

Directional Derivatives MCQ Questions

July 10, 2020

Questions

Q1. The slope in any direction pointed by the vector $\hat{\mathbf{u}}$ can be calculated using the directional derivative.

- a. True
- b. False

Q2. Find the gradient $\nabla f(2, 3)$, if $f(x, y) = x^3y$.

- a. $\nabla f(2, 3) = 24\mathbf{i} + 24\mathbf{j}$
- b. $\nabla f(2, 3) = 24\mathbf{i} + 8\mathbf{j}$
- c. $\nabla f(2, 3) = 8\mathbf{i} + 8\mathbf{j}$
- d. $\nabla f(2, 3) = 8\mathbf{i} + 24\mathbf{j}$

Q3. Find the unit vector in the direction $(1, 2)$.

- a. $\hat{\mathbf{u}} = \left\langle \frac{1}{\sqrt{5}}, \frac{2}{\sqrt{5}} \right\rangle$
- b. $\hat{\mathbf{u}} = \left\langle \frac{2}{\sqrt{5}}, \frac{1}{\sqrt{5}} \right\rangle$
- c. $\hat{\mathbf{u}} = \langle 1, 2 \rangle$
- d. $\hat{\mathbf{u}} = \langle \frac{1}{\sqrt{5}}, \frac{1}{\sqrt{5}} \rangle$

Q4. Find the directional derivative of $f(x, y) = x^3y$ in the direction $(1, 2)$ at the point $(2, 3)$.

- a. $D_u f(2, 3) = \frac{40}{\sqrt{5}}$
- b. $D_u f(2, 3) = 40$
- c. $D_u f(2, 3) = \frac{30}{\sqrt{5}}$

d. $D_u f(2, 3) = \sqrt{5}$

Q5. Find the directional derivative $D_u f$, when $\theta = 0$.

a. $D_u f = |\nabla f|$

b. $D_u f = -|\nabla f|$

Q6. Find the directional derivative $D_u f$, when $\theta = \pi$.

a. $D_u f = |\nabla f|$

b. $D_u f = -|\nabla f|$

Answer Key

Q1. True

Q2. $\nabla f(2, 3) = 24\mathbf{i} + 8\mathbf{j}$

Q3. $\hat{\mathbf{u}} = \left\langle \frac{1}{\sqrt{5}}, \frac{2}{\sqrt{5}} \right\rangle$

Q4. $D_u f(2, 3) = \frac{40}{\sqrt{5}}$

Q5. $D_u f = |\nabla f|$

Q6. $D_u f = -|\nabla f|$