Scilab Textbook Companion for Digital Telephony by J. C. Bellamy¹

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Book Description

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Scilab numbering policy used in this document and the relation to the above book.

Exa Example (Solved example)

Eqn Equation (Particular equation of the above book)

AP Appendix to Example(Scilab Code that is an Appednix to a particular Example of the above book)

For example, Exa 3.51 means solved example 3.51 of this book. Sec 2.3 means a scilab code whose theory is explained in Section 2.3 of the book.

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Voice Digitization

Scilab code Exa 3.1 Program to calculate quantization interval and bits needed to encode each sample

```
1
2
3 //Example 3.1
4
5 //Page 101
6
7 sqr=30//SQR=30dB
8
9 q=1*10^[-(sqr-7.78)/20]
10
11 disp('Thus 13 quantization intervals arer needed for each polarity for a total of 26 intervals in all . The number of bitz required are determined as')
12
13 N=log2(26)
14
15 //Result
16
17 //q = 0.078 V
```

Scilab code Exa 3.2 Program to calculate the minimum bit rate for a PCM encoder must provide for high fidelity

```
1
3
  //Example 3.2
5 // Page 105
7 dr=40//dynamic range=400dB
9 SNR=50//signal to noise ratio =5 0dB
10
11 SQR=dr+SNR
12
13 n = [(SQR - 1.76)/6.02]
15 disp('This can be approximated to 15 bits per sample
      ')
16
17 disp('Assuming excess sampling factor using D-type
      channel, we choose sampling rate as 48KHz')
18
19 disp('Therefore required bit rate is')
20
21 15*48000
22
23 // Result
24
25 //720 \,\mathrm{kbps}
```

Scilab code Exa 3.4 Program to calculate how many bits per sample can be saved by using DPCM

```
1
2
   //Example 3.4
  //Page 128
7 \text{ w} = 800 / \text{Omega} = 800 \text{Hz}
   //x(t)=A \sin(2\pi i \cdot wt), equation for sine wave with
      maximum amplitude
10
  //x'(t)=A(2pi).w.cos(2pi.wt), diff w.r.t time
11
12
13
  (2*%pi)*800*(1/8000)
14
  //0.62831*a, x'(t)max
15
16
17 disp('savings in the bits per sample can be
      determined as ')
18
19 log2(1/0.628)
20
21 //Result
22
23 //0.67 bits
```

Digital Switching

Scilab code Exa 5.1 Program to find the idle path in a three stage 8192 line switch

```
1
  //Example 5.1
5 //Page243
7 //Refer to table 5.2 on page236
9 disp('From the table, space expansion factor of
     0.234 is 0.002. Hence the utilization of each
     interstage is given by')
10
11 0.1/0.234
12
13 p=1-[(1-0.427)^2]// probability that one of two
     links in series is busy
14
15 disp('Therefore, the expected number of paths to be
      tested are, ')
16
```

```
17  Np=[1-(0.672)^15]/(1-0.672)
18
19  // Result
20
21  // Only 3 of the 15 paths should be tested before an idle path is found
```

Scilab code Exa 5.2 Program to determine the implementation complexity of the TS switch

```
1
2
  //Example 5.2
  //Page 253
  //Refer to figure 5.19 on page 252
9 N=80//Number of links
10
11
  Nc=24//Number of control words
12
13 Nb1=7//Number of bits per control word
14
  Nb2=5//Number of bits per control word
15
16
  disp('The number of crosspoints in the space stage
      is')
18
19 Nx = N^2
20
21 disp('The total number of memory bits for the space
      stage control store is')
22
23 \, \text{Nbx} = \text{N} * \text{Nc} * \text{Nb1}
```

Scilab code Exa 5.3 Program to determine the implementation complexity of a 2048 channel

```
1
2
3
4 //Example 5.3
5
6 //Page 256
7
8 k=7//from equation 5.14 on page 256
9
10 disp('Using the value of k')
11
12 disp('Using the value of k, the number of crosspoint determined are')
13
14 2*7*16
15
16 disp('The number of bits of memory can be determined are')
```

Scilab code Exa 5.5 Program to determine the implementation complexity of a 131072 channel

```
1
2
3
   //Example 5.5
   //Page 261
8
10 n=32//binary w.r.t (N/2)^2
11
12 k=27//determined as a blocking probability of 0.0015
13
14 //Refer equations 5.18 and 5.19
15
16 Nx = [2*1024*27] + [27+(32^2)]
17
18 Nx = [2*1024*27] + [27*(32^2)]
19
20 Nbx = [2*27*128*32*5] + \{27*128*32*5\}
21
22 Nbt = [2*1024*128*8]
23
24 Nbtc = [2*1024*128*7]
```

```
25
26 cmplx=[Nx+{(Nbx+Nbt+Nbtc)/100}]
27
28 //Result
29
30 //Complexity is 138,854 equivalent crosspoint.
```

Digital Modulation and Radio Systems

Scilab code Exa 6.4 Program to determine system gain of 10Mbps 2Ghz digital microwave repeater using 4 PSK modulation

```
1
2
3 //Example 6.4
4
5 //Page 325
6
7 //Refer to figure 6.17 on page 300
8
9
10 disp('SNR detector is 3dB higher than Eb/N0, therefore')
11
12 snr=13.7//SNR=13.7dB
13
14 disp('Since 4 PSK modulation provides 2bps/Hz, the sampling rate is 5 MHz, which is Nqyuist rate, therefore')
15
```

```
16 a1=10*log10(12500000000000)
17
18 \quad a2=10*log10(1.3)
19
20 \quad A0 = a1 - 13.7 - 7 - 3 - a2
21
22 disp('At a carrier frequency of 2GHz, the wavelength
        is ')
23
24 (3*10^8)/(2*10^9)
25
26 FM=116+60+20*log10(0.15)-5-20*log10(4*%pi*5*10^4)//
      Fade Margin can be found by Equation 6.31
27
28 / Result
29 / A0 = 116 dB
30 / \text{wavelength} = 0.15 \text{ m}
31 / \text{Fade Margin} = 38.5 \text{ dB}
```

Network Synchronization Control and Management

Scilab code Exa 7.2 Program to determine relative accuracy of maintaining a mutual slip rate ojective of one slip in 20hrs

```
1
2
3  //Example 7.2
4
5  //Page 350
6
7
8  dF=(1/20*60*60)
9
10  dF=[1/(20*60*60)]
11
12  disp('Since there are 8000 frame per second, the relative accuracy is determined as')
13
14  ans=[dF/8000]
15
16  //Result
```

18 //Hence the clock must be accurate to 1.7 parts in 10^{9} .

Scilab code Exa 7.3 Program to determine the minimum and maximum input channel rate accommodated by an M12 multiplexer

```
1
2
3 //Example 7.3
5 / Page 354
7 disp("The maximum information rate per channel is
      determined as")
  Imax = [(6.312*288)/1176]
10
11 disp ('The minimum information rate per channel is
      determined as')
12
13 Imin = [(6.312*287)/1176]
14
15 disp('Since there are three possible combinations of
       two errors in the C bits, the probability of
      misinterpreting an S bit is')
16
17 3*(10^-6)^2
18
  1176/6.312//duration of each master frame
19
20
  [(3*10^-12)/(186*10^-6)]
21
22
23 //Result
24
25 //0.016*10^-6 misframes per second
```

Fiber Optic Transmission System

Scilab code Exa 8.1 Program to determine the loss limit and the multimode dispersion limit of a graded index FOC

```
//Caption:Program to determine the loss limit and
the multimode dispersion limit of a graded index
FOC

//Example 8.1

//Page 388

//Refer to figure 8.2 on page 385

Pin=42//input power = 42dB

A=3//attenuation

LL=(Pin/A)//Loss Limit
```

Scilab code Exa 8.2 Program to determine the loss limit and the chromatic dispersion limit of a high performance SMF FOC

```
1
2
  //Example 8.2
5 //Page 389
  //Refer figure 8.2 on page 385
  disp ('The attenuation of single-mode fibre operating
       at 1300nm is approximately 0.35dB/km. Thus,')
10
11 Pin=42//input power = 42dB
12
13 \quad A = 0.35
14
15 LL=(Pin/A)//Loss Limit
16
17 disp ('Using 250 Gbps-km as BDP of a silica single-
      mode fiber, the chromatic dispersion limit is
      determined as')
```

```
18
19 Cd=(250000/417)//Chromatic dispersion limit
20
21 //Result
22
23 //Loss Limit = 120 km
24
25 //Chromatic Dispersion Limit = 599.52 = 600 km
```

Scilab code Exa 8.3 Program to determine the BDP of SMF system and DS SMF system using DFB LD

```
1
2
  //Example 8.3
6 //Page 393
  //Refer to table 8.1 on page 392, also to figure 8.6
       on page 391
9
10
  smf = 16
11
   smf=16//dispersion co-efficient of SMF at 1550nm
12
13
  sw=0.4//spectral width of the source
14
15
  BDP = [250/(smf*sw)]/(assuming line code as NRZ)
16
17
  disp ('The BDP of the DS SMF system is determined as'
18
19
  smf=3.5//dispersion co-efficient of DS SMF at 1550nm
20
21
```

```
22 BDP=[250/(smf*sw)]//assuming line code as NRZ
23
24 //Result
25
26 //BDP = 39 Gbps=km (SMF)
27
28 //BDP = 179 Gbps-km (DS SMF)
```

Scilab code Exa 8.4 Program to determine the difference in wavelength of two optical signal

```
1
2
3
   //Example 8.4
5 / Page 402
  c=3*10^8//\text{speed} of light
9 wl=1500*10^-9/wavlength = 1500nm
10
11 f = [(3*10^8)/w1]
12
13 disp('Thus the upper and lower frequencies are
      determined as 200,001 and 199,999 GHz
      respectively. The corresponding wavelengths are')
14
15
   lam1 = [c/(199999*10^9)]
16
17 lam2 = [c/(200001*10^9)]
18
19 // Result
20
21 //The difference in wavelenghts is 0.015nm
```

Scilab code Exa 8.5 Program to determine the system gain

```
1
  //Example 8.5
3
  //Page 405
  //Refer to table 8.2 and figure 8.8 on page 394
9 dr = 565 // data rate
10
  wl=1550*10^-9/wavelength
11
12
13 disp('The use of 5B6B line code implies the line
      data rate is,')
14
15 565*(6/5)
16
17 / 678 \text{Mbps}
18
19 disp('The receiver sensitivity for 678 Mbps is
      determined from fig 8.8 or table 8.2 as ')
20
21 \text{ rsen} = -34.5
22
23 A=(-5-rsen)//system gain
24
  BDP = [500/(17*0.4)]
25
26
27 BDPs = [73.6/0.678]
28
  lossp = (0.2+0.2)*(65)
29
30
```

```
31
   lossm=A-lossp
32
   //Result
33
34
35
   //System gain = 29.5 dB
36
   //BDP = 73.6 \text{ Gbps}
37
38
   //BDP \text{ spacing} = 109 \text{ km}
39
40
  //Path Loss = 26 dB
41
42
43
   //Loss Margin = 3.5 dB
```

Scilab code Exa 8.6 Program to determine the range of SPE data rates that can be accommodated by the byte stuffing operation

```
1
  //Example 8.6
3
  //Page 415
5
  frames=4*9*87//Four SPE frames
7
  rate=8*frames*2000//normal rate SPE
9
10
11
12
  Rmin=8*3131*2000//minimum SPE rate
13
14 disp('When negative byte stuffing is used to
      accomodate a fast incoming SPE rate, 3133 bytes
      of data are transmitted in four frames. Thus, the
       highest slip rate is')
15
```

```
16 Rmax=8*3133*2000//maximum SPE rate
17
18 //Result
19
20 //Normal SPE rate = 50.112 Mbps
21
22 //Minimum SPE rate = 50.096 Mbps
23
24 //Maximum SPE rate = 50.128 Mbps
```

Digital Mobile Telephony

Scilab code Exa 9.1 Progam to determine the probability of maximum interference of a 64 channel CDMA system

```
1
2
3
  //Example 9.1
5 //Page 447
  disp ('The probability of 63 destructive interferers
     is merely the probability of occurence of 63
     equally likely binary events, ')
9 Pmax = (0.5) ^63 //maximum probability
10
11 disp('The value of a desired receive signal is the
      autocorrelation of a codeword with itself and can
       therefore be represented as a value of 64. ')
12
13 disp('The mean and varience of a sum of 63 such
      variable are 0 and 63, respectively. The signal-
     to-interference ratio is now determined as,')
14
```

```
15 a=[(64^2)/63]
16
17 SIR=10*log10(a)
18
19 //Result
20
21 //Signal to interference ratio = 18.1 dB
```

Data and Asynchronous Transfer Mode Network

Scilab code Exa 10.1 Program to determine the amount of transmission capacity

```
1
2
3 //Example 10.1
4
5 //Page 472
6
7 //(a)With link-by-link
8
9 frame=1000*10^-8
10
11 disp('The expected number of bits of transmission capacity required to retransmit is')
12
13 frame*1000
14
15 //(b)With end-to-end
16
17 frames=10*10^-5//corrupted frame
```

```
18
19 disp ('The expected number of bits of transmission
      capacity required is')
20
21
   frames *1000
22
23
  //(c) With bit error 10^{-5}
24
   ans1=1000*10^-5
25
26
  ans1=1000*10^-5*1000
27
28
29
  ans=10*10^-2*1000
30
31 //Result
32
33 //(a) 0.01  bit / link
34
35 //(b) 0.1  bit/link
36
37 //(c)1. 10 bits/link
38
39 //(c)2. 100 bits/link
```

Scilab code Exa 10.3 Program to determine the probability that the delay of an ATM voice cell

```
1
2
3 //Example 10.3
4
5 //Page 488
6
7 disp('Assuming the access link is 90% utilized on average.')
```

```
9 disp('The queuing theory is provided in Chapter 12.
      It involves determining the probability that the
      DSI access queue contains enough cells to
      represent 10 msec of transmission time')
10
11 tm = [(53*8)/(192*8000)]
12
13 disp('Therefore, 10 msec delay represents 10/0.276 =
        36.2 cell times.')
14
15 p=(0.9)*{%e^[-(1-0.9)*36.2]}//Refer to equation
      12.25 in chap 12
16
17 disp("Result")
18
19 \operatorname{disp}(\operatorname{P}(\&\operatorname{gt};10\operatorname{msec}) = 2.5\% delay will be displayed
      by more than 10 msec ")
```

Digital Subscriber Access

Scilab code Exa 11.1 Program to determine the distance limit imposed by the need to echo E bit in a BRI ST interface

```
1
  //Example 11.1
4 // Page 501
6 //Refer to figure 11.5 on page 500
8 disp('By seeing the figure, it can be seen that the
     minimum delay between a terminal transmitting D
     bit and receiving it back in the following E bit
     is seven bit times')
10 disp('At a 192 kbps data rate the duration of bit is
      5.2 usec. Thus, the total round trip propagation
      time is ')
11
12 7*5.2//usec
13
14 disp('Assuming no appreciable circuitry delays in
     the NT, ')
```

```
15
16 c=3*10^8// speed of light
17
18 Lmax = (36.4*10^-6)*(1/3)*c
19
20
  disp('Because round trip propagation involves both
      direction of transmission')
21
22 \quad Dmax = (1/2) * Lmax
23
24 disp("Result")
25
26 disp("Maximum length of wire(Lmax) = 3640 \text{ m} = 3.64
      km")
27
  disp ("Maximum distance (Dmax) = 1820 m = 1.82 km")
28
```

Scilab code Exa 11.2 Program to determine the theoretical maximum data rate of a prefectly equalized voiceband modem

```
//Example 11.2
//Page 513

disp('The signal-to-quantizing-noise ratio(SQR) is given in chap3 to be on the order of 36dB, which corresponds to power ratio of 3981.')

disp('Using this value in Shannon theorem for the theoretical capacity of a channel yield,')

SNR=3981
C=3100*[log2(1+SNR)]
```

```
13
14 disp("Result")
15
16 disp("data rate = 37 kbps")
```

Traffic Analysis

Scilab code Exa 12.1 Program to calculate how often do two calls arrive with less than 1 milisec between them

```
1
2 //Example 12.1
4 / Page 524
6 disp('The average arrival rate is')
8 \, lam = (3600/10000) / arrivals per sec
  disp('From equation 12.2, the probability on arrival
       in 0.01-\sec interval is')//equation on page 524
11
12 P0 = (\%e^-0.0278)
13
14 disp('Thus 2.7% arrivals occur withnin 0.01 sec of
      the pervious arrival. Since the arrival rate is
      2.78 arrivals per second, the rate of occurrence
      of intervarrival time less than 0.01 sec is')
15
16 2.78*0.027
```

```
17
18 disp("Result")
19
20 disp("0.075 times/sec")
```

Scilab code Exa 12.2 Program to calculate the probability that eight or more arrivals occur in an chosen 30 sec

```
1
  //Example 12.2
4 //Page 526
6 disp('The average number of arrivals in a 30 sec
      interval is,')
7
  lamt = 4*(30/60)
10 disp('The probability of eight or more arrivals is,'
      )
11
12 P0=1
13
14 P1 = [(2^1)/(1)]
15
16 P2 = [(2^2)/(1*2)]
17
18 P3 = [(2^3)/(1*2*3)]
19
20 P4 = [(2^4)/(1*2*3*4)]
21
22 P5 = [(2^5)/(1*2*3*4*5)]
23
24 P6 = [(2^6)/(1*2*3*4*5*6)]
25
```

```
26 P7=[(2^7)/(1*2*3*4*5*6*7)]
27
28 i=1-{(%e^-2)*[P0+P1+P2+P3+P4+P5+P6+P7]}
29
30 disp("Result")
31
32 disp("P(2) = 0.0011")
```

Scilab code Exa 12.3 Program to calculate the probability that a 1000 bit data block experiences exactly 4 errors while being transmitted over a link having error

```
1
2
  //Example 12.3
5 //Page 527
7 disp('Assuming inpendenterror, we can obtain the
      probability of exactly 4 errors directly from the
       Poisson distribution. The average number of
      errors is, ')
8
  lamt = [(10^3) * (10^-5)]
9
10
11 disp('Thus,')
12
13 P4 = \{ [(0.01^4)/(1*2*3*4)] *\%e^-0.01 \}
14
15 disp("Result")
16
17 disp("P(4) = 4.125*10^-10")
```

Scilab code Exa 12.4 Program to calculate the percentage of total traffic carried by first five ckt and traffic carried by all other remaining

```
1
2
  //Example 12.4
5 / Page 529
7 disp('The Traffic intensity of system is,')
8
9 A = 1 * 2
10
11 disp('The raffic intensity carried by i active ckt
      is exactly i erlangs. Hence the traffic carried
      by 1st 5 ckt is,')
12
13 P1 = [(1*2^1)/(1)]
14
15 P2 = [(2*2^2)/(1*2)]
16
17 P3 = [(3*2^3)/(1*2*3)]
18
19 P4 = [(4*2^4)/(1*2*3*4)]
20
21 P5 = [(5*2^5)/(1*2*3*4*5)]
22
23 A5 = \{ (\%e^-2) * [P1+P2+P3+P4+P5] \}
24
25 disp('All of remaining ckts carry,')
26
27 \text{ Ar} = 2 - 1.89
28
29 disp("Result")
30
31 disp("A(5) = 1.89 erlangs")
32
33 disp("A(remaining) = 0.11 erlangs")
```

Scilab code Exa 12.5 Program to calculate how much traffic can the trunk group carry

```
1
3
  //Example 5.5
  //Page 534
7 //Refer figure 12.5 on page 533
9 disp('From fig, it can be that the output circuit
      utilization for B=0.1 and N=24 is 0.8.')
10
11 N = 24
12
13 op=0.8
14
15 disp('Thus the carried traffic intensity is ')
16
17 N*op
18
19 disp('Since the blocking probability is 0.1, the
     maximum level of offered traaffic is,')
20
21 A = [19.2/(1-0.1)]
22
23 disp("Result")
24
25 disp("A = 21.3 erlangs")
```