltion coefficient
13 c6=integrate('((sin(2*%pi*t))^2)*x','t',t0,t1);
14 disp(c6/sqrt(y*e6), 'correlation coefficient=');

```

Chapter 3

ANALYSIS AND TRANSMISSION OF SIGNALS

Scilab code Exa 3.1 problem1

```
1 clc;  
2 //page no 75  
3 //prob 3.1  
4 // given signal is  $x(t) = e^{-at} * u(t)$   
5 //unity function  $u(t)=1$  for 0 to infinity  
6 //therefore  
7 x=1;  
8 //here we consider 'infinity' value as 10 and the  
   value of 'a' is 1  
9 t= 0:1:10;  
10 a=1; // a >0  
11 z=((%e)^(-a*t) * x);  
12 y=fft(z);  
13 disp(y, 'fourier transform of x(t)=');
```

Scilab code Exa 3.2 problem2

```
1 clc ;
2 //page no 81
3 //prob 3.2
4 //given signal is  $x(t) = \text{rect}(t/T)$ 
5 // $\text{rect}(t/T) = 1$  for  $|t| < T/2$  and
6 //  $= 0$  for  $|t| > T/2$ 
7 // therefore we have to find out fourier transform
  of  $x(t) = 1$  for  $|t| < T/2$  thus ,
8 x=1;
9 T= 200; // consider
10 t= -T/2 : 1 : T/2; //range for fourer transform
11 y=fft(x);
12 disp(y, 'fourier transform of  $x(t)=$ ');
```

Scilab code Exa 3.3 problem3

```
1 clc ;
2 //page no 82
3 //prob 3.3
4 // given signal is  $x(t) = \text{unit impulse } d(t)$ 
5 //it is defined as  $d(t) = 1$  for  $t=0$ 
6 //therefore
7 x=1;
8 y=fft(x);
9 disp(y, 'fourier transform of  $x(t)=$ ');
```

Scilab code Exa 3.7 problem7

```
1 clc ;
2 //page 84
3 // problem 3.7
```

```
4 t=-10:1:10;
5 y=sign(t);
6 g=fft(y);
7 disp(g,"fourier transform of signum funcion is");
```

Chapter 4

AMPLITUDE MODULATION

Scilab code Exa 4.5 problem5

```
1  clc ;
2  //page 166
3  //problem 4.5
4  // we have given 1)u=.5 and 2)u=.3
5  // efficiency n is calculated by using formula  $n = (u^2) / (2+u^2) * 100$  %
6  //for u=0.5
7  u1=0.5;
8  n1= (u1^2) / (2+u1^2) *100 ;
9  disp(n1,'efficiency in % is ');
10 // Hence only 11.1111% of total power is in
    sidebands.
11 //for u=0.3
12 u2=0.3;
13 n2= (u2^2) / (2+u2^2) *100;
14 disp(n2,'efficiency in % is ');
15 // Hence only 4.3062% of the total power is the
    useful power (power in sidebands)
```

Chapter 5

ANGLE MODULATION

Scilab code Exa 5.1 problem1

```
1  clc;
2  //page 212
3  //problem 5.1
4  // The values of constants Kf and Kp are given as Kf
   = 2*pi*10^5 and Kp=10*pi, and carrier frequency
   fc=100MHz
5
6  // For FM :
7  // fi= fc + Kf*m(t)/2*pi
8  // Minimum value of m(t) = -1 and Maximum value of m
   (t)= +1
9  Kf= 2*pi*10^5 ; Kp=10*pi;
10 fc=100*10^6 ; // in Hz
11 Mmin = -1 ; Mmax=1;
12 fimin1= fc + Kf*Mmin/(2*pi);
13 disp(+ 'MHz',fimin1/10^6, 'Minimum frequency in MHz is
   ');
14 fimax1= fc + Kf*Mmax/(2*pi);
15 disp(+ 'MHz',fimax1/10^6, 'Maximum frequency in MHz is
   ');
16
```

```

17 //For PM :
18 //fi= fc + Kp*m(t)'/2*pi
19 // Minimum value of m(t)' = -20,000 and Maximum
    value of m(t) '= +20,000
20 Mmin1=-20000 ; Mmax1=20000;
21 fimin2= fc + Kp*Mmin1/(2*%pi);
22 disp(+ 'MHz',fimin2/10^6, 'Minimum frequency in MHz is
    ');
23 fimax2= fc + Kp*Mmax1/(2*%pi);
24 disp(+ 'MHz',fimax2/10^6, 'Maximum frequency in MHz is
    ');
25
26 // Since m(t) is increases and decreases linearly
    with time, the instantaneous frequency increases
    linearly from fimin to fimax

```

Scilab code Exa 5.2 problem2

```

1 clc;
2 //page 213
3 //problem 5.2
4 // The values of constnts Kf and Kp are given as Kf
    = 2*pi*10^5 and Kp=pi/2, and carrier frequency fc
    =100MHz
5 // For FM :
6 //fi= fc + Kf*m(t)/2*pi
7 // Minimum value of m(t) = -1 and Maximum value of m
    (t)= +1
8 Kf= 2*%pi*10^5 ; Kp=%pi/2;
9 fc=100*10^6 ;// in Hz
10 Mmin = -1 ; Mmax=1;
11 fimin1= fc + Kf*Mmin/(2*%pi);
12 disp(+ 'MHz',fimin1/10^6, 'Minimum frequency in MHz is
    ');
13 fimax1= fc + Kf*Mmax/(2*%pi);

```

```

14 disp(+ 'MHz',fimax1/10^6, 'Maximum frequency in MHz is
    ');
15 // Since m(t) is increases and decreases linearly
    with time, the instantaneous frequency increases
    linearly from fimin to fimax

```

Scilab code Exa 5.3a problem3a

```

1  clc;
2  //page 222
3  //problem 5.3.a
4  // refer fig from page no. 212 Fig.5.4a
5  // The values of constnts Kf and Kp are given as Kf
    = 2*pi*10^5 and Kp=5*pi .
6  // Here we are assuming the Bandwidth B of m(t) as
    the frequency of the third harmonic, i.e.
    3(10^4/2)Hz= 15kHz
7  B=15; // in kHz
8  // For FM:
9  // Here peak amplitude of m(t) is mp=1
10 mp=1;
11 // df=kf*mp/2*pi
12 Kf= 2*pi*10^5; Kp=5*pi;
13 df= (Kf*mp)/(2*pi); // in Hz
14 df=df/10^3; // in KHz
15 Bfm=2*(df+B);
16 disp(+ 'KHz',Bfm, 'Bfm in kHz is ');
17 // For PM:
18 //Here peak amplitude of m(t)' is mp=20000
19 mp=20000;
20 // df=kp*mp/2*pi
21 df= (Kp*mp)/(2*pi); // in Hz
22 df=df/10^3; // in KHz
23 Bpm=2*(df+B);
24 disp(+ 'KHz',Bpm, 'Bpm in kHz is ');

```

Scilab code Exa 5.3b problem3b

```
1  clc;
2  //page 222
3  //problem 5.3.b
4  // The values of constants Kf and Kp are given as Kf
   = 2*pi*10^5 and Kp=5*pi .
5  // Here we are assuming the Bandwidth B of m(t) as
   the frequency of the third harmonic, i.e.
   3(10^4/2)Hz= 15kHz
6  B=15;// in kHz
7  // For FM:
8  // Here peak amplitude of m(t) is doubled ,mp=2
9  mp=2;
10 // df=kf*mp/2*pi
11 Kf= 2*pi*10^5; Kp=5*pi;
12 df= (Kf*mp)/(2*pi);// in Hz
13 df=df/10^3;// in KHz
14 Bfm=2*(df+B);
15 disp(+'KHz',Bfm,'Bfm in kHz is ');
16 // For PM:
17 //Here peak amplitude of m(t)' is doubled mp=40000
18 mp=40000;
19 // df=kp*mp/2*pi
20 df= (Kp*mp)/(2*pi);// in Hz
21 df=df/10^3;// in KHz
22 Bpm=2*(df+B);
23 disp(+'KHz',Bpm,'Bpm in kHz is ');
24 // doubling the signal amplitude roughly doubles the
   bandwidth of both FM and PM waveform
```

Scilab code Exa 5.4 problem4

```

1  clc;
2  //page 224
3  //problem 5.4
4  // Repeat example 5.3 with m(t) expanded by a factor
   of 2 i.e. if the period of m(t) is  $4 \times 10^{-4}$ 
5  // The values of constants Kf and Kp are given as Kf
   =  $2 \times \pi \times 10^5$  and  $Kp = 5 \times \pi$  .
6  // we know that time expansion by a factor 2 reduces
   the signal spectrum width by a factor 2
7  // Therefore bandwidth is half the previous
   bandwidth
8  B=7.5; // in KHz
9  // For FM:
10 // Time expansion does not affect the peak
   amplitude so that mp=1.
11 mp=1;
12 // df=kf*mp/2*pi
13 Kf= 2*%pi*10^5; Kp=5*%pi;
14 df= (Kf*mp)/(2*%pi); // in Hz
15 df=df/10^3; // in KHz
16 Bfm=2*(df+B);
17 disp(+'KHz',Bfm,'Bfm in kHz is ');
18 // For PM:
19 //mp is halved i.e. mp=10000
20 mp=10000;
21 // df=kp*mp/2*pi
22 df= (Kp*mp)/(2*%pi); // in Hz
23 df=df/10^3; // in KHz
24 Bpm=2*(df+B);
25 disp(+'KHz',Bpm,'Bpm in kHz is ');
26 // Time expansion of m(t) has very little effect on
   the FM bandwidth, but it halves the PM bandwidth

```

Scilab code Exa 5.5 problem5

```

1  clc;
2  //Assuming SI unit for all quantities
3  //page 225
4  //problem 5.5
5  // An angle modulated signal with carrier frequency
    $w_c = 2\pi \cdot 10^5$  is described by the equation  $Q_{em} = 10 \cos(\theta(t))$  where  $\theta(t) = w_c t + 5 \sin 3000t + 10 \sin 2000\pi t$ 
6  B=2000*%pi/(2*%pi); //signal bandwidth is the highest
   frequency in m(t)
7  Ac=10; //carrier amplitude
8  P=Ac^2/2; // carrier power
9  disp(+'watt',P,'a') The carrier power is ');
10 // to find frequency derivative df, we find
   instantaneous freq. w as
11 //  $w_i = d/dt(\theta(t)) = w_c + 15000 \cos 3000t + 20000\pi \cos 2000\pi$ 
   *t;
12 // The carrier derivative is  $15000 \cos 3000t + 20000\pi \cos 2000\pi t$ . The two sinusoids will add in phase
   at some point and the maximum value of the
   expression is  $dW = 15000 + 20000\pi$ 
13 dW=15000+20000*%pi;
14 df=dW/(2*%pi);
15 disp(+'Hz',df,'b') The frequency deviation in Hz is ');
   ');
16 // The deviation ratio B1 is given as
17 B1=df/B;
18 disp(B1,'c') The deviation ratio is ');
19 //The phase deviation is the maximum value of the
   angle  $\theta(t)$  and is given by d@
20 d=5+10;
21 disp(+'rad',d,'d')The phase deviation in rad is ');
22 Bem=2*(df+B);
23 disp(+'Hz',Bem,'e')Bandwidth is ');

```

Chapter 6

SAMPLING AND PULSE CODE MODULATION

Scilab code Exa 6.2 problem2

```
1  clc;
2  // page no 271
3  // prob no. 6.2
4  fm=input("Enter the band limited freq in hertz = ");
5  Rn=2*fm; // Nyquist sampling rate
6  Ra=Rn*(4/3); // actual Nyquist sampling rate
7  // here the maximum quantization error(E) is 0.5% of
   the peak amplitude mp. Hence,  $E=mp/L=0.5*mp/100*$ 
   L
8  mp=1; //we assume peak amplitude is unity
9  L=(mp*100)/(0.5*mp);
10 for (i=0:10)
11     j=2^i;
12     if(j>=L)
13         L1=j;
14         break;
15     end
16 end
17 n=log2(L1); // bits per sample
```



```

18 c=n*Ra; // total no of bits transmitted
19 // Beause we can transmit up to 2bits/per hertz of
    bandwidth,we require minimum transmission
    bandwidth Bt=c/2
20 Bt=c/2;
21 disp(+'Hz ',Bt,"minimum transmission bandwidth in
    hertz = ");
22 s=input("enter the no of signal to be multiplexed =
    ");
23 Cm=s*c; //total no of bits of 's' signal
24 c1=Cm/2; // minimum transmission bandwidth
25 disp(+'Hz ',c1,"minimum transmission bandwidth in
    hertz = ")

```

Scilab code Exa 6.3 problem3

```

1  clc;
2  //page no 273
3  // prob no 6.3
4  // from the expresion given on the page no 272; (So/
    No)=(a+6n) dB where a=10log[3/[ln(1+u)]^2]
5  //check the ollowing code for L=64 and L=256
6  L=input("enter the value of L = ");
7  B=input("enter the bandwidth of signal in hertz = ")
    ;
8  n=log2(L);
9  Bt=n*B;
10 u=100; //given
11 a=10*log10(3/[log(1+u)]^2);
12 SNR=(a+(6*n));
13 disp(SNR,"SNR ratio is = ");
14 // Here the SNR ratio for the two cases are found
    out. The difference between the two SNRs is 12dB
    which is the ratio of 16. Thus the SNR for L=256
    is 16 times the SNR for L=64. The former requires

```

just about 33% more bandwidth compared to the
later.

Chapter 7

PRINCIPLES OF DIGITAL DATA TRANSMISSION

Scilab code Exa 7.1 problem1

```
1 clc;  
2 // page no 314  
3 // prob no 7.1  
4 //The transmission bandwidth is given by the  
    equation  $B_t=(1+r)R_b/2$  and hence transmission rate  
    is given by  $R_b=2B_t/(1+r)$ ; where  $r$ =roll-off factor  
    and  $0 \leq r \leq 1$ . Since 'r' can take value in between  
    0 and 1, bandwidth varies from  $2B_t$  to  $B_t$ .  
5  $B_t=32000$ ;  $r=1$ ; //assume values of  $B_t$  and  $r$   
6  $R_b=(2*B_t)/(1+r)$ ;  
7 disp( $R_b$ , "transmission rate"); //  $R_b=B_t$  for  $r=1$ 
```

Scilab code Exa 7.3 problem3

```
1 clc;  
2 //page no 326
```

```

3 //prob no 7.3
4 // problem fig. is ggiven on page no 324. Referring
   the fig. we are given the values of a0,a1,a-1,a-2
5 a=1;b=-0.3;c=0.1;d=-0.2;e=0.05;
6 //design a three-tap (N=1) equalizer by substituting
   these values into eq no 7.45 of the page no 325
7 A=[0;1;0];
8 B=[a d e;b a d;c b a];
9 c=inv(B)*A;// As, A=B*C Hence c is obtained as given
10 disp(c);// values of C-1,C0,C1 are obtained

```

Scilab code Exa 7.4 problem4

```

1 clc;
2 // page no 334
3 //PROB NO 7.4 a) Find detection error probability
4 //Given: Ap=1mV, 6n=192.3uV
5 // The formula for polar case is given by Ap/6n
6 Ap=1;sigma_n=192.3;
7 x=Ap/sigma_n;//here we have to find the value of P(e
   )=Q(x) from the table10.2 given on page no. 454
8 disp(x);
9 Q1=(0.9964)*10^(-7);
10 disp(Q1,"error probability = ");//this is nearly
   equal to zero
11
12 //PROB NO 7.4 b) Find detection error probability.
13 //In this case, only half the bits are transmitted
   by no pulse, there are, on the average, only half
   as many pulses in the on-off case(compared to
   the polar).
14 //To maintain the same power,we need to double the
   energy of each pulse in the on-off or the
   bipolar case(compared to the polar).
15 //Now, doubling the pulse energy is accomplished by

```

```

    multiplying the pulse by sqrt(2).
16 //Thus, for on-off Ap is sqrt(2) times the Ap in the
    polar case ,that is , Ap=sqrt(2)*10^-3
17 x=Ap/2*sigma_n;//here we have to find the value of P
    (e)=Q(x) from the table10.2 given on page no. 454
18 disp(x);
19 Q2=(1.166)*10^-4;
20 disp(Q2,"error probability = ");
21 //for a given power , the Ap for both the on-off and
    the bipolar cases are identical. Hence P(e)=1.5
    Q(x);
22 Q3=1.5*Q2;
23 disp(Q3,"error probability = ");

```

Chapter 8

EMERGING DIGITAL COMMUNICATIONS TECHNOLOGIES

Scilab code Exa 8.3 problem3

```
1  clc ;
2  // page no. 367
3  //prob no. 8.3
4  //since both the plots can be out of synchronization
   by as much as 6 parts (bits)in  $10^{13}$  , we have
5  // timing error bits per second can be calculated as
   -
6  //error in synchronization is given as
7  e=6/( $10^{13}$ ); //timing error bits per transmitted bits
8  //bit rate is given as
9  r =1544000 ; // in bits/sec
10 //timing error bits per second ,Te is given as
11 Te=e*r;
12 S=1/Te; // seconds per timing error bits
13 H=S/3600; // hours per timing error bits
14 //since a synchronization error can occur whenever
   the network is out of synchronization by 1/5 bits
```

, the time between resynchronizing is given as

```
15 T=H/5;  
16 disp(+ 'Hr ',T,"No. of hours for resynchronizing");
```

Chapter 10

Introduction to Theory of Probability

Scilab code Exa 10.1 problem1

```
1 //page no 437
2 //prob 10.1
3 // referred to fig 10.1 on the page no. 435
4 // the occurance of each outcome is assumed to be
   equal.
5 n=input("number of outcomes= ");
6 p=1/n;
7 disp(p,"probability of each outcome=");
```

Scilab code Exa 10.3 problem3

```
1 // page no 438
2 //problem no 10.3
3 clc;
4 m=input("enter the number of faces = ");// m = 6
5 n=input("enter the number of dice = ");// n = 2
```



```

6 l=m^n ;// j is total number of outcomes = 36
7 a=input("enter the number which is to be obtained as
    the sum of dice = ") // a=7
8 c=0 ; // counter value for favorable outcome
9 for i=1:6
10     for j=1:6
11         if(i+j==a)
12             c=c+1;
13         else
14             continue
15         end
16     end
17 end
18 p=c/l;
19 disp(p,"probability = ");

```

Scilab code Exa 10.4 problem4

```

1 // page no 438
2 //problem no 10.4
3 clc;
4 m=input("enter the number of faces = ");// m = 2
5 n=input("enter the number of tosses = ");// n = 4
6 l=m^n ;// j is total number of outcomes = 16
7 a=input(" enter exact no of heads = "); // to obtain
    exactly 'a' heads
8 p=gamma (n+1)/(gamma(n+1-a) * gamma (a+1));// to
    find combination
9 disp(p/l,"probability = ");

```

Scilab code Exa 10.5 problem5

```

1 // page no 440

```

```

2 //problem no 10.5
3 clc;
4 a=52; // total no of cards in a deck
5 b=input ("enter the no of cards to be drawn = ");
6 pA1= b/a;// probability of getting first red ace =
   pA1
7 //the cards are drawn in succession without
   replacement, therefore the probability that the 2
   nd card will be the red ace = pA2
8 pA2=1/(a-1);
9 disp(p= pA1*pA2,"total probability = ");

```

Scilab code Exa 10.6 problem6

```

1 // page no 441
2 // prob no 10.6
3 // This problem is based on Bernoulli Trials formula
   which is  $P(k \text{ successes in } n \text{ trials}) = n! * p^k * (1-p)^{(n-k)} / k! * (n-k)!$ 
4 // hence the probability of finding 2 digits wrong
   in a sequence of 8 digits is
5 clc;
6 k= input ("no. of successes =");
7 p= input ("probability of success =");
8 n=input (" no. of trials =");
9 A=gamma (n+1)* (p^k)*((1-p)^(n-k))/(gamma(k)*gamma(n
   +1-k));
10 disp(A,"probability =");

```

Scilab code Exa 10.9 problem9

```

1 // page no 446
2 //problem no 10.9

```

```

3  clc;
4  m=input("enter the number of faces = ");
5  n=input("enter the number of dice = ");
6  l=m^n ;// j is total number of outcomes
7  a=input("enter the number which is to be obtained as
           the sum of dice = ") // a is varied from 2 to
           12
8  c=0 ; // counter value for favorable outcome
9  for i=1:6
10     for j=1:6
11         if(i+j==a)
12             c=c+1;
13         else
14             continue
15         end
16     end
17 end
18 p=c/l;
19 disp(p,"probability = ");

```

Scilab code Exa 10.10 problem10

```

1  // page no 447
2  //prob no 10.10
3  clc;
4  Pe= input ("enter error probability = ");
5  Q= input("enter the probability of transmitting 1 =
           ");//Hence probability of transmitting zero is 1-
           Q = P
6  P=1-Q;
7  Px(1)=Q;
8  Px0=P;
9  // If x and y are transmitted digit and received
           digit then for BSC  $P(y=0/x=1) = P(y=1/x=0) = Pe$  ,
            $P(y=0/x=10) = P(y=1/x=1) = 1-Pe$ 

```

```

10 // to find the probability of receiving 1 is  $P_y(1) =$ 
     $P_x(0)*P(y=1/x=0) + P_x(1)*P(y=1/x=1)$ 
11  $P_y(1) = ((1-Q)*Pe) + (Q*(1-Pe));$ 
12 disp(Py(1), "Py(1)");
13  $P_{y0} = ((1-Q)*(1-Pe)) + (Q*Pe)$ 
14 disp(Py0, "Py0");

```

Scilab code Exa 10.11 problem11

```

1 //page no 448
2 //prob 10.11
3 clc;
4  $P_{x0} = .4$  ,  $P_{x1} = .6$  ,  $PE0 = 10^{-6}$  ,  $PE1 = 10^{-4}$  ;// given
5  $PE = (P_{x0}*PE0) + (P_{x1}*PE1)$  // formula for probability
    of error
6 disp(PE, "probability of error = ");

```

Scilab code Exa 10.20 problem20

```

1 //page no 472
2 //prob no 10.20
3 //Gaussian PDF:  $Q(x) = \frac{e^{-(x^2)/2}}{x*\sqrt{2*\pi}}$ 
4 clc;
5  $x = \text{input}(\text{"input for the function Q = "});$ 
6  $Q(x) = \frac{e^{-((x^2)/2)}}{x*\sqrt{2*\pi}};$ 
7  $P = 1 - (2*Q(x));$ 
8 disp(P); // P gives the width or spread of Gaussian
    PDF

```

Scilab code Exa 10.21 problem21

```

1 // page no 479
2 //prob no 10.21
3 // formula for estimate error E is  $E = mk^{\wedge} - mk = a1$ 
   *  $mk-1 + a2 * mk-2 - mk$ 
4 //given: various values of correlation  $(mk*mk)^{\wedge} = (m$ 
    $^2)^{\wedge}$ ,  $(mk*mk-1)^{\wedge} = .825 * (m^2)^{\wedge}$ ,  $(mk*mk-2)^{\wedge} = .562 * (m$ 
    $^2)^{\wedge}$ ,  $(mk*mk-3)^{\wedge} = .825 * (m^2)^{\wedge}$ ,  $R02 = .562 * (m^2)^{\wedge}$ ,  $a1$ 
    $= 1.1314$ ,  $a2 = -0.3714$ 
5 // mean square error is given by  $I = (E^2)^{\wedge} = [1 - ((.825 *$ 
    $a1) + (.562 * a2)) * (m^2)^{\wedge} = .2753 * (m^2)^{\wedge}$ 
6 clc;
7 m=1;
8 I = .2753 * (m^2)^{\wedge};
9 S = 10 * log ((m^2)^{\wedge} / I);
10 disp(+ 'dB', S, "SNR improvement = ");

```

Chapter 11

RANDOM PROCESSES

Scilab code Exa 11.2 Example 2 of chapter 11

```
1 //page 500
2 //example 11.2 (assuming SI units)
3 //given signal is  $S_x=(N/2)*\text{rect}(w/4(\%pi)B)$ 
4 clc;
5 N=1;B=1;
6 T=input("enter the value of T");
7 Rx=(N*B)*(sinc(2*(%pi)*B*T));
8 disp(+'Watt',Rx,"mean square value of the signal is"
    );
```

Scilab code Exa 11.3 Example 3 of chapter 11

```
1 //page 501
2 // example 11.3(Assuming SI units)
3 // autocorrelation function of given signal is  $A^2/2$ 
   *  $\cos(wct)$ 
4 clc;
5 A=2;
```

```
6 wct=input("enter the value of wct");
7 Rx=((A^2)/2)* cos(wct);
8 disp('Watt',Rx,"mean square value of the process is
      ");
```

Scilab code Exa 11.7 Example 7 of chapter 11

```
1 //page 506
2 //example 11.7
3 clc;
4 P1=input("enter prob of symbol 1");
5 P2=input("enter prob of symbol -1");
6 ak=(1)*P1+(-1)*P2;
7 disp(ak,"mean is");
8 Ro=(1^2)*P1+((-1)^2)*P2;
9 disp(Ro,"mean square is");
```

Scilab code Exa 11.8a Example 8a of chapter 11

```
1 //page 507
2 // example 11.8a
3 clc;
4 P1=input("enter prob of symbol 1");
5 P0=input("enter prob of symbol 0");
6 ak=(1)*P1+(0)*P2;
7 disp(ak,"mean is");
8 Ro=(1^2)*P1+((0)^2)*P2;
9 disp(Ro,"mean square is");
```

Scilab code Exa 11.8b Example 8b of chapter 11

```
1 //page 508
2 // example 11.8b
3 // bipolar signalling
4 clc;
5 P0=input("enter prob of symbol 0");
6 P1=input("enter prob of symbol 1");
7 P2=input("enter prob of symbol -1");
8 ak=(0)*P0+(1)*P1+(-1)*P2;
9 disp(ak,"mean is");
10 Ro=(0^2)*P0+(1^2)*P1+((-1)^2)*P2;
11 disp(Ro,"mean square is");
```

Chapter 12

BEHAVIOUR OF ANALOG SYSTEMS IN THE PRESENCE OF NOISE

Scilab code Exa 12.1 problem1

```
1 // page no 536
2 // Example 12.1
3 // Let the received signal be  $km(t)\cos(wct)$  ,
  demodulator input is  $[km(t)+nc(t)]\cos(wct)+[ns(t)$ 
   $\sin(wct)]$ . When this is multiplied by  $2\cos wct$  and
  low pass filtered the output is  $s_0(t)+n_0(t)=km(t)$ 
   $+nc(t)$ .
4 // Hence  $S_o=k^2m^2'$  ,  $N_o=nc^2'$ . But the power of
  the received signal  $km(t)\cos(wct)=1\mu W$ . Hence  $k$ 
   $^2m^2'/2=10^{-6}$ 
5 clc;
6  $S_o=2*10^{-6}$ ;
7 // to compute  $nc$ :  $(nc^2)'=(n^2)'=x$ 
8  $t_0=496000$ ;  $t_1=504000$  ;
9  $a=10^6 * \%pi$ ;
10  $y=\text{integrate} ('1/((t^2)+(a^2))'$ , 't',  $t_0, t_1$ );
11 // to compute output SNR
```

```

12 SNR=So/y;
13 val=(10*(log (SNR)));
14 disp(+ 'dB',val,"output SNR = ");

```

Scilab code Exa 12.2 find gamma threshold

```

1 //page 540
2 //problem 12.2
3 //as  $E_n = \sqrt{nc^2 + ns^2}$ , where both  $nc$  and  $ns$  are
   gaussian with variance  $6n^2$ , according to the
   following eqn  $P(E_n \geq A) = \int (En/6n^2) * e^{(-En
   ^2/2*6n^2)} dEn$ ;
4 // the value of this integral is the probability of
   which is 0.01
5 //hence  $e^{(-A^2/2*6n^2)} = 0.01$ 
6 //let  $g = A^2/(2*6n^2)$ ;
7 clc;
8  $g = -(\log(0.01)/\log(\%e))$ ;
9 // the variance  $6n^2$  of the bandpass noise of PSD  $N$ 
   /2 and the bandwidth  $2B$  is  $2NB$ . Hence at the onset
   of the threshold
10 // therefore  $A^2/(2*6n^2) = A^2/(4NB) = g$ 
11 //for tone modulation
12 //  $S_i = A^2 + m'^2/2$ ;
13 //  $S_i = 3*A^2/4$ ;
14  $gma\_th = 3*(g)$ ; //  $gma\_th = S_i/NB = 3*A^2/(4NB)$ ;
15 disp(gma_th, 'gamma threshold');

```

Scilab code Exa 12.3 find output SNR

```

1 //page 547
2 //problem 12.3
3 // for a gaussian  $m(t)$ ,  $mp$  will be assumed as  $36m$ 

```

```

4  clc;
5  Sg=3; //assumed
6  Mbar=(Sg^2);
7  MP=((3*Sg)^2);
8  B=0.2; //ASSUMED
9  gma=0.4; //assumed
10 SNR=3*B^2*(Mbar/MP)*gma;
11 disp(SNR, 'SIGNAL TO NOISE RATIO IS ');

```

Scilab code Exa 12.4 prove the given expression

```

1  //page 550
2  //problem 12.4
3  clc;
4  t0=-5;t1=5;
5  y=integrate('t^2','t',t0,t1);
6  f=integrate('1','t',t0,t1);
7  Bm=y/f;
8  disp(Bm, 'value of Bm is ');

```

Scilab code Exa 12.5 prove the given expression

```

1  //page 550
2  //problem 12.5
3  //  $S_m(w)=k*e^{(-w^2/26^2)}$  this is given
4  // let us the assume the value of constant  $6^2/4(\pi^2) =3$ 
5  // thus the variance can be calculated as
6  clc;
7  f0=0;f1=15;
8  y=integrate('(f^2)*(%e^{-(f^2)/6})','f',f0,f1);
9  g=integrate('%e^{-(f^2)/6}','f',f0,f1);
10 v=y/g;

```

```
11 disp(v, 'Bm2');
```

Scilab code Exa 12.6 show that PM is superior to FM by factor of 3

```
1 //page 552
2 //prob 12.6
3 //for the same transmission bandwidth variance of PM
  and FM systems is same
4 //hence the ratio of SNR of PM to FM is B^2/(3Bm'^2)
5 //assuming 6=1
6 clc;
7 B=3/(2*%pi); //because W=2*%pi*B
8 //variance is Bm2
9 f0=0; f1=15;
10 y=integrate('(f^2)*(%e^(-(f^2)*2*(%pi^2)))', 'f', f0,
  f1);
11 g=integrate('%e^(-(f^2)*2*(%pi^2))', 'f', f0, f1);
12 Bm2=y/g;
13 l=(B^2)/(3*(Bm2));
14 disp(l, 'factor of superiority of PM over FM');
```

Scilab code Exa 12.7 problem7

```
1 // page no 555
2 // Example 12.7
3 clc;
4 B=4; SNR=20.5; // given
5 r=20*(B+1); //as B=4
6 //output SNR is given as So/No=3*B^2*r*(m^2'/mp^2)
7 m=4; // m=mp/6m is given
8 SNRt=3*(B^2)*r*(1/m)^2;
9 disp(SNRt, "threshold SNR = ");
10 // to calculate output SNR in dB
```

```

11 SNRdB=20*log(SNR);
12 disp('dB',SNRdB," Threshold SNR in dB = ");
13 if 20.5< SNRdB
14     disp("system is in threshold")
15 else
16     disp('system is not in threshold");
17 end

```

Scilab code Exa 12.8 determine output SNR

```

1 //page 561
2 //prob 12.8
3 //for a gaussian signal,mp=infinity(∞),but we may
  assume 36 loading,thus mp=3*6,
4 clc;
5 Sgm=3;
6 m2=(Sgm^2);
7 mp2=((3*Sgm)^2);
8 y=(m2)/(mp2);
9 // to calculate SNR,we have  $SNR=3(2^n)*((m^2)/(mp^2))$ 
10 n=8;//given
11 l=3*(2^(2*n))*y;//by formula
12 disp(1,'SNR is equal to');
13 disp('dB',(10*(log10(l))), 'SNR in dB');

```

Scilab code Exa 12.10 find output SNR

```

1 //page 567
2 //prob 12.10
3 // to calculate |m|
4 clc;
5 m0=0;m1=50;

```

```

6 m=integrate(' (m*(%e^-((m^2)/2))) ', 'm', m0, m1); //
   assuming 6m=1
7 disp((sqrt(2/%pi)*m), 'value of |m| ');

```

Scilab code Exa 12.11 find output SNR

```

1 //page 569
2 //prob 12.11
3 a=1400*%pi; //given
4 clc;
5 c=1; //assumed
6 w0=0; w1=8000*%pi;
7 S=integrate(' 1/((w^2)+(a^2)) ', 'w', w0, w1);
8 So=S/%pi;
9 disp(So, 'transmitted power'); //assuming G=1, hence St
   =So
10 //assuming N=1
11 No=4000; //because No=N*B
12 SNR=So/No;
13 disp(SNR, 'SNR without pre-emphasis and de-emphasis')
   ;
14 S=integrate(' 1/(sqrt((w^2)+(a^2))) ', 'w', w0, w1);
15 disp(S, 'S is ');
16 SNRo=(10^-8)*4*(%pi^2)/(2*(S^2));
17 disp(SNRo, 'SNR at the output is ');
18 disp((SNRo/SNR), 'Improvement factor in SNR with pre-
   emphasis and de-emphasis ');

```

Chapter 13

BEHAVIOUR OF DIGITAL COMMUNICATION SYSTEMS IN THE PRESENCE OF NOISE

Scilab code Exa 13.1 problem1

```
1 // page no 620
2 // prob no 13.1
3 //Determinaion of the transmission bandwidth and the
  signal power required at the receiver input for
  i) Binary ii) 16-ary ASK iii) 16-ary PSK
4 //given  $R_b=2.08 \times 10^6$ ,  $P_b \leq 10^{-6}$ 
5
6 //i) for BINARY we have to consider  $P_b=P_e=10^{-6}=Q(\sqrt{2E_b/N})$ . This yields  $E_b/N=11.35$ .
7 //Signal power is given by  $S_i=E_b \times R_b=11.35 \times N \times R_b$ 
8 clc;
9  $N=2 \times 10^{-8}$ ; //for binary. Channel noise PSD= $10^{-8}$ 
10  $R_b=2.08 \times 10^6$ ;
11  $S_i1=11.35 \times N \times R_b$ ;
12 disp(+ 'Watts',  $S_i1$ , "signal power required at the
```

```

    receiver = ");
13 Bt1=Rb;// Bandwidth for baseband pulses
14 disp('Hertz',Bt1," Bandwidth is = ");
15
16 //ii) for 16-ary ASK we have to consider  $P_b=10^{-6}=P_{em}$ 
    /log2(16)
17 // therefore  $P_{em}$  is given as  $P_{em}=P_b*\log_2(16)$ 
18  $P_b=10^{-6}$ ;
19  $P_{em}=P_b*\log_2(16)$ ;
20 // 'Pem' is also given as  $P_{em}=2(M-1/M)*Q*\sqrt{6E_b*}$ 
    log2(16)/(N(M2-1))
21 M=16;// for 16-array ASK
22 // By using above formula for 'Pem' , we can
    calculate the value of  $E_b$ , which is come out to be
    equal to  $0.499*10^{-5}$ ;
23  $E_b=0.499*10^{-5}$ ;// if the M-ary pulse rate is  $R_M=R_b$ 
    /4 then
24  $R_M=R_b/4$ ;
25  $S_i2=E_b*(\log_2(M))*R_M$ ;
26 disp('Watts',Si2," signal power required at the
    receiver= ");
27 Bt2= $R_M$ ;//transmission bandwidth
28 disp('Hertz',Bt2," Bandwidth is = ");
29
30 //iii) for 16-array PSK we have to consider  $P_{em}=4*P_b$ 
    . This is approximately equal to  $2*Q(\sqrt{2*\pi^2*}$ 
     $E_b*\log_2(16))/256*N$ ). This yields
31  $E_b=137.8*10^{-8}$ ;
32  $S_i3=E_b*\log_2(16)*R_M$ ;
33 disp('Watts',Si3," signal power required at the
    receiver = ");
34 Bt3= $R_M$ ;//normally
35 //But for PSK, as it is a modulated signal the
    required bandwidth is  $2Bt3$ .
36  $B_{psk}=2*(Bt3)$ ;
37 disp('hertz',Bpsk," Bandwidth is = ");

```

Chapter 14

OPTIMUM SIGNAL DETECTION

Scilab code Exa 14.1 Represent the given signal

```
1 //page 631
2 //prob 14.1
3 // the co-ordinates of the vectors are
4 // s1(1, -0.5), s2=(-0.5,1), s3=(0, -1), s4=(0.5,1)
5 x4=0:0.1:0.5;
6 y4=2*x4;
7
8 plot2d(x4,y4,style=1); // black line
9 x1=0:0.1:1;
10 y1=-0.5*x1;
11 plot(x1,y1,style=3); //blue line
```

Scilab code Exa 14.2 Example 2 of chapter 14

```
1 clc;
2 //page no. 650
```

```

3 // problem no. 14.2
4 // the two symbols to be transmitted are m1 and m2,
   the probabilities of which are not equal
5 // To design the optimum receiver we need to decide
   the threshold say d
6 // N be the given noise PSD,E the energy of the
   signal , assume N =1, E=1.5
7 Pm1=input("probability of symbol m1=");
8 Pm2=input("probability of symbol m2=");
9 //d is calculated as follows
10 N=1;
11 E=1.5;
12 d=(N/(4*sqrt(E)))*log(Pm2/Pm1);
13 disp(d,"the threshold is=");

```

Scilab code Exa 14.7 Example 7 of chapter 14

```

1 //page no 665
2 // example 14.7
3 // we know  $k_1P(m_1)=k_2P(m_2)$ , where  $k_1$  and  $k_2$  are the
   distances of the signals  $s_1$  and  $s_2$  resp.,hence  $k_1$ 
   + $k_2=d$ 
4 clc;
5 Pm1=input("probability of symbol m1=");
6 Pm2=input("probability of symbol m2=");
7 //assume d=1
8 d=1;
9 E1=(((Pm1)*((d^2)/2))+((Pm2)*((d^2)/2)));
10 disp(+ 'units ',E1,"mean energy of the first signal");
11 E2=Pm1*Pm2*(d^2);
12 disp(+ 'units ',E2,"mean energy of the second signal")
   ;
13 if(E1==E2)
14     disp("signals are equiprobable");
15     end

```


Chapter 15

INTRODUCTION TO INFORMATION THEORY

Scilab code Exa 15.1 problem1

```
1 //page no 687
2 // prob no 15.1
3 // Here we have given six messages. For 4-ary
  Huffman code, we need to add one dummy variable
  to satisfy the required condition of  $r+k(r-1)$ 
  messages.
4 //probabilities are given as  $p(1)=0.3$ ;  $p(2)=0.25$ ;  $p$ 
   $(3)=0.15$ ;  $p(4)=0.12$ ;  $p(5)=0.1$ ;  $p(6)=0.08$ ;  $p(7)=0.$ 
5
6 //The length L of this code is calculated as
7 clc;
8
9   n=input("enter the length of probability vector p,
  n= ");
10 p=[.3 .25 .15 .12 .1 .08 0]; // enter probabilities
  in descending order
11 l=[1 1 1 2 2 2 2]; // code length of individual
  message according to order
12 L=0;
```

```

13 for i=1:n
14     L=L+(p(i)*l(i));
15 end
16 disp('4-ary digits ',L,'Length = ');
17
18 // Entropy of source is calculated as
19 H=0;
20 for i=1:n-1//since the value of log(1/0) for the
    last entry is infinite which when multiply by 0
    gives result as 0
21     H=H+(p(i)*log(1/p(i)));
22 end
23 H1=H/log(4)
24 disp('4-ary units ',H1,'Entropy of source is , H = ')
    ;
25
26 // Efficiency of code is given as
27 N=H1/L;
28 disp(N,'Efficiency of code , N = ');

```

Scilab code Exa 15.2 problem2

```

1 // Page no 688
2 // Example no. 15.2
3 // N=1
4 //Here we have given two messages with probabilities
    m1=0.8 and m2=0.2 . Therefore , Huffman code for
    the source is simply 0 and 1.
5
6 //The length L of this code is calculated as
7 clear all;
8 clc;
9 close;
10 N=1;
11 p=[.8 .2]; //enter probabilities in descending order

```

```

12 n=length(p)
13 l=[1 1]; //code length of individual message
    according to order
14 L=0;
15 for i=1:n
16     L=L+(p(i)*l(i));
17 end
18 disp(L,"Length = ");
19
20 // Entropy of source is calculated as
21 H=0;
22 for i=1:n
23     H=H+(p(i)*log2(1/p(i)));
24 end
25 disp('bit',H,"Entropy of source is , H = ");
26
27 // Efficiency of code is given as
28 N1=H/L;
29 disp(N1,"Efficiency of code , N = ");
30
31 //for N=2
32 //There are four (2^N) combinations and their
    probabilities obtained by multiplying individuals
    probability.
33 //The length L of this code is calculated as
34 N=2;
35 p=[0.64 0.16 0.16 0.04]; //enter probabilities in
    descending order
36 n=length(p);
37 l=[1 2 3 3]; //code length of individual message
    according to order
38 L1=0;
39 for i=1:n
40     L1=L1+(p(i)*l(i));
41 end
42 L=L1/N; // word length per message
43 disp(L,"Length = ");
44

```

```

45 // Efficiency of code is given as
46 N2=H/L;
47 disp(N2,"Efficiency of code , N = ");
48
49
50 //for N=3
51 //There are eight (2^N) combinations and their
    probabilities obtained by multiplying individuals
    probability
52 //The length L of this code is calculated as
53 N=3;
54 p=[.512 .128 .128 .128 .032 .032 .032 .008]; //enter
    probabilities in descending order
55 n=length(p);
56 l=[1 3 3 3 5 5 5 5]; //code length of individual
    message according to order
57 L1=0;
58 for i=1:n
59     L1=L1+(p(i)*l(i));
60 end
61 L=L1/N; // word length per message
62 disp(L,"Length = ");
63
64 // Efficiency of code is given as
65 N3=H/L;
66 disp(N3,"Efficiency of code , N = ");

```

Scilab code Exa 15.4 problem4

```

1 // page no 702
2 // prob no 15.4
3 clc;
4 x0=(-1);x1=1; //given
5 y0=(-2);y1=2; //given
6 G=2; //gain of amplifier

```

```

7 //the probabilities are given as  $P(x)=1/2$  for  $|x|<1$  &
    $P(y)=1/4$  for  $|y|<2$  otherwise  $P(x)=P(y)=0$ .
8 // $P(x<1 \& -x<1)=1/2$ ;
9 // $P(y<2 \& -y<2)=1/4$ ;
10 // hence entropies are given as
11  $g1=(1/2)*\log_2(2)$ ;
12  $g2=(1/4)*\log_2(4)$ ;
13  $X=\text{integrate}('g1*1', 'x', x0, x1)$ ;
14  $Y=\text{integrate}('g2*1', 'y', y0, y1)$ ;
15  $\text{disp}('bit', X, 'entropy =')$ ;
16  $\text{disp}('bits', Y, 'entropy =')$ ;
17 //Here the entropy of random variable 'y' is twice
   that of the 'x'. This results may come as a
   surprise, since a knowledge of 'x' uniquely
   determines 'y' and vice versa, since  $y=2x$ . Hence
   , the average uncertainty of x and y should be
   identical.
18 // The reference entropy R1 for x is  $-\log dx$ , and
   The reference entropy R2 for y is  $-\log dy$  (in the
   limit as  $dx, dy \rightarrow 0$ ).
19 //  $R1 = \lim_{dx \rightarrow 0} -\log dx$ 
20 //  $R2 = \lim_{dy \rightarrow 0} -\log dy$ 
21 //and  $R1 - R2 = \lim_{dx, dy \rightarrow 0} \log(dx/dy) = \log(dy/dx)$ 
   =  $\log_2 2 = 1$  bit
22 //Therefore, the reference entropy of x is higher
   than the reference entropy for y. Hence we
   conclude that
23  $\text{disp}('if x and y have equal absolute entropies,$ 
   their relative (differential) entropies must
   differ by 1 bit');
```

Chapter 16

ERROR CORRECTING CODES

Scilab code Exa 16.1 Linear block codes

```
1 //page no 732
2 // example no 16.1.
3 //here generator matrix is given
4 clc;
5 G=[1 0 0 1 0 1;0 1 0 0 1 1;0 0 1 1 1 0];
6 d1=[1 1 1];
7 d2=[1 1 0];
8 d3=[1 0 1];
9 d4=[1 0 0];
10 d5=[0 1 1];
11 d6=[0 1 0];
12 d7=[0 0 1];
13 d8=[0 0 0];
14     c1=d1*G;
15     for i=1:6
16         if c1(i)==2 then
17             c1(i)=0;
18         end
19 end
```

```
20 c2=d2*G;
21     for i=1:6
22         if c2(i)==2 then
23             c2(i)=0;
24         end
25     end
26 c3=d3*G;
27     for i=1:6
28         if c3(i)==2 then
29             c3(i)=0;
30         end
31     end
32 c4=d4*G;
33     for i=1:6
34         if c4(i)==2 then
35             c4(i)=0;
36         end
37     end
38 c5=d5*G;
39     for i=1:6
40         if c5(i)==2 then
41             c5(i)=0;
42         end
43     end
44 c6=d6*G;
45     for i=1:6
46         if c6(i)==2 then
47             c6(i)=0;
48         end
49     end
50 c7=d7*G;
51     for i=1:6
52         if c7(i)==2 then
53             c7(i)=0;
54         end
55     end
56 c8=d8*G;
57     for i=1:6
```

```
58     if c8(i)==2 then
59         c8(i)=0;
60     end
61 end
62 disp("code words are given as")
63 disp(c1);
64 disp(c2);
65
66 disp(c3)
67 disp(c4)
68 disp(c5);
69 disp(c6);
70
71 disp(c7);
72
73 disp(c8);
```
